

# KARPAGAM ACADEMY OF HIGHER EDUCATION

(Deemed to be University)
(Established under Section 3 of UGC Act, 1956)
Pollachi Main Road, Coimbatore – 641 021, Tamil Nadu

# **Department of Mathematics**

Subject : Mathematical Statistics Practical Semester III L T P C Subject Code : 17MMP311 Class : II M.Sc Mathematics 4 0 0 4

#### **List of Practical:**

- 1. Introduction to SPSS Package
- 2. Working with windows in SPSS
- 3. Defining variables in variable view window in SPSS
- 4. Drawing of graphs and diagrams in SPSS Package
- 5. Standard deviation for individual and discrete series using SPSS Package.
- 6. Standard deviation continuous series using SPSS Package.
- 7. Coefficient of variation for individual and discrete series using SPSS Package.
- 8. Calculation of Mean and variance for binomial distribution using SPSS Package.
- 9. Calculation of Mean and variance for Poisson distribution using SPSS Package.
- 10. Karl Pearson's Correlation using SPSS Package.
- 11. Rank Correlation Coefficient using SPSS Package.
- 12. Testing Hypothesis using t test in SPSS Package.
- 13. Testing Hypothesis using Z test in SPSS Package.
- 14. Testing Hypothesis using chi-square test in SPSS Package.
- **15**. Interpretation of results in the SPSS output viewer.

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# **DEPARTMENT OF MATHEMATICS**

# **M.Sc Mathematics**

Name of the Course : Mathematical Statistics

Course Code : 17MMP311

Year : II Year

Semester : III Semester

Class : II M.Sc Mathematics

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# **Department of Mathematics**

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Ex. No: 01

# INTRODUCTION TO SPSS PACKAGE

# **Objective**

To understand how SPSS package is useful for the purpose of data analysis.

#### Introduction

Originally it is an acronym of "Statistical Package for the Social Science" but now it stands for "Statistical Product of Service Solution".

One of the most popular statistical packages which can perform highly complex data manipulated and analysis with simple instruction.

#### The Four Windows

- Data Editor
- ❖ Output Viewer
- ❖ Syntax Editor
- Script Window

# The Basic Analysis of SPSS Frequencies

The Analysis produces frequency table showing frequency counts and percentage of the values of individual variable.

#### **Descriptive**

This analysis shows the maximum, minimum, mean and standard deviation of the variables.

# **Correlation and Linear Regression Analysis**

Association between correlation and linear regression estimates the co-efficient of the linear equation.

# Chi-Square, ANOVA, T-Test

Independence (cross table), Frequency (Goodness of fit) one way and two way ANOVA and test.

# **WORKING WITH WINDOWS IN SPSS**

# **Objectives**

To understand how the windows in SPSS work.

#### The Four Windows

**Data Editor** 

**Output Viewer** 

Syntax Editor

Script Window

#### **Data Editor**

Spread sheet like system for defining entering, editing and displaying data, extension of the saved file will be 'save'.

# **Output Viewer**

Displaying output and errors, extension of the saved file will be 'SPV'.

# **Syntax Editor**

Text editor for syntax composition extension of saved file will be 'SPS'.

# **Script Window**

To provides the opportunity to write full-blown programs in a basic like language. Tex editor for syntax composition extension of saved file will be 'SBS'.

#### WORKING WITH VARBIALE VIEW WINDOW IN SPSS

# **Objective**

To know how to define variables in the variable view in data editor view.

# **Opening SPSS**

Start  $\rightarrow$  All programs  $\rightarrow$  SPSS Inc  $\rightarrow$  SPSS.

There are two sheets in the window.

- Data View
- Variable View

#### **Data View Window**

The data view window.

This sheet is visible when you first open the data editor and this sheet contains the data.

Click on the tab labeled variable view.

#### Variable View Window

This sheet contains information about the data set that is stored with the data set.

#### Name

The first character of the variable name must be alphabetic.

Variable names must be unique, and have to be less than 64 characters.

Spaces are NOT allowed.

# **Type**

Click on the "type" box .The two basic types of variables that you will use are numeric and string. This column enables you to specify the type of variable.

#### Width

Width allows you to determine the number of character SPSS will allow to be entered for the variable.

# **Decimals**

Number of decimals.

It has to be less than or equal to 16.

#### Label

You can specify the details of the variable.

You can write characters with spaces upto 256 characters.

#### **Values**

This is used and to suggest which numbers represent which categories when the variable represents a category.

# **Defining The Value Label**

Click the cell in the value column.

For the value, and the label, you can put upto 60 characters.

After defining the values click add and then click OK.

# DRAWING OF GRAPHS AND DIAGRAMS IN SPSS PACKAGE

# **Objective**

To know how to draw graphs and diagrams in SPSS package.

# Algorithm

**Step 1:** Start  $\rightarrow$  All program  $\rightarrow$  SPSS Inc  $\rightarrow$  SPSS

**Step 2:** Enter the given data in the variable view.

**Step 3**: Click Analysis → Descriptive statistics → Frequency

**Step 4:** Click gender and put it into the variable box.

**Step 5:** Click chart  $\rightarrow$  Bar / Pie chart and continue.

**Step 6:** Finally click ok in the frequency box.

#### **Problem**

How would you put the following information into SPSS?

NAME	GENDER	HEIGHT
Juanita	2	5.4
Sally	2	5.3
Donna	2	5.6
Sabrin	2	5.7
a		
John	1	5.7
Mark	1	6
Eric	1	6.4
Bruce	1	5.9

Value 1: Represents MaleValue 2: Represents Female

# **SPSS Output**

# **Frequencies**

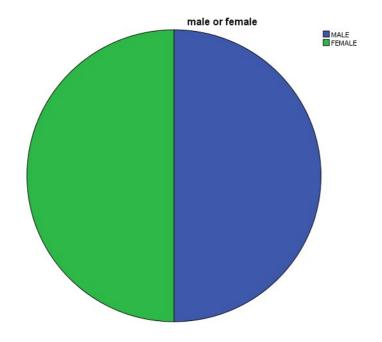
#### **Statistics**

Male or Female

N	Valid	8
	Missing	0

# Male or Female

				Valid	Cumulative
		Frequency	Percent	Percent	Percent
Valid	MALE	4	50.0	50.0	50.0
	FEMAL E	4	50.0	50.0	100.0
	Total	8	100.0	100.0	



# Frequencies

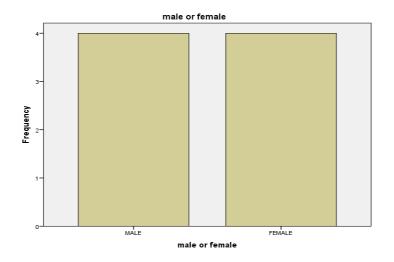
# Statistics

male or female

N	Valid	8
	Missing	0

# male or female

				Valid	Cumulative
		Frequency	Percent	Percent	Percent
Valid	MALE	4	50.0	50.0	50.0
	FEMALE	4	50.0	50.0	100.0
	Total	8	100.0	100.0	



# CALCULATION OF STANDARD DEVIATION FOR INDIVIDUAL AND DISCRETE SERIES USING SPSS PACKAGE

# **Objective**

To calculate the standards deviation for individual and discrete series using SPSS package.

# Algorithm

**Step 1:** Start  $\rightarrow$  all programs  $\rightarrow$  SPSS Inc  $\rightarrow$  SPSS

**Step 2:** Enter the given data in the variable view.

**Step 3:** Click analysis → descriptive statistics → frequency.

**Step 4:** click statistic option to choose the standard deviation  $\rightarrow$  continue and click ok.

**Step 5:** Finally we get the output.

#### **Individual Series**

# **Problem**

1. Calculate the standard deviation for the data given below using SPSS package.

X	25	18	27	10	30	42	20	53	20
---	----	----	----	----	----	----	----	----	----

# Formula:

Standard deviation=

# **Discrete Series**

2. Calculate the standard deviation for the following data using SPSS package.

No of Members	1	2	3	4	5	6	7	8	9	10	11	12
Frequency	1	3	5	6	10	13	9	5	3	2	2	1

# Formula:

Standard deviation=

#### 1. OUTPUT

#### No. of students

N	Valid	9
	Missing	0
Std. I	Deviation	13.14133

# 2. **OUTPUT:**

# No. of members

N	Valid	60
	Missing	0
Std.	Deviation	2.35038

# **Inference**

Standard deviation for the given data for individual series using SPSS is 13.141. Standard deviation for the given data for discrete series using SPSS is 2.350.

#### Ex. No: 06

#### STANDARD DEVIATION CONTINUOUS SERIES

# **Objective:**

To know how to calculate the standard deviation for continuous series using SPSS Package.

# Algorithm

**STEP 1:** Start  $\rightarrow$  All programs  $\rightarrow$  SPSS inc  $\rightarrow$  SPSS.

**STEP 2:** Enter the given data in the variable view.

**STEP 3:** Click analysis → Descriptive statistics → Frequencies.

**STEP 4:** Click statistic option to choose the mean and standard

Deviation → Continue and Click OK.

**STEP 5:** Finally we get the output.

#### **Problem**

Calculate the standard deviation for the following data using SPSS package

Income	0-10	10-20	20-30	30-40	40-50	50-60	60-70
Rs(100)	6	8	10	12	7	4	3

#### **Solution**

#### Given:

X	0-10	10-20	20-30	30-40	40-50	50-60	60-70
f	6	8	10	12	7	4	3

# Formula:

# Standard deviation=

#### **Calculation:**

X	f	m	m²	fm	fm
0-10	6	5	25	30	150
10-20	8	15	225	120	1800
20-30	10	25	625	250	62500
30-40	12	35	1225	420	14700
40-50	7	45	2025	315	14175
50-60	4	55	3025	220	12100
60-70	3	65	4225	195	12675

$$\Sigma f = 50$$
  $\Sigma f m = 1550$   $\Sigma f m^2 = 61850$ 

Standard deviation =

=

=

=16.613

Output

N	Valid	50
	Missing	0
Mean	_	31.00
Std. D	eviation	16.782

		Eroguenav	Dorgont	Valid	Cumulative
		Frequency	Percent	Percent	Percent
	5	6	12.0	12.0	12.0
	15	8	16.0	16.0	28.0
	25	10	20.0	20.0	48.0
Valid	35	12	24.0	24.0	72.0
v aliu	45	7	14.0	14.0	86.0
	55	4	8.0	8.0	94.0
	65	3	6.0	6.0	100.0
	Total	50	100.0	100.0	

# Inference

The standard deviation for the given data for continuous series using SPSS is 16.782.

# CALCULATION OF COEFFICIENT OF VARIATION FOR INDIVIDUAL SERIES

# **Objective**

To know how to calculate the coefficient of variation individual and discrete series using SPSS package.

# **Algorithm**

**Step 1**: Start  $\rightarrow$  All programs  $\rightarrow$  SPPS in C  $\rightarrow$  SPPS.

**Step 2:** Enter the given data in the variable view.

**Step 3:** Click Analyze → Descriptive Statistics → Frequencies.

**Step 4:** Click statistics option to choose the mean and standard deviation  $\rightarrow$  continue and click ok.

**Step 5:** Collect the mean and standard deviation values.

**Step 6:** Click Transforms → Compute variables.

**Step 7:** Enter the target values.

**Step 8:** Finally find the coefficient of variation.

**Step 9:** The result will be appeared in data view.

#### **Individual Series**

Calculate the coefficient of mean and standard deviation for the given data below:

X	25	18	27	10	30	42	20	53	20

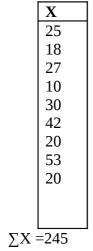
# **Formula**

Formula for individual value for mean

Mean = 
$$\sum X/N$$

Where N=number of items.

#### Calculation



Mean = 
$$245/9$$
 =  $27.22$ 

#### **Formula**

Standard deviation =  $\sqrt{\sum X-X}/n$ 

 $=\sqrt{1381.5556/9}$   $=\sqrt{153.5061778}$  =12.38976101

Standard deviation = 12.39

Coefficient of variation of individual series value = std dev /mean

= 12.39/27.22= 0.45518

# **OUTPUT**

# **Individual Series**

N Valid	9
Missing	0
Mean	27.2222
Std. Deviation	13.14133

Coefficient of variation is = 0.48

# **Discrete Series**

Calculate the coefficient of variation for the data given below using SPSS

No. of. Members	1	2	3	4	5	6	7	8	9	10	11	12
Frequency	1	3	5	6	10	13	9	5	3	2	2	1

# **Formula**

 $Mean = \sum f \mathbb{I} / \sum f$ 

# Calculation

X	F	<b>f</b> □			
1	1	1			
2	3	6			
3	5	15			
4	6	24			
5	10	50			
6	13	78			
7	9	63			
8	5	40			
9	3	27			
10	2	20			
11	2	22			
12	1	12			
$\Sigma f = 60$	∑f□ =358				

Mean = 
$$\sum f || / \sum f||$$
  
= 358 / 60 = 5.96667  
Mean = 5.9 (or) 6.0

# **Formula**

Standard deviation = $\sqrt{\sum f} \mathbb{I}^2 / \sum f - [\sum f \mathbb{I} / \sum f]^2$ 

# Calculation

X	$\mathbf{X}^2$	F	<b>f</b> □	<b>f</b> □²
1	1	1	1	1

2	4	3	6	12
3	9	5	15	45
4	16	6	24	96
5	25	10	50	250
6	36	13	78	468
7	49	9	63	441
8	64	5	40	320
9	81	3	27	243
10	100	2	20	200
11	121	2	22	242
12	144	1	12	144
		f□ = 58	$\sum \mathbf{f} \mathbb{D}^2 = 2$	2462

Standard deviation  $= \sqrt{2462/60} - [358/60]^2$   $= \sqrt{41.03} - [5.96]^2$   $= \sqrt{41.03} - 35.52$   $= \sqrt{5.5}$ = 2.347

Coefficient of variation of discrete series value = std.dev /mean = 2.347 / 5.967 = 0.3933

#### **OUTPUT**

# **Discrete Series**

N Valid	60
Missing	0
Mean	5.9667
Std. Deviation	2.35038

Coefficient of variation is = 0.39

#### Inference

The coefficient of variation for the given data for individual series is 0.48 The coefficient of variation for the given data for discrete series is 0.39

Ex. No: 08

# CALCULATING MEAN AND VARIANCE FOR BINOMIAL DISTRIBUTION USING SPSS PACKAGE

# **Binomial Distribution**

A Random Variable X is said to follow binomial distribution ,if its probability mass function is given by

```
P(X=x) = P(x) = \{ nC_x p^x q^{n-x} ; x=0,1,2,....n \}
= \{ 0 ; otherwise\}
```

Hence the two independent constant n and p are known as the 'Parameters' of the distribution .The distribution is completely determined if n and p are known X refer the number of successes.

#### **Problem**

Assuming that one in 80 births in a case of twins, calculate the probability of 2(or)more sets of twins on a day when 30 births occurs obtained by using the binomial distribution.

#### Solution

```
Probability of twins birth = p = 1/80
                                           =0.0125
                                         q = 1-p
                                           =1-0.0125
                                         q = 0.9875
                            n = 30
                        Mean = np
                             =30*0.0125
                             =0.375
                     Variance= npq
                              = 30*0.0125*0.9875
                              =0.3703125
Binomial distribution is given by
   P(x) = nc_x p^x q^{n-x}
   P(x \ge 2) = 1 - p(x < 2)
          =1-\{p(x=0)+p(x=1)\}
          =1-{30 C_0(0.0125)^0(0.9875)^{30}+30 C_1(0.0125)^1(0.9875)^{29}}
          =1-\{1*1(0.9875)^{30}+30(0.9875)^{29}(0.0125)\}
          =1-(0.6839+0.2597)
          =1-0.9436
  P(x \ge 2) = 0.0564
```

# CALCULATION OF MEAN AND VARIANCE FOR POISSON DISTRIBUTION USING SPSS PACKAGE

#### **Poisson Distribution**

Poisson distribution was discovered by a French Mathematician-Cum-Physicist Simeon Denis Poisson in 1837. Poisson distribution is also a discrete distribution. He derived it as a limiting case of binomial distribution for n-trials. The binomial distribution is  $(q+p)^n$ . The probability of X successes is given by  $P(X=x) = nC_x p^x q^{n-x}$ . If the number of trials n is very large and the probability of success 'p' is very small so that the product np=m is non-negative and finite. The probability of x success is given by,

$$e^{-m}m^x/x!$$
 for  $x=0,1,2,...$   
 $P(X=x)=$ 

1 Otherwise

Here 'm' is known as parameter of the distribution so that m>0.

#### **Problem**

Find the mean and variance to the following data which gives the frequency of the number of deaths due to horse kick in 10 corps per army per annum over twenty years.

Obtain by using Poisson distribution.

# **Solution**

Let us calculate the mean and variance of the given data

Xi	$\mathbf{f_i}$	$f_i x_i$	$f_i x_i^2$	
0	109	0	0	
1	65	65	65	
2	22	44	88	
3	3	9	27	
4	1	4	16	
Total	Total 200		196	

Mean, = 
$$\sum$$
 = 122/200 = 0.61  
Variance,  $\sigma^2 = \sum$  - ( = 196/200 –(0.61)<sup>2</sup> = 0.61  
Hence, Mean = Variance = 0.61

# CALCULATION OF KARL PEARSON CORRELATION USING SPSS PACKAGE

# **Objective**

To find the correlation coefficient by Karl Pearson Correlation Coefficient for the given variables using SPSS package.

# Algorithm

**STEP 1:** Start  $\rightarrow$  All Program  $\rightarrow$  SPSS Inc  $\rightarrow$  SPSS.

**STEP 2:** Enter the given data in the variable view.

**STEP 3:** Click analysis  $\rightarrow$  Correlate  $\rightarrow$  Bivariate click the variable X and Y And put it into the variable box.

**STEP 4:** Select the check box Karl Pearson Correlation and continue Then click OK in the frequency box.

**STEP 5**: Finally we get the Output.

# **Problem**

Calculate the Karl Pearson coefficient of correlation between two variables X and Y from the following data.

Height of	6	6	6	6	6	6	70	
Father	4	5	6	7	8	9	/0	
IIaiaht of Come	6	6	6	6	7	6	70	
Height of Sons	6	7	5	8	0	8	/2	

#### **Formula**

r =

	ι,	,		,		
X	d	dx	У	d	dy	dxdy
	X	2		У	2	
6	-3	9	6	-2	4	6
4			6			
6	-2	4	6	-1	1	2
5			7			
6	-1	1	6	-3	9	3
6			5			
6	0	0	6	0	0	0
7			8			
6	1	1	7	2	4	2

8			0			
6 9	2	4	6	0	0	0
9			8			
7	3	9	7	4	16	12
0			2			

$$\sum dx^{2} = 28$$

$$\sum dy^{2} = 34$$

$$\sum dxdy = 25$$

$$r =$$

$$=$$

$$r = 0.81$$

# **OUTPUT**

# **Correlations**

		Height of	Height of
		Father	Sons
Height of Father	Pearson Correlation	1	.810*
	Sig. (2-tailed)		.027
	N	7	7
Height of Sons	Pearson Correlation	.810*	1
	Sig. (2-tailed)	.027	
	N	7	7

<sup>\*.</sup> Correlation is significant at the 0.05 level (2-tailed).

# Inference

 $0.75 \le 0.8 < 1$  strong positive relationship existing between the height of father and the height of son.

# CALCULATION OF RANK CORRELATION USING SPSS PACKAGE

**Aim:** To calculate the given value by Rank correlation coefficient in the package.

# **Algorithm**

**STEP 1:** Start  $\rightarrow$  All program  $\rightarrow$  SPSS in c  $\rightarrow$  SPSS.

**STEP 2:** Enter the given data in the variable view.

**STEP 3:** Click analyze → Correlation → Bivariate.

**STEP 4:** Click the variable X and Y, Put it into the variable box.

**STEP 5:** Select Spearman check box and continues, then click ok in the Bivariate box.

**STEP 6:** Finally we get the output.

# Calculation

Calculate rank correlation coefficient for the following data using SPSS package.

First exam Score(X)	8	9	7	6	5	8	7	85
	8	5	0	0	0	0	5	
Second exam Score	8	9	8	5	4	8	8	72
(Y)	4	0	8	5	8	5	2	

# **Formula**

=1-

Where D = Different between X and Y

N = Number of observation

#### Calculation

X	Y	RX	RY	D=(RX-RY)	D=(
88	8	2	4	-2	4
	4				
95	9	1	1	0	0
	0				
70	8	6	2	4	16
	8				
60	5	7	7	0	0
	5				
50	4	8	8	0	0
	8				
80	8	4	3	1	1
	5				
75	8	5	5	0	0
	2				
85	7	3	6	-3	9
	2				

=1-

- =1-
- =1-
- =1-
- =1-0.3571 = 0.6429

# **SPSS OUTPUT**

# **Correlations**

_				
			first exam	second exam
			score x	score y
Spearman's rho	first exam score x	Correlation	1.000	642
		Coefficient	1.000	.643
		Sig. (2-tailed)		.086
		N	8	8
	second exam score	Correlation	642	1 000
	y	Coefficient	.643	1.000
		Sig. (2-tailed)	.086	
		N	8	8

# Inference

0.25 0.6429 0.75, moderate degree positive relationship existing between the first exam score and second exam score.

# TESTING HYPOTHESIS USING T-TEST IN SPSS PACKAGE

# Aim

Testing Hypothesis using t-test in SPSS package.

# **Algorithm**

**STEP 1**: Start All Programs SPSS in C SPSS

**STEP 2:** Enter the given data in the variable view

**STEP 3:** Click Analyze Compare means One Sample T-test

**STEP 4**: Click the Variable X and put it into the variable box

**STEP 5:** Click options Confidence integral percentage at 95% continue

**STEP 6:** Put test value 10 ok

**STEP 7:** Finally we get the out put

# **Problem**

Certain pesticide is packed in to bags be a machine a random sample of 10 days is drawn and their contents are found to weight (in kg) as follows

5	4	5	4	4	4	4	4	4	4
0	9	2	4	5	8	6	5	9	5

Test if the average packing can be taken to be 50 kg.

# **Solution**

# **Null Hypothesis**

H□:µ=50 kgs in the average packing in 50 kgs

# **Alternative Hypothesis**

H□:≠50 Kgs [Two Tailed]

# **Level Of Significance**

Let  $\alpha = 0.05$ 

#### Calculation

$$= 47.3$$

$$=$$
  $s = 2.668$ 

50	2.7	7.29
49	1.7	2.89
52	4.7	22.09
44	-3.3	10.89
45	-2.3	5.29
48	0.7	0.49
46	-1.3	1.69
45	-2.3	5.29
49	1.7	2.89
45	-2.3	5.29
	64.	1

= =

= 3.2

# **Expected Value**

= follows t-distribution with (10-1) degrees of freedom is 2.262.

# **OUTPUT**

**One-Sample Statistics** 

			Std.	Std. Error			
	N	Mean	Deviation	Mean			
weights of pesticide	10	47.3000	2.66875	.84393			

**One-Sample Test** 

	Test Value = 10							
		95% Confidence Interv						
			Sig. (2-	Mean	the Difference			
	t	df	tailed)	Difference	Lower	Upper		
weights of pesticide	44.198	9	.000	37.30000	35.3909	39.2091		

# Inference

Since. is rejected at 5% level of significance and we conclude that the average packing cannot be taken to be 50 kgs.

# TESTING HYPOTHESIS USING Z TEST IN SPSS PACKAGE

# Aim

Testing hypothesis using z test in SPSS package.

# Algorithm

**STEP 1:** Start  $\rightarrow$  All Program  $\rightarrow$  SPPS in C  $\rightarrow$  SPPS.

**STEP 2:** Enter the given data in the variable view.

**STEP 3:** Click Analyze  $\rightarrow$  Compare mean  $\rightarrow$  One sample t test.

**STEP 4:** Click the variable x and put it into the variable box.

**STEP 5:** Click Option → Confidence interval percentage at 95% → Continue.

**STEP 6:** Put test value 100 Ok.

**STEP 7:** Finally we get the output.

# Testing Hypothesis Using Z Test in SPSS Package

#### **Problem**

The life time fluorescent bulbs of 100 samples are given below. Test the samples for the expected mean life time of 1600 for 5% level of significance.

1640	161	163	1672
	5	8	
1650	162	163	1632
	5	9	
1660	163	165	1653
	5	9	
1670	164	167	1671
	5	9	
1680	165	168	1673
	5	9	
1690	166	167	1534
	5	3	
1465	167	155	1644
	5	6	
1475	168	145	1486
	5	8	
1487	145	146	1476
	3	8	
1495	146	156	1566
	8	7	
1515	149	164	1498
	7	8	
1525	148	162	1493
	8	3	
1535	152	167	1463
	6	4	
1545	153	168	1532
	9	4	
1555	149	167	1573
	1650 1660 1670 1680 1465 1475 1487 1495 1515 1525 1535	1650       162         1660       163         1670       164         5       165         1680       165         1690       166         5       167         1465       167         5       148         1475       168         3       145         4       3         1495       146         8       1515         1525       148         8       153         1545       153         6       1545         1545       153         9       9	1650     162     163       1660     163     165       1670     164     167       5     9       1670     164     167       5     9       1680     165     168       5     9       1690     166     167       5     3       1465     167     155       6     1475     8       1487     145     146       3     8       1495     146     156       8     7     8       1515     149     164       7     8       1525     148     162       8     3       1535     152     167       6     4       1545     153     168       9     4

		9	3	
1590	1565	157	149	1593
		7	4	
1600	1575	146	159	1461
		9	1	
1610	1585	156	159	1582
		9	3	
1620	1595	158	157	1536
		9	3	
1630	1605	159	158	1476
		9	2	

# **Solution**

Given n=100,  $\mu$ =1600.

# **Null hypothesis**

$$H_0: \mu = 1600.$$

(i.e) there is no significant difference between the sample mean and population mean.

# Alternative hypothesis

 $H_1: \mu \neq 1600$ .(two tailed)

# Level of significance:

Let []=0.05

# **Calculation of statistics**

# **Expected value**

$$Z_e = Z_0 = \sim N(0,1) = 1.96 \text{ for } \square = 0.05$$

#### **SPSS OUTPUT:**

**One-Sample Statistics** 

			Std.	Std. Error
	N	Mean	Deviation	Mean
z test	100	1570.73	73.496	7.350

**One-Sample Test** 

	Test Value = 100					
					95% Confider	nce Interval of
			Sig. (2-	Mean	the Dif	ference
	t	Df	tailed)	Difference	Lower	Upper
z test	200.109	99	.000	1470.730	1456.15	1485.31

#### **Inference**

Since  $Z_0 > Z_e$ . We reject the null hypothesis at 5% level of significance and we conclude that there is a significant difference between the sample mean and the population mean.

Mathematical Statistics - Practical	<b>2017 Batch</b>

Ex: No: 14

# TESTING HYPOTHESIS USING CHI-SQUARE TEST IN SPSS PACKAG

# **Objective**

Testing hypothesis using chi -square test in SPSS package.

# **Algorithm**

**Step 1:** start  $\rightarrow$  all programs  $\rightarrow$  SPSS in c  $\rightarrow$  SPSS

**Step 2:** Enter the given data in the variable view.

**Step 3:** Click the data  $\rightarrow$  weight cases and select the frequency variable.

**Step 4:** Click analysis  $\rightarrow$  nonparametric test  $\rightarrow$  one sample test  $\rightarrow$  select automatically compare Observed data to hypothesized and click run.

**Step 5:** Finally we get the output.

#### **Problem**

For goodness of fit the following information is derived from the record of an employee payroll the absenteeism of the employees during the weekdays is given below

DAYS	ABSENCE
Monday	12
Tuesday	10
Wednesday	7
Thursday	8
Friday	13

Test the distribution of absenteeism is uniform across the week days.

# **Solution**

# **Null hypothesis**

 $H \square : \mu = \mathbb{k}$ 

There is no significance difference between during the absenteeism of weekdays.

# Alternative hypothesis

H1:μ≠k

There is a significance difference between the absenteeism of weekdays.

#### Level of significance

Let  $\alpha$ =0.05

# Calculation of $\chi^2$ statistics

$$\chi^2 =$$

0	E	O-E	$(O-E)^2$	$(O-E)^2/E$
12	10	2	4	0.4
10	10	0	0	0
7	10	-3	9	0.9
8	10	-2	4	0.4
13	10	3	9	0.9

# **Degrees of freedom**

$$df = (r-1)(c-1)$$

$$= (5-1)(2-1)$$
 d

# **Expected value:**

$$\chi^{2}_{e} = 9.488$$
 $\chi^{2}_{o} < \chi^{2}_{e}$ 
2.6<9.488

# **OUTPUT**

# **Test Statistics**

	no of absent
Chi-Square	2.600a
df	4
Asymp. Sig.	.627

a. 0 cells (0.0%) have expected frequencies less than 5. The minimum expected cell frequency is 10.0.

# **Inference**

Since  $\chi^2_o < \chi^2_e$  we accept the null hypothesis at 5% level of significance and we conclude that there is no significance difference between during the absenteeism of weekdays.

# INTERPERTATION OF RESULT IN THE SPSS OUTPUT VIEWER

Representation of data in the form of graphs and diagrams for use for better decision making going through graph and diagram one can easily understand the pattern of data over a period of time and one easily identify the up and downs of the data points by which the decision making is easy.

Standard deviation is measure of the dispersion which is mostly used. It is shows the amount of variation amount the shows in a particular variable. The compare two difference variable coefficient of variation is used with help of standard deviation and coefficient of variation decision making is easy.

When we get the measure of central value are closed each other for difference variables decision making is with the complicated foe such situation standard deviation. It the standard deviation values are consistence in natural. If the standard deviation values is more is shows that the values of seated one to another.

Binomial and Poisson are discrete are discrete probability distribution which gives an idea about how values of distributed .Binomial distribution is when we get only two possible outcomes and Poisson distribution is similar binomial and it is which rare events. The Binomial distribution the mean is calculated by  $\mu$ = n p and variance = n pq. But in Poisson distribution the mean and variance  $\lambda$ = n p.

To measure the relationship between the variable correlation coefficient is used. There is different method but most popularly Karl Pearson correlation coefficient is used for measuring the relationship between quantitative data and spearman Rank correlation is used for measuring relationship between qualitative data. The correlation coefficient (value denoted by r) ranges between -1 to 1.

The relationship between r-value from the following table.

r value	Relationship
1	Perfect positive
≥0.75 and<1	Strong positive
$\geq$ 0.25 and <0.75	Moderate degree positive
>0 and < 0.25	Low degree positive
0	No correlation
$\geq$ - 0.25 and $\leq$ 0	Low degree negative
$\geq$ - 0.75 and $\leq$ - 0.25	Moderate degree negative
$\geq$ - 0.75 and $\leq$ -1	Strong negative
-1	Perfect negative

In Hypothesis test if the asymptotic significance value is less than the level of significance value ( $\alpha$ ).we accept the null hypothesis otherwise we reject the null hypothesis.