14BEME501, 14BEAE501, 14BEEC501, 14BECS601 NUMERICAL ANALYSIS 3 1 0 4 100

INTENDED OUTCOMES:

- To make the students acquainted with the basic concepts in numerical methods and their uses.
- To impart the procedure for solving different kinds of problems occur in engineering numerically.

UNIT-I TYPES OF ERRORS, SOLUTION OF ALGEBRAIC EQUATIONS Different types of errors- Newton Raphson method, Modified Newton Raphson method, Method of false position.

UNIT -II SOLUTION OF ALGEBRAIC SIMULTANEOUS EQUATIONS

Gauss - Jordan elimination, Cholesky method, Crout's method, Gauss - Jacobi method, Gauss - Seidel method. Matrix Inverse by Gauss - Jordan method.

Eigenvalues and eigenvectors: Power method for finding dominant eigenvalue and inverse power method for finding smallest eigenvalue, Jacobi method for symmetric matrices.

UNIT- III FINITE DIFFERENCES AND INTERPOLATION

Finite difference operators $-E, \Delta, \nabla, \delta, \mu, D$ - Interpolation-Newton-Gregory forward and backward interpolation, Lagrange's interpolation formula, Newton divided difference interpolation formula.

UNIT- IV DIFFERENTIATION AND INTEGRATION

Numerical differentiation using Newton-Gregory forward and backward polynomials. Numerical Integration-Gaussian quadrature, Trapezoidal rule and Simpson's one third rule.

Ordinary differential equations: Taylor series method, Euler and Modified Euler method, (Heun's method). Runge-Kutta method, Milne's method, Adams-Moulton method, Solution of boundary value problems of second order by finite difference method.

UNIT- V PARTIAL DIFFERENTIAL EQUATIONS

Classification of partial differential equations of second order. Liebmann's method for Laplace equation and Poisson equation, Explicit method and Crank - Nicolson method for parabolic equations. Explicit method for hyperbolic equations.

MATLAB : Matlab – Toolkits – 2D Graph Plotting – 3D Graph Plotting.

TEXT BOOKS:

S. No.	Author(s) Name	Title of the book	Publisher	Year of Publication
1	Burden, R. L. and Faires, T. D	Numerical Analysis	Thomson Asia Pvt. Ltd., Singapore.	2002
2	Curtis F. Gerald and Patrick O. Wheatley	Applied Numerical Analysis	Pearson Education, South Asia	2009

REFERENCES:

S. No.	Author(s) Name	Title of the book	Publisher	Year of Publication
1	Steven C.Chapra and Raymond P.Canale	Numerical Methods for Engineers with Software and Programming Applications	Tata McGraw Hill, New Delhi	2004
2	Gerald,C.F. and Wheatley,P.O	Applied Numerical Analysis	Pearson Education Asia, New Delhi	2002
3	Balagurusamy.E	Numerical Methods	Tata McGraw Hill Pub.Co.Ltd, New Delhi.	2009

WEBSITES:

- 1. www.nr.com
- 2. www.numerical-methods.com
- 3. www.math.ucsb.edu
- 4. www.mathworks.com

KARPAGAM ACADEMY OF HIGHER EDUCATION



COIMBATORE-21. FACULTY OF ENGINEERING II B.E COMPUTER SCIENCE AND ENGINEERING (2014 Batch)

NUMERICAL ANALYSIS LESSON PLAN

14BEME501, 14BEAE501, 14BEEC501, 14BECS601

S.NO.	TOPICS TO BE COVERED	HOUR(S)	
	UNIT I : TYPES OF ERRORS, SOLUTION OF ALGEBRAIC EQUATIONS		
	Different types of errors	1	
	Different types of errors	1	
	Newton Raphson method	1	
	Newton Raphson method	1	
Unit-I	Tutorial 1 Newton Raphson method	1	
	Modified Newton Raphson method	1	
	Modified Newton Raphson method	1	
	Method of false position	1	
	Method of false position	1	
	Tutorial 2 Method of false position	1	
	TOTAL	10	
	EQUATIONS	1	
	Gauss - Jordan elimination	1	
	Cholesky method	1	
	Crout's method	1	
	Gauss - Jacobi method	1	
	Gauss - Seidel method	1	
	Tutorial 3 Gauss - Jordan elimination, Cholesky method, Crout's method, Gauss - Jacobi method	1	
	Matrix Inverse by Gauss - Jordan method	1	
	Matrix Inverse by Gauss - Jordan method	1	
	Power method for finding dominant eigenvalue	1	
	Inverse power method for finding smallest eigenvalue	1	
	Power method for finding dominant eigenvalue and inverse power method for finding smallest eigenvalue	1	
	Tutorial 4 Power method for finding dominant eigenvalue and inverse power method for finding smallest eigenvalue	1	

	Jacobi method for symmetric matrices	1
	Jacobi method for symmetric matrices	1
	TOTAL	14
	UNIT III : FINITE DIFFEREN	
	INTERPOLATION	
	Finite difference operators $-E, \Delta, \nabla, \delta, \mu, D$	1
	Finite difference operators $-E, \Delta, \nabla, \delta, \mu, D$	1
	Interpolation	1
	Newton-Gregory forward and backward interpolation	1
	Newton-Gregory forward and backward interpolation	1
Unit-III	Tutorial 5 Finite difference operators – $E, \Delta, \nabla, \delta, \mu, D$ - Interpolation-Newton-	1
	Gregory forward and backward interpolation	
	Lagrange's interpolation formula	1
	Lagrange's interpolation formula	1
	Newton divided difference interpolation formula	1
	Newton divided difference interpolation formula	1
	Tutorial 6 Lagrange's interpolation formula, Newton divided difference interpolation formula.	1
	TOTAL	11
Unit-IV	UNDIFINERENTIATION AND INTEGRATION Numerical differentiation using Newton-	
	Gregory forward and backward polynomials	1
	Gaussian quadrature	1
	Trapezoidal rule	1
	Sumpson's one third rule	
	Simpson's one third rule	1
	Tutorial 7 Numerical differentiation using Newton-Gregory forward and backward polynomials. Numerical Integration-Gaussian quadrature, Trapezoidal rule and Simpson's one third rule.	1
	Tutorial 7 Numerical differentiation using Newton-Gregory forward and backward polynomials. Numerical Integration-Gaussian quadrature, Trapezoidal rule and Simpson's one	1
	Tutorial 7 Numerical differentiation using Newton-Gregory forward and backward polynomials. Numerical Integration-Gaussian quadrature, Trapezoidal rule and Simpson's one third rule.	
	Tutorial 7 Numerical differentiation using Newton-Gregory forward and backward polynomials. Numerical Integration-Gaussian quadrature, Trapezoidal rule and Simpson's one third rule. Taylor series method	1
	Tutorial7NumericaldifferentiationusingNewton-Gregoryforwardandbackwardpolynomials.NumericalIntegration-Gaussianquadrature,Trapezoidalrule andSimpson's onethird rule.Taylor seriesmethodEuler and ModifiedEulermethodRunge-KuttamethodRunge-Kuttamethod	1
	Tutorial 7 Numerical differentiation using Newton-Gregory forward and backward polynomials. Numerical Integration-Gaussian quadrature, Trapezoidal rule and Simpson's one third rule. Taylor series method Euler and Modified Euler method Runge-Kutta method	1 1 1
	Tutorial7NumericaldifferentiationusingNewton-Gregoryforwardandbackwardpolynomials.NumericalIntegration-Gaussianquadrature,Trapezoidalrule andSimpson's onethird rule.Taylor seriesmethodEuler and ModifiedEulermethodRunge-KuttamethodRunge-Kuttamethod	1 1 1 1

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	Runge-Kutta method, Milne's method, Adams-		
	Moulton method		
	Solution of boundary value problems of second	1	
	order by finite difference method.	1	
	Solution of boundary value problems of second	4	
	order by finite difference method.	1	
	TOTAL	14	
	UNIT V : PARTIAL DIFFERENTIAL EQUA		
	Classification of partial differential equations of		
	second order	1	
	Liebmann's method for Laplace equation	1	
	Liebmann's method for Laplace equation	1	
	Liebmann's method for Poisson equation	1	
	Liebmann's method for Poisson equation	1	
	Tutorial 9 Liebmann's method for Laplace		
	equation and Poisson equation	1	
	Explicit method for parabolic equations	1	
Unit-V	Crank - Nicolson method for parabolic	1	
	equations	1	
	A		
	Crank - Nicolson method for parabolic	1	
	equations	1	
	Explicit method for hyperbolic equations	1	
	Tutorial 10 Explicit method and Crank -		
	Nicolson method for parabolic equations.	1	
	Explicit method for hyperbolic equations.	-	
	TOTAL	11	
		50	
	GRAND TOTAL	+ 10	
	1	• 10	

STAFF

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Unit - I Solutions of Equations and Eigen Value Problems. () Write the gr eqn f(x) = 0 into the form $x = \sigma(x)$ Itenative Method : () Write the given $\chi = \varphi(\chi)$ form $\chi = \varphi(\chi)$ (2) Assume that $\chi = \chi_0$ be the proof q the given eqn (3) The joint approximation to the proof is qn by $\chi_1 = \varphi(\chi_0)$ $\eta = \chi_2 = \varphi(\chi_1)$ $\eta = \chi_3 = \varphi(\chi_2)$ $= \Re(x_{n-1})$ $= \Re(x_n)$ $= \Re(x$ ● Find the most of the equation as x = 3x - 1, using iteration Method soln (2004 0 - 3x + 1) f(x) = (05x - 3x + 1)f(0) = 00 - 3(0) + 1 = 2 -> + ve f(1) = 00 - 3(1) + 1 = 0 - 3(1) + 1 - 2. The groot lies between 0 and 1 3

The opn can be written an

$$(3 \times -3 \times +1) = 0$$

 $-3 \times - (3 \times -1)$
 $3 \times -3 \times +1$
 $x = \frac{1}{3} \int 1 + (3 \times)$
 $1 \times (x) = \frac{1}{3} \int 1 + (3 \times)$
 $q'(x) = -\frac{1}{3} \sin x$
 $|q'(x)| = \frac{1}{3} \sin x$
 $|q'(x)| = \frac{1}{3} \sin x$
 $|q'(x)| = \frac{1}{3} \sin x$
 $1q'(x)| = \frac{1}{3} \sin x$
 $1q'(x) = \frac{1}{3} (1 + (3 \times)) = \frac{1}{3} (1 + (3 \times))$
 $x_1 = q(x_0) = \frac{1}{3} (1 + (3 \times)) = \frac{1}{3} (1 + (3 \times))$
 $x_2 = q(x_1) = \frac{1}{3} (1 + (3 \times)) = \frac{1}{3} (1 + (3 \times))$
 $x_2 = q(x_2) = \frac{1}{3} (1 + (3 \times)) = \frac{1}{3} (1 + (3 \times))$
 $x_3 = 0.66073$
 $x_3 = 0.6073$
 $x_4 = q(x_3) = \frac{1}{3} (1 + (3 \times)) = \frac{1}{3} (1 + (3 \times))$
 $x_4 = 0.6067$

$$\begin{aligned} &\mathcal{X}_{5} = \varphi(x_{4}) = \frac{1}{3} (1 + 01 \times 4) = \frac{1}{3} (1 + 03 \circ 6067) \\ &\mathcal{X}_{5} = 0.6072 \\ &\mathcal{X}_{6} = \varphi(x_{5}) = \frac{1}{3} (1 + 01 \times 5) = \frac{1}{3} (1 + 01 \circ 607) \\ &\mathcal{X}_{6} = \varphi(x_{5}) = \frac{1}{3} (1 + 01 \times 5) = \frac{1}{3} (1 + 01 \circ 607) \\ &\mathcal{X}_{7} = \varphi(x_{5}) = \frac{1}{3} (1 + 01 \times 6) = \frac{1}{3} (1 + 01 \circ 607) \\ &\mathcal{X}_{7} = 0.6071 \\ &\mathcal{X}_{7} = 0.6071 \\ &\vdots. The stequired store is 0.6071. \end{aligned}$$

(read) $\varphi(x) = \sqrt{2x+3} = (2x+3)^{1/2}$ (cros) $\varphi'(x) = \frac{1}{2}(2x+3)^{-1/2} \frac{1}{2}$ $|q'(x)| = |(2x+3)^{-1/2}|$ $|q'(2)| \neq |q'(3)| < |$ $\begin{aligned} \text{Take} \quad \begin{array}{l} \mathcal{N}_{0} &= 2.5 \\ \mathcal{N}_{1} &= \varphi(\mathbf{x}_{0}) = \sqrt{2\mathbf{x}_{0}+3} \pm \sqrt{2(2.5)+3} = 2.8284 \\ \mathcal{N}_{2} &= \varphi(\mathbf{x}_{1}) = \sqrt{2\mathbf{x}_{1}+3} = \sqrt{2(2.8284)+3} = 2.9422 \\ \mathcal{N}_{2} &= \varphi(\mathbf{x}_{1}) = \sqrt{2\mathbf{x}_{1}+3} = \sqrt{2(2.9422)+3} = 2.9807 \\ \mathcal{N}_{3} &= \varphi(\mathbf{x}_{2}) = \sqrt{2\mathbf{x}_{3}+3} = \sqrt{2(2.9422)+3} = 2.99807 \\ \mathcal{N}_{4} &= \varphi(\mathbf{x}_{2}) = \sqrt{2\mathbf{x}_{3}+3} = \sqrt{2(2.9807)+3} = 2.9936 \\ \mathcal{N}_{5} &= \varphi(\mathbf{x}_{4}) = \sqrt{2\mathbf{x}_{4}+3} \pm \sqrt{2(2.9807)+3} = 2.9977 \\ \mathcal{N}_{5} &= \varphi(\mathbf{x}_{4}) = \sqrt{2\mathbf{x}_{4}+3} \pm \sqrt{2(2.9936)+3} = 2.99972 \end{aligned}$ $\mathcal{H}_{6} = \varphi(\mathcal{H}_{5}) = \sqrt{2\mathcal{H}_{5}^{+3}} = \sqrt{2(2.979)+3} = 2.999.3$ $\begin{aligned} &\mathcal{H}_{7} = \varphi(\mathcal{H}_{6}) = \sqrt{2\mathcal{H}_{6}^{+3}} = \sqrt{2(2.9993)} = 2.9998 \\ &\mathcal{H}_{8} = \varphi(\mathcal{H}_{7}) = \sqrt{2\mathcal{H}_{7}^{+3}} = \sqrt{2(2.9998)} = 2.99999 \end{aligned}$ $\mathcal{H}_{g} = \varphi(x_{g}) = \sqrt{2x_{g}+3} = \sqrt{2(2\cdot9999)+3} = 2\cdot9999$ The required groot is 2.9999

(3) Solve 1 by "tertation Method
$$\Im x - \log_{10} x = 7$$

Bolo
 $\Im x - \log_{10} x - 7 = 0$
 $\varphi(x) = \Im x - \log_{10} x - 9$
 $\varphi(x) = \Im x - \log_{10} x - 9$
 $\varphi(x) = \Im x - \log_{10} x - 9$
 $\varphi(x) = \Im x - \log_{10} x - 9$
 $\varphi(x) = -3 \cdot 3010 - 5 - 92$
 $\varphi(x) = -1 \cdot 4717 - 5 - 92$
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 $\varphi(x) = -1 \cdot 4717 - 5 - 92$
 $\varphi(x) = -1 \cdot 4717 - 5 - 92$
 $\varphi(x) = -1 \cdot 4717 - 5 - 92$
 $\varphi(x) = -1 \cdot 109_{10}^{x}$
 $\varphi(x)$

 $\chi_{2} = \varphi(\chi_{1}) = \frac{1}{2} [109_{10}\chi_{1} + 7]$ = 1 [log 3.7782 +7] 2= 3.7886 x3 = q(x2) = 1/2 [109, x2 + 7] = 1 [109 3.7886+7] x3 = 3.7892 $x_{4} = \varphi(x_{3}) = \frac{1}{2} \left[\log_{10} x_{3} + 7 \right]$ = 1 [109 10 3.7892 +7] 24=3.7893 $x_{5} = \varphi(x_{4}) = \frac{1}{2} [\log_{10} x_{4} + 7]$ Bal = 1 [log 3.7892+7] ×5=3.7893 The magnined root is 3.7.893 H. W find the negative proof q the eqn $\chi^3 - 2\chi + 5 = 0$

Grauss Jordan Method 2x - y + 6z = 22 x + 7y - 3z = -225x - 2y+3z = 18 Soln $-2 \quad 1 \quad -6 \quad | \quad -22 \quad]R_1 - 2 - 2R_1 \\ R_2 - 2R_1 \\ R_2 - 2R_2 \\ R_3 - 2R_2 \\ R_3 - 2R_3 \\$.

-> R, X-5-26 3 0 5/35/2 0 -5 0 R2 -2 $R_2 - 2R_2 \times \frac{7}{5}$ $R_1 - 2R_1 \times \frac{13}{5}$ 0 オニ3. -2 y = $\chi + 3y + 3z = 16$ $\chi + 4y + 3z = 18$ $\chi + 3y + 4z = 19$ Solve 2

3 3 b 343 (A,B] = 33 16/3 C 2 0 3 0 3 C 3 2 2 2 0 0 3 x = 1, y = 2,Z=3

Solve 10x + y + z = 12 2x + 10y + z = 13 x + y + 5z = 7soln $\begin{bmatrix} A, B \end{bmatrix} = \begin{bmatrix} 10 & 1 & 1 & 12 \\ 2 & 10 & 1 & 13 \\ 1 & 1 & 5 & 7 \end{bmatrix}$ X=1, y=2, 223

49 0 53 49 2365 R,-Ra 10/9 3/4 8 0 0 北 R2 $R_3 -$ 98 99 49 0 0 O a 0 C B 4

Inverse of a Matin Gauss Jordan Method invour of the Method. Jordan Grauss ung colo 3 - 3 100-2

100 Ri-3 -1/20 Ri-3 -1/20 Ri-3 1 4 6 6 3/2 1/2 0/2 $R_{1} - 2R_{1} - R_{2}$ $R_{3} - 2R_{3} - R_{2}$ 2 $-\frac{1}{12}$ 0 $R_1 - 2R_1/6$ $-\frac{1}{12}$ 0 $R_2 - 2R_2/2$ $-\frac{1}{12}$ $-\frac{1}{14}$ $R_2 - 2R_3/2$ 06 1/2 1/6 1/4 5/12 -1/4 -1/1 -1/4 $R_1 \rightarrow R_1 - R_2$ $R_2 \rightarrow R_2 - R_3$ 0-0 16 0 3 1 22 0 -5/4 -1/4 -3/4 0 -1/4 -1/4 -1/4 R,-7R, × 6 3 -5/4 -1/4 -1/4 -1/4 is 1 7

he Matrin Grauss Jordan the inverse the 8 find D 3-15 -521 using Method. Soln 3 15 6 0 -15 -5 0 C 64 0 0 3 B 3 10 C 3 2 57 0

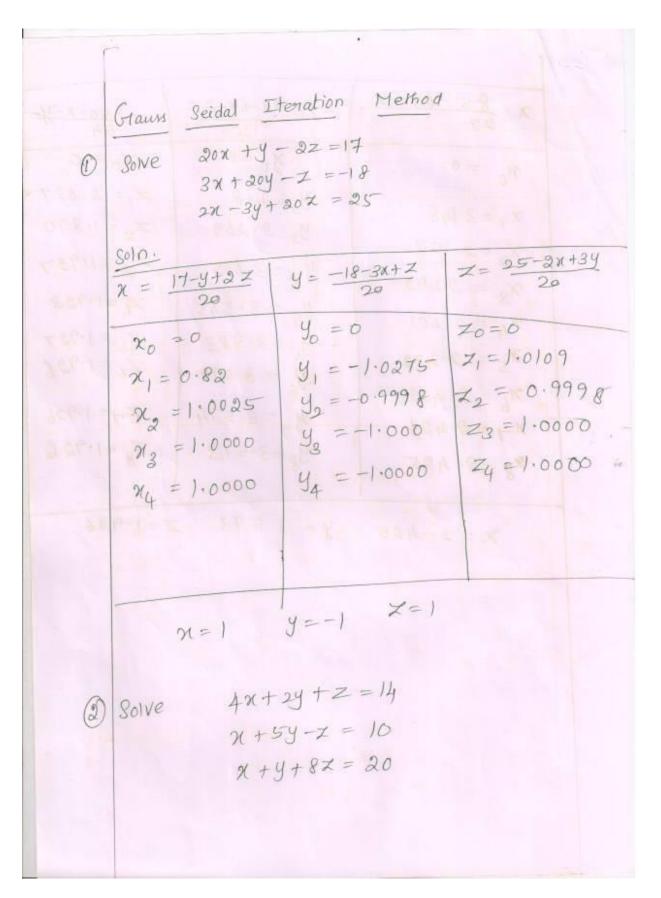
 $= \frac{1}{10} \begin{bmatrix} 6 & 1 & 0 \\ 1 & 0 \\ 1 & 0 \\ 1 & 10 \\ 1 &$ 0 0 1 35 1 -3 R - 28; 10 0 29/2 1/0 3 R - 28; 0 1 1/3 0 3/3 R - 28; = [I] (A) $= inverse q A is <math>\begin{pmatrix} 85 \\ 93 \\ 37 \\ 290 \\ 62 \\ 1 \\ -30 \\ 37 \\ 37 \\ -37 \\$

٠ find Jordan Method Grauss re onve he 3 C Solo 2 0 0 C B 0 D 2

 $\begin{bmatrix} -1 & 0 & 1 & -1 & 0 & 0 \\ -1 & 0 & 1 & -1 & 0 & 0 \\ \hline -3 & 5 & 0 & R_{-} & -2 \\ \hline 0 & 1 & -2 & 3 & 5 & R_{-} & -2 \\ \hline 0 & 0 & 1 & -2 & 3 & 5 & R_{-} & -2 \\ \hline 0 & 0 & 1 & -2 & 3 & 5 & R_{-} & -2 \\ \hline 0 & 0 & 1 & -2 & 3 & 5 & R_{-} & -2 \\ \hline 0 & 0 & 1 & -2 & 3 & 5 & R_{-} & -2 \\ \hline 0 & 0 & 1 & -2 & 3 & 5 & R_{-} & -2 \\ \hline 0 & 0 & 1 & -2 & 3 & 5 & R_{-} & -2 \\ \hline 0 & 0 & 1 & -2 & 3 & 5 & R_{-} & -2 \\ \hline 0 & 0 & 1 & -2 & 3 & 5 & R_{-} & -2 \\ \hline 0 & 0 & 1 & -2 & 3 & 5 & R_{-} & -2 \\ \hline 0 & 0 & 1 & -2 & 3 & 5 & R_{-} & -2 \\ \hline 0 & 0 & 1 & -2 & 3 & 5 & R_{-} & -2 \\ \hline 0 & 0 & 1 & -2 & 3 & 5 & R_{-} & -2 \\ \hline 0 & 0 & 1 & -2 & 3 & 5 & R_{-} & -2 \\ \hline 0 & 0 & 1 & -2 & 3 & 5 & R_{-} & -2 \\ \hline 0 & 0 & 0 & 1 & -2 & 3 & 5 & R_{-} & -2 \\ \hline 0 & 0 & 0 & 1 & -2 & 3 & 5 & R_{-} & -2 \\ \hline 0 & 0 & 0 & 1 & -2 & 3 & 5 & R_{-} & -2 \\ \hline 0 & 0 & 0 & 1 & -2 & 3 & 5 & R_{-} & -2 \\ \hline 0 & 0 & 0 & 1 & -2 & 3 & 5 & R_{-} & -2 \\ \hline 0 & 0 & 0 & 1 & -2 & 3 & 5 & R_{-} & -2 \\ \hline 0 & 0 & 0 & 1 & -2 & 3 & 5 & R_{-} & -2 \\ \hline 0 & 0 & 0 & 1 & -2 & 3 & 5 & R_{-} & -2 \\ \hline 0 & 0 & 0 & 1 & -2 & 3 & 5 & R_{-} & -2 \\ \hline 0 & 0 & 0 & 1 & -2 & 3 & 5 & R_{-} & -2 \\ \hline 0 & 0 & 0 & 0 & 1 & -2 & 0 \\ \hline 0 & 0 & 0 & 0 & 0 & -2 \\ \hline 0 & 0 & 0 & 0 & 0 & -2 \\ \hline 0 & 0 & 0 & 0 & 0 & -2 \\ \hline 0 & 0 & 0 & 0 & 0 & -2 \\ \hline 0 & 0 & 0 & 0 & 0 & -2 \\ \hline 0 & 0 & 0 & 0 & 0 & -2 \\ \hline 0 & 0 & 0 & 0 & 0 & 0 \\ \hline 0 & 0 & 0 & 0 & 0 & 0 \\ \hline 0 & 0 & 0 & 0 & 0 & 0 \\ \hline 0 & 0 & 0 & 0 & 0 & 0 \\ \hline 0 & 0 & 0 & 0 & 0 & 0 \\ \hline 0 & 0 & 0 & 0 & 0 & 0 \\ \hline 0 & 0 & 0 & 0 & 0 & 0 \\ \hline 0 & 0 & 0 & 0 & 0 & 0 \\ \hline 0 & 0 & 0 & 0 \\ \hline 0 & 0 & 0 & 0 & 0 \\ \hline$ $= \begin{bmatrix} 1 & 0 & 0 & 1/10 & 3/10 & 5 \\ 0 & 1 & 0 & 21/20 & -7/20 & -3/5 \\ 0 & 0 & 1 & -9/10 & 3/10 & 1/5 \\ = \begin{bmatrix} 1/A \end{bmatrix} & \begin{bmatrix} 1/A \\ -9/10 & 3/10 & 5 \\ -9/10 & -7/20 & -7/50 \\ -9/10 & 3/10 & 5 \\ -9/10 & 3/10 & 5 \\ -9/10 & 3/10 & 5 \end{bmatrix}$

X= 24-X-39 y=35-4x-2x $\chi = \frac{32 - 4y + z}{28}$ 70=0 Y0 = 0 No = 0 y,=2.0588 Z,=2.4 21 = 1.1429 y2=1.3597 Z= 1.6681 2=0.9345 yg=1.5564 Z2 = 1.898 2 = 1.0082 $M_4 = 0.9883$ $Y_4 = 1.4935$ $Z_4 = 1.832 = 3$ x5-=0.9949 JS-=1.514 Z5=1.8531 $\varkappa_6 = 0.9931$ $y_6 = 1.5058$ $z_6 = 1.847$ $\chi_7 = 0.9937$ $y_7 = 1.5074$ $Z_7 = 1.8490$ 28 = 0.9936 Y8 = 1.5069 Z8 = 1.8484 - 21g = 0.9936 Jg = 1.5070 Zg = 1.8486 2210=0.9936 410=1.5070 Z10=1.8485 Z1=1-8485n = 0.9936 Y = 1.5070 . The Soln is x = 0.9936 y=1.5076 z=1.8485 Solve 27x + 6y - Z = 85 (3) 2+4+547=110 6x + 15y + 2 = 72

Z= 110-X-Y 20=0 20=0 210 = 0 Y,=4.8 Z,=2.037 x, = 3.148 y2=3.269 Z2=1.890 2=2.157 Y3=3.685 Z3=1.937 N3 = 2.492 94 = 2.401 75= 2.432 N6 = 2. 423 27=3.574 Zy=1.926 03 po- xy = 2.426 yg=3.573 Zg=1.926 a 2. 425 y= 3.573 Z=1.926, x=2.425



y= 72-6x-22 Z= 110-x-y 15 Z= 10-x-y 54 $\mathcal{H} = \frac{85 - 6y + Z}{27}$ y0=0 Z0=0 No = 0 $\chi_1 = 3.148$ $\chi_2 = 2.432$ $\chi_3 = 2.426$ $\chi_4 = 2.426$ 94 = 3.573 Z4=1.926 $\chi = 2.4 26$ $\gamma = 3.573$ $\chi = 1.926$

$$\begin{aligned} \begin{array}{c} \begin{array}{c} \hline Figen \quad Values \quad \underline{q} \quad \underline{a} \quad Matrix \quad \underline{by} \quad powen \quad Method \\ \hline \hline Find \quad Hie \quad numerically \quad largest \quad eigen \quad Value \\ \hline q \quad A = \begin{bmatrix} 25 & 3 & 0 \\ 2 & 0 & -4 \end{bmatrix} \quad and \quad ids \quad Corresponding \\ eigen \quad Vector \quad by \quad powen \quad method, \quad baking \quad Hie \\ \hline initial \quad eigen \quad Vector \quad as \quad (1 \ 0 \ 0)^T \quad (upto \\ Hince \quad decimal \quad places \\ \hline Hince \quad decimal \quad places \\ \hline \end{array} \end{aligned}$$

$$\begin{aligned} \begin{array}{c} \hline A = \begin{pmatrix} 25 & 1 & 2 \\ 1 & 3 & 0 \\ 2 & 0 & -4 \end{pmatrix} \\ \hline A \times_1 = \begin{pmatrix} 1 \\ 0 \\ 1 & 3 & 0 \\ 2 & 0 & -4 \end{pmatrix} \\ \hline A \times_2 = \begin{pmatrix} 25 & 1 & 2 \\ 1 & 3 & 0 \\ 2 & 0 & -4 \end{pmatrix} \begin{pmatrix} 0 & 0 \\ 0 \end{pmatrix} = \begin{pmatrix} 25 \\ 1 \\ 2 \end{pmatrix} = 25 \begin{pmatrix} 0 & 0 \\ 0 & 0 \\ 0 & 08 \end{pmatrix} = 25 \times \frac{1}{2} \\ \hline 0 & 08 \\ 0 & 0667 \end{pmatrix} \\ \hline = 25 \cdot 2 \times \frac{3}{3} \\ \hline \end{array} \\ \hline \end{array} \\ \hline \end{array}$$

I.

$$A X_{\mu} = \begin{pmatrix} 25 & i & 2 \\ 1 & 3 & 0 \\ 2 & 0 & -4 \end{pmatrix} \begin{pmatrix} 0 & 0450 \\ 0 & 0698P \\ 0 & 069PP \end{pmatrix} = \begin{pmatrix} 25 & 1926 \\ 1 & 1935 \\ 0 & 0685 \\ \end{pmatrix} = 25 \cdot 1824 \begin{pmatrix} 1 \\ 0 & 0457 \\ 0 & 0685 \\ \end{pmatrix} = 25 \cdot 1824 \begin{pmatrix} 1 \\ 0 & 0457 \\ 1 & 13353 \\ 1 & 17240 \\ \end{pmatrix}$$

$$= 25 \cdot 1824 \begin{pmatrix} 1 \\ 0 & 0457 \\ 0 & 0685 \\ \end{pmatrix} = 25 \cdot 1824 \begin{pmatrix} 1 \\ 0 & 0457 \\ 0 & 0685 \\ \end{pmatrix} = 25 \cdot 1824 \begin{pmatrix} 1 \\ 0 & 0457 \\ 0 & 0685 \\ \end{pmatrix}$$

$$Dominant eigen Value \lambda = 25 \cdot 1821 \\ 0 & 0685 \\ 0 & 0685 \\ \end{pmatrix}$$

$$Determine by Powen ruemod the larger value and the conseptending largest eigen Value and the conseptending largest eigen Value A = 25 \cdot 1824 \begin{pmatrix} 1 \\ 0 & 0457 \\ 0 & 0685 \\ 0 & 0685 \\ \end{pmatrix}$$

$$\begin{array}{l} y_{0}b_{0} \\ X_{1} = \int_{0}^{1} \int_{0}^{1$$

$$\begin{aligned} A \times_{q} &= \begin{pmatrix} 0 \cdot 4 | 72 - \\ 5 - 0 \cdot 86 \cdot 9 \\ | 1 + 74 \cdot 7 \cdot 3 \end{pmatrix} = 11 \cdot 74 \cdot 75 \begin{pmatrix} 0 \cdot 0 \cdot 3 \cdot 5 \cdot 7 \\ 0 \cdot 4 \cdot 3 \cdot 3 \cdot 0 \end{pmatrix} = 11 \cdot 6 \cdot 96 \cdot f \begin{pmatrix} 0 \cdot 0 \cdot 28 \cdot 6 \\ 0 \cdot 4 \cdot 25 \cdot 0 \end{pmatrix} = 11 \cdot 6 \cdot 96 \cdot f \begin{pmatrix} 0 \cdot 0 \cdot 28 \cdot 6 \\ 0 \cdot 4 \cdot 25 \cdot 0 \end{pmatrix} = 11 \cdot 6 \cdot 96 \cdot f \begin{pmatrix} 0 \cdot 0 \cdot 28 \cdot 6 \\ 0 \cdot 4 \cdot 25 \cdot 0 \end{pmatrix} = 11 \cdot 6 \cdot 96 \cdot f \begin{pmatrix} 0 \cdot 0 \cdot 28 \cdot 6 \\ 0 \cdot 4 \cdot 25 \cdot 0 \end{pmatrix} = 11 \cdot 6 \cdot 96 \cdot f \begin{pmatrix} 0 \cdot 0 \cdot 28 \cdot 6 \\ 0 \cdot 4 \cdot 25 \cdot 0 \end{pmatrix} = 11 \cdot 6 \cdot 18 \begin{pmatrix} 0 \cdot 0 \cdot 24 \cdot 0 \\ 0 \cdot 4 \cdot 25 \cdot 0 \end{pmatrix} = 11 \cdot 6 \cdot 18 \begin{pmatrix} 0 \cdot 0 \cdot 27 \cdot 3 \\ 0 \cdot 4 \cdot 25 \cdot 0 \end{pmatrix} = 11 \cdot 6 \cdot 5 \cdot 6 \cdot 5 \cdot 6 \cdot 5 \cdot 6 \cdot 7 \cdot 7 \cdot 7 = 11 \cdot 6 \cdot 5 \cdot 6 \cdot 7 \cdot 7 \cdot 7 \cdot 7 \cdot 6 \cdot 5 \cdot 6 \cdot 7 \cdot 7 \cdot 7 \cdot 7 \cdot 7 = 11 \cdot 6 \cdot 5 \cdot 6 \cdot 7 \cdot 7 \cdot 7 \cdot 7 \cdot 7 = 11 \cdot 6 \cdot 5 \cdot 7 \cdot 7 \cdot 7 \cdot 7 \cdot 7 = 11 \cdot 6 \cdot 5 \cdot 6 \cdot 7 \cdot 7 \cdot 7 \cdot 7 = 11 \cdot 6 \cdot 6 \cdot 7 \cdot 7 \cdot 7 \cdot 7 = 11 \cdot 6 \cdot 6 \cdot 7 \cdot 7 \cdot 7 = 11 \cdot 6 \cdot 6 \cdot 7 \cdot 7 \cdot 7 = 11 \cdot 6 \cdot 6 \cdot 7 \cdot 7 \cdot 7 = 11 \cdot 6 \cdot 6 \cdot 7 \cdot 7 \cdot 7 = 11 \cdot 6 \cdot 6 \cdot 7 \cdot 7 \cdot 7 = 11 \cdot 6 \cdot 6 \cdot 7 \cdot 7 \cdot 7 = 11 \cdot 6 \cdot 6 \cdot 7 \cdot 7 \cdot 7 = 11 \cdot 6 \cdot 7 \cdot 7 \cdot 7 = 11 \cdot 6 \cdot 7 \cdot 7 \cdot 7 = 11 \cdot 6 \cdot 7 \cdot 7 \cdot 7 = 11 \cdot 6 \cdot 7 \cdot 7 \cdot 7 = 11 \cdot 6 \cdot 7 \cdot 7 \cdot 7 = 11 \cdot 6 \cdot 7 \cdot 7 \cdot 7 = 11 \cdot 6 \cdot 7 \cdot 7 \cdot 7 = 11 \cdot 6 \cdot 7 \cdot 7 \cdot 7 = 11 \cdot 6 \cdot 7 \cdot 7 \cdot 7 = 11 \cdot 6 \cdot 7 \cdot 7 \cdot 7 = 11 \cdot 6 \cdot 7 \cdot 7 \cdot 7 = 11 \cdot 6 \cdot 7 \cdot 7 = 11 \cdot 6 \cdot 7 \cdot 7 \cdot 7 = 11 \cdot 6 \cdot 7 \cdot 7 \cdot 7 = 11 \cdot 6 \cdot 7 \cdot 7 = 11 \cdot 7 = 11 \cdot 6 \cdot 7 = 11 \cdot 6 \cdot 7 = 11 \cdot 6 \cdot 7 = 11 \cdot 7 = 11 \cdot 6 \cdot 7 = 11 \cdot 6 \cdot 7 = 11 \cdot 6 \cdot 7 = 11 \cdot 7 = 11 \cdot 6 \cdot 7 = 11 \cdot 7 = 11 \cdot 6 \cdot 7 = 11 \cdot 6 \cdot 7 = 11 \cdot 6 \cdot 7 = 11 \cdot 7 = 11 \cdot 6 \cdot 7 = 11 \cdot 7 = 11 \cdot 6 \cdot 7 = 11 \cdot 7 = 11 \cdot 6 \cdot 7 = 11 \cdot 6 \cdot 7 = 11 \cdot 7 = 11 \cdot 6 \cdot 7 = 11 \cdot 7 = 11 \cdot 6 \cdot 7 = 11 \cdot 7 = 11 \cdot 6 \cdot 7 = 11 \cdot 7 = 11 \cdot 6 \cdot 7 = 11 \cdot 7$$

$$A_{X_{1}} = \begin{pmatrix} 1 & 6 & 1 \\ 0 & 0 & 24 & 9 \\ 0 & 0 & 24 & 9 \\ 0 & 0 & 24 & 9 \\ 0 & 0 & 24 & 9 \\ 0 & 0 & 24 & 9 \\ 0 & 0 & 24 & 9 \\ 0 & 0 & 24 & 9 \\ 0 & 0 & 24 & 9 \\ 0 & 0 & 24 & 9 \\ 0 & 0 & 24 & 9 \\ 0 & 0 & 24 & 9 \\ 0 & 0 & 24 & 9 \\ 0 & 0 & 24 & 9 \\ 0 & 0 & 24 & 9 \\ 0 & 0 & 24 & 9 \\ 0 & 0 & 0 & 24 \\ 0 & 0 & 0 & 1 \\ 1 & 2 & 0 \\ 0 & 0 & 3 & 9 \\ 1 & 2 & 0 \\ 0 & 0 & 0 & 3 \\ 1 & 2 & 0 \\ 0 & 0 & 0 & 3 \\ 1 & 2 & 0 \\ 0 & 0 & 0 & 3 \\ 1 & 2 & 0 \\ 1 & 2 & 0 \\ 1 & 2 & 0 \\ 0 & 0 & 0 & 0 \\ 1 & 2 & 0 \\ 0 & 0 & 0 & 0 \\ 1 & 2 & 0$$

$$A \times_{5^{-}} = \begin{pmatrix} +3 \cdot 97 \ 0 \cdot 6 \\ 1 \cdot 99 \ 0 \cdot 2 \end{pmatrix} = 3 \cdot 970 \cdot 6 \begin{pmatrix} 0 \cdot 502 \\ 0 \cdot 92 \\ 0 \end{pmatrix} = 3 \cdot 970 \cdot 6 \begin{pmatrix} 0 \cdot 4997 \\ 0 \end{pmatrix} = 4 \cdot 0072 \times_{7}$$

$$A \times_{7} = \begin{pmatrix} 3 \cdot 9982 \\ 1 \cdot 9994 \\ 0 \end{pmatrix} = 3 \cdot 9782 - (0 \cdot 500 \ 0) = 3 \cdot 9787 \times_{7}$$

$$A \times_{7} = \begin{pmatrix} 4 \\ 2 \\ 0 \end{pmatrix} = 4 \begin{pmatrix} 1 \\ 0 \\ 0 \end{pmatrix} = 4 \times_{9}$$

$$A \times_{9} = \begin{pmatrix} 4 \\ 2 \\ 0 \end{pmatrix} = 4 \begin{pmatrix} 1 \\ 0 \\ 0 \end{pmatrix}$$

$$A \times_{9} = \begin{pmatrix} 4 \\ 2 \\ 0 \end{pmatrix} = 4 \begin{pmatrix} 1 \\ 0 \\ 0 \end{pmatrix}$$

$$Do \text{Minant eigen Value in } = 4$$

$$Grresponding eigen Vector in \begin{pmatrix} 1 \\ 0 \\ 0 \end{pmatrix}$$

<u>Eigen Value q a Matrix by Jacobi</u> Method for Symmetric Matrix Let $P = \begin{pmatrix} Coro & -\sin O \\ \sin O & \end{pmatrix}$ $Q = \frac{1}{2} \tan^{-1} \left(\frac{2a_{ij}}{a_{ij} - a_{jj}} \right)$ D=PAP D Apply Jacobi process to evaluate Apply Jacobi process to evaluate the eigen values and eigen vectors the eigen Matrix (5001 9 the Matrix (5001 0-20) 105) Solo A = (5 -2 0) Solo The langest non diagonal element is a13 = 3, = 1 a. = 5 = 0 a₁₁ = 5 , a₃₃ = 5

tan 20 a, tan 20 20 0 TI -000 0 Sinto 5 Sing 630 C Sin 0 C 61 7) O 1) 6

I St transformation $D = P^T A P$ $= \left(\frac{1}{10} \circ \frac{1}{10}\right) \left[\frac{1}{10} \circ \frac{1}{10}\right] \left[$ $D = \begin{bmatrix} 6 & 0 & 0 \\ 0 & -2 & 0 \\ 0 & 0 & 4 \end{bmatrix}$ The eigen values are 6, -2, 4 corresponding eigen vectors are 120 - 12 120 - 12 120 - 12 Find all the eigen values and eigen vectors of the Matrix [1 V2 2 V2 3 V2] using Jacobi Method. 2 V2 1]

5 12 Here the largest non diagonal element is $a_{13} = a_{31} = 2$. $a_{11} = 1, a_{33} = 1$ $S_{1} = \begin{bmatrix} a_{10} & 0 & 0 & -sin0 \\ 0 & 1 & 0 \\ sin0 & 0 & an0 \end{bmatrix}$ $\tan 20 = 2a_{13}$ $a_{11} - a_{33}$ $\tan 20 = 8$ 20 = TT/2 0=11/4 S,= (1/2) / 1/2]

$$B_{1} = S_{1}^{-1}AS_{1} \circ = \begin{cases} \frac{1}{12} \circ \frac{1}{12} \circ \frac{1}{12} \\ \frac{1}{22} \\ \frac{1}{22} \circ \frac{1}{12} \\ \frac{1}{22} \\$$

Sa (12 12 0) 12 12 0 12 12 0 $B_{2} = S_{1}^{-1}B_{1}S_{2}$ $= \begin{pmatrix} \frac{1}{12} & \frac{1}{12} & 0 \\ \frac{1}{12} & 0$ $= \frac{1}{2} \begin{pmatrix} 1 & 0 \\ -1 & 0 \\ 0 & 72 \end{pmatrix} \begin{pmatrix} 9 & 2 & 0 \\ 2 & 3 & 0 \\ 0 & 0 & 72 \end{pmatrix} \begin{pmatrix} 1 & -1 & 0 \\ 0 & 0 & 72 \end{pmatrix}$ $= \begin{pmatrix} 5 & 0 & 0 \\ 0 & 0 & -1 \end{pmatrix}$ $= \begin{pmatrix} 5 & 0 & 0 \\ 0 & 0 & -1 \end{pmatrix}$ $\therefore A \text{ is preduced to the diagonal}$ Matrix B₂: Hence the eigen values g A is 5, 1, -)

S= S, S_2 = (t2 0 t2)(t2 t2 0) (t2 0 t2 0)(t2 t2 0) (t2 0 t2 0)(t2 0) -12-12-12 -12-12-12 -12-12-12 eigen vectors are (ta 1/2 $\begin{pmatrix} -1\\ V_{2} \end{pmatrix}$ \neq $\begin{pmatrix} -1\\ 0\\ 1 \end{pmatrix}$

Questions	opt1	opt2	opt3	opt4	
In Regula-Falsi method, to reduce the number of iterations we start with interval	Small	large	equal	no	
The rate of convergence in Newton-Raphson method is of order		1	2	3	4
The condition for convergence for Newton-Raphson method is	f(x) < f'(x) ^2	f(x) > f'(x) ^2	f(x)f"(x) < f'(x) ^2	f(x) <1	
Newton's method is useful when the graph of the function crosses the x-axis is nearly	vertical	horizontal	close to zero	zero	
If the initial approximation to the root is not given we can find any two values of x say a and b such that f (a) and f(b) are	2				
ofsigns.	opposite	same	positive	negative	
f(a) f(b) then 'a' can be taken as the first approximation to the root.	<	>	=	2	
The Newton - Raphson method is also known as method of	secant	tangent	iteration	interpolation	
The Newton- Raphson method will fail if in the neighborhood of the root	f'(x)=0	f (x) ≥0	f(x) <0	f'(x) ≥1	
If f(x)=0 method should be used.	Newton - Raphson	Regula-Falsi	iteration	interpolation	
The rate of convergence of Newton - Raphson method is	quadratic	cubic		4	5
If f (a) and f (b) are of opposite signs the actual root lies between	(a, b)	(0, a)	(0, b)	(0, 0)	
The convergence of root in Regula-Falsi method is slower than	Gauss - Elimination	Gauss - Jordan	Newton - Raphson	Power method	
Regula-Falsi method is known as method of	secant	tangent	chords	elimination	
method converges faster than Regula-Falsi method.	Newton - Raphson	Power method	elimination	interpolation	
f(x) is continuous in the interval (a, b) and if f (a) and f (b) are of opposite signs the equation f(x) = 0 has at least one	-				
lying between a and b.	equation	function	root	polynomial	
$x^2 + 3x - 3 = 0$ is a polynomial of order		2	3	1	0
x is a root of f(x)=0 with multiplicity p, then method is used.	Generalized Newton - Raphson	Newton - Raphson	Regula-Falsi	Power	
Errors which are already present in the statement of the problem are called errors.	Inherent	Rounding	Truncation	Absolute	
Rounding errors arise during	Solving	Computation	Truncation	Absolute	
The other name for truncation error is error.	Absolute	Rounding	Inherent	Algorithm	
Rounding errors arise from the process of the numbers.	Truncating	Rounding off	Approximating	Solving	
Absolute error is denoted by	E_a	E_r	E_p	E_x	
Truncation errors are caused by using results.	Exact	True	Approximate	Real	
Truncation errors are caused on replacing an infinite process by one.	Approximate	True	Finite	Exact	
Graffe's root squaring method is used for solving equation.	Polynomial	Algebraic	transcendental	wave	
Bairstow's method is used for finding roots of a polynomial equation.	Complex	real	second order	first order	
The actual root of the equation lies between a and b when f (a) and f (b) are of signs.	Opposite	same	negative	positive	
If a word length is 4 digits, then the truncation of 15.758 is		15.75	15.76	15.758	16
If a word length is 4 digits, then rounding off of 15.758 is		15.75	15.76	15.758	16

opt7 Small 2 $|f(x)f''(x)| < |f'(x)|^2$ vertical opposite < < tangent f'(x)=0 Regula-Falsi quadratic (a, b) Newton – Raphson chords Newton – Raphson root Generalized Newton – Raphson Inherent Computation Algorithm Rounding off E_a Approximate Finite Polynomial Complex Opposite 2

15.75 15.76

$$= \frac{(\chi - 1)(\chi - 3)}{3}(5) + \frac{\chi(\chi - 3)}{-2}(6) + \frac{\chi(\chi - 1)}{6}(5)$$

$$= \frac{5}{3}[\chi^{2} + 4\chi + 3] - 3[\chi^{2} - 3\chi] + \frac{50}{6}[\chi^{2} - \chi]$$

$$= \chi^{2}[\frac{5}{3} - 3 + \frac{50}{6}] + \chi[-\frac{30}{3} + 9 - \frac{50}{6}]$$

$$= \chi^{2}[\frac{5}{3} - 3 + \frac{50}{6}] + \chi[-\frac{30}{3} + 9 - \frac{50}{6}]$$

$$= \chi^{2}[\frac{5}{3} - 3 + \frac{50}{6}] + \chi[-\frac{30}{3} + 9 - \frac{50}{6}]$$

$$= \chi^{2}[\frac{5}{3} - 3 + \frac{50}{6}] + \chi[-\frac{5}{3}]$$

$$= -\chi^{2} + (-6)\chi + 5$$

$$\frac{\chi}{9} = \rho(\chi) = -\chi^{2} - 6\chi + 5$$

$$\frac{\chi}{9} = \rho(\chi) = -\chi^{2} - 6\chi + 5$$

$$\frac{\chi}{9} = 0 \quad \chi_{1} = 1 \quad \chi_{2} = 3 \quad \chi_{3} = 4, \quad \chi_{4} = 5$$

$$\frac{\chi_{0}}{9} = 0 \quad \chi_{1} = 1 \quad \chi_{2} = 3 \quad \chi_{3} = 4, \quad \chi_{4} = 5$$

$$\frac{\chi_{0}}{9} = 0 \quad \chi_{1} = 1 \quad \chi_{2} = 3 \quad \chi_{3} = 4, \quad \chi_{4} = 5$$

$$\frac{\chi_{0}}{9} = 0 \quad \chi_{1} = 1 \quad \chi_{2} = 3, \quad \chi_{3} = 4, \quad \chi_{4} = 5$$

$$\frac{\chi_{0}}{9} = 0 \quad \chi_{1} = 1 \quad \chi_{2} = 3, \quad \chi_{3} = 4, \quad \chi_{4} = 5$$

$$\frac{\chi_{0}}{9} = 0 \quad \chi_{1} = 1 \quad \chi_{2} = 3, \quad \chi_{3} = 4, \quad \chi_{4} = 5$$

$$\frac{\chi_{0}}{9} = 0 \quad \chi_{1} = 1 \quad \chi_{2} = 3, \quad \chi_{3} = 4, \quad \chi_{4} = 5$$

$$\frac{\chi_{0}}{9} = 0 \quad \chi_{1} = 1 \quad \chi_{2} = 3, \quad \chi_{3} = 4, \quad \chi_{4} = 5$$

$$\frac{\chi_{0}}{9} = 0 \quad \chi_{1} = 1 \quad \chi_{2} = 3, \quad \chi_{3} = 4, \quad \chi_{4} = 5$$

$$\frac{\chi_{0}}{9} = 0 \quad \chi_{1} = 1 \quad \chi_{2} = 3, \quad \chi_{3} = 4, \quad \chi_{4} = 5$$

$$\frac{\chi_{0}}{9} = 0 \quad \chi_{1} = 1 \quad \chi_{2} = 3, \quad (\chi_{2} - \chi_{3}) (\chi_{2} - \chi_{4}), \quad y_{0}$$

$$+ (\chi_{2} - \chi_{0}) (\chi_{2} - \chi_{3}) (\chi_{2} - \chi_{3}) (\chi_{2} - \chi_{4}), \quad y_{0}$$

$$+ (\chi_{2} - \chi_{0}) (\chi_{2} - \chi_{3}) (\chi_{2} - \chi_{3}) (\chi_{2} - \chi_{4}), \quad y_{2}$$

$$+ (\chi_{2} - \chi_{0}) (\chi_{2} - \chi_{1}) (\chi_{2} - \chi_{3}) (\chi_{2} - \chi_{4}), \quad y_{2}$$

$$+ (\chi_{2} - \chi_{0}) (\chi_{2} - \chi_{1}) (\chi_{2} - \chi_{3}) (\chi_{2} - \chi_{4})$$

$$\begin{aligned} p_{ut} = x = 2 \\ y(z) &= \frac{(2-1)(2-3)(2-4)(2-5^{-1})}{(2-1)(2-3)(2-4)(2-5^{-1})} \\ + \frac{(2-0)(2-3)(2-4)(2-5^{-1})}{(1-0)(1-3)(1-4)(1-5^{-1})} \\ (1) \\ + \frac{(2-0)(2-1)(2-4)(2-5)}{(3-0)(2-4)(2-5)} \\ (81) \\ (3-0)(3-1)(3-4)(3-5) \\ + \frac{(2-0)(2-1)(2-3)(2-5)}{(4-0)(4-1)(4-3)(4-5)} \\ (550) \\ + \frac{(2-0)(2-1)(2-3)(2-4)}{(5-0)(5-3)(5-4)} \\ (625) \\ &= \frac{(2)(-1)(-2)(-3)}{(1)(-2)(-3)(-4)} \\ + \frac{(2)(1)(-1)(-3)}{(1)(-2)(-3)(-4)} \\ + \frac{(2)(1)(-1)(-3)}{(2-5)(-4)} \\ + \frac{(2)(1)(-1)(-3)}{(2-5)(-4)(-4)} \\ + \frac{(2)(1)(-1)(-3)}{(2-5)(-4)(-4)(-4)} \\ + \frac{(2)(1)(-1)(-3)}{(2-5)(-4)(-4)(-4)} \\ + \frac{(2)(1)(-1)(-3)}{(2-5)(-4)(-4)(-4)} \\ + \frac{(2)(1)(-1)(-3)}{(2-5)(-4)(-4)(-4)(-4)} \\ + \frac{(2)(1)(-1)(-2)}{(2-5)(-4)(-4)(-4)(-4)} \\ + \frac{(2)(1)(-1)(-3)}{(2-5)(-4)(-4)(-4)(-4)} \\ + \frac{(2)(1)(-3)(-3)}{(2-5)(-4)(-4)(-4)(-4)} \\ + \frac{(2)(1)(-3)(-3)}{(2-5)(-4)(-4)(-4)(-4)} \\ + \frac{(2)(1)(-3)}{(2-5)(-4)(-4)(-4)(-4)} \\ + \frac{(2)(1)(-3)}{(2-5)(-4)(-4)(-4)} \\ + \frac{(2)(1)(-3)}{(2-5)(-4)(-4)} \\ + \frac{(2)(1)(-3)}{(2-5)(-4)(-4)} \\ + \frac{(2)(1)(-3)}{(2-5)(-4)(-4)} \\ + \frac{(2)(1)(-3)}{(2-5)(-4)} \\ +$$

$$\begin{array}{c} y = f(x) = \frac{(x - x_{1})(x - x_{2})(x - x_{3})}{(x_{0} - x_{1})(x_{0} - x_{2})(x_{0} - x_{3})} \cdot y_{0} \\ + \frac{(x - x_{0})(x - x_{1})(x_{0} - x_{3})}{(x_{1} - x_{0})(x - x_{1})(x_{0} - x_{3})} \cdot y_{1} \\ + \frac{(x - x_{0})(x - x_{1})(x_{0} - x_{3})}{(x_{2} - x_{0})(x_{2} - x_{1})(x_{3} - x_{3})} \cdot y_{2} \\ + \frac{(x - x_{0})(x - x_{1})(x_{0} - x_{3})}{(x_{3} - x_{0})(x_{3} - x_{1})(x_{3} - x_{3})} \cdot y_{3} \\ p_{ut} = f(65b) = \frac{(65b - 658)(65b - 659)(65b - 66b)}{(65y - 658)(65y - 659)(65b - 66b)} \cdot (2.8182) \\ + \frac{(656 - 65y)(65b - 659)(65b - 659)(65b - 66b)}{(659 - 65y)(65b - 66b)}(2.8182) \\ + \frac{(656 - 654)(65b - 659)(65b - 659)(65b - 66b)}{(65b - 659)(65b - 659)(65b - 66b)} \cdot (2.8182) \\ + \frac{(656 - 654)(65b - 659)(65b - 659)(65b - 659)}{(65b - 659)(65b - 659)(65b - 659)} \cdot (2.8182) \\ - \frac{(-2)(-3)(-5)}{(-x)(-7)}(2 - 8156) + \frac{2(-3)(-5)}{4(-1)(-3)}(2 - 8182) \\ - \frac{(-2)(-3)(-5)}{(-x)(-2)}(2 - 8189) + \frac{(2)(-2)(-3)}{(-3)(2)}(2 - 8202) \\ (5)(1)(-2)(-2)(-5) - 5(-538)(-538) + 0.8058 \\ = 2 \cdot 8168 \\ \end{array}$$

$$\begin{aligned} \frac{\Im f_{0}}{\Im_{0}} & \begin{array}{l} \chi_{0} = 3 & \chi_{1} = 7 & \chi_{2} = 9 & \chi_{3} = 10 \\ \chi_{0} = 168 & \chi_{1} = 120 & \chi_{2} = 72 & \chi_{3} = 63 \\ \Im & y = f(x) = \frac{(\chi - \chi_{1})(\chi - \chi_{2})(\chi - \chi_{2})}{(\chi_{0} - \chi_{1})(\chi_{0} - \chi_{2})(\chi_{0} - \chi_{3})} & \chi_{0} \\ & + \frac{(\chi - \chi_{0})(\chi - \chi_{2})(\chi - \chi_{3})}{(\chi_{1} - \chi_{0})(\chi - \chi_{1})(\chi - \chi_{3})} & y_{1} \\ & + \frac{(\chi - \chi_{0})(\chi - \chi_{1})(\chi - \chi_{3})}{(\chi_{3} - \chi_{0})(\chi_{3} - \chi_{1})(\chi_{3} - \chi_{3})} & y_{2} \\ & + \frac{(\chi - \chi_{0})(\chi - \chi_{1})(\chi - \chi_{3})}{(\chi_{3} - \chi_{0})(\chi_{3} - \chi_{1})(\chi_{3} - \chi_{3})} & y_{3} \\ & R_{t} & \chi = 6 \\ & y = f(6) & = \frac{(6 - 7)(6 - 9)(6 - 10)}{(3 - 7)(3 - 9)(3 - 10)}(16.8) \\ & + \frac{(6 - 3)(6 - 9)(6 - 10)}{(\gamma - 3)(\gamma - 9)(\gamma - 10)}(120) \\ & + \frac{(6 - 3)(6 - 9)(6 - 10)}{(\gamma - 3)(\gamma - 9)(\gamma - 10)}(120) \\ & + \frac{(6 - 3)(6 - 7)(6 - 10)}{(\gamma - 3)(\gamma - 9 - 1)(10 - 9)}(63) \\ & = \frac{(-1)(-3)(-1)}{(-4)(-6)(-7)}(16.8) + \frac{(3)(-3)(-4)}{(4(-3)(-3))}(120) \\ & + \frac{(3)(-1)(-4)}{(6)(2)(-1)}(\gamma - 2) + \frac{(3)(-1)(-3)}{(7)(3)(1)}(63) \\ & = 12 + 180 - (72 + 27) \\ & = 147 \end{aligned}$$

6) Find the Mining both in the following
has been using Lagranges interpolation

$$\frac{\pi}{y} = 0 \quad x_1 = 1 \quad x_2 = 3 \quad x_3 = 1, \\
y_0 = 1 \quad y_1 = 3 \quad y_2 = 9 \quad y_3 = 8, \\
y_0 = 1 \quad y_1 = 3 \quad y_2 = 9 \quad y_3 = 8, \\
y_0 = 1 \quad y_1 = 3 \quad y_2 = 9 \quad y_3 = 8, \\
y_0 = 1 \quad y_1 = 3 \quad y_2 = 9 \quad y_3 = 8, \\
y_0 = 1 \quad y_1 = 3 \quad y_2 = 9 \quad y_3 = 8, \\
y_0 = 1 \quad y_1 = 3 \quad y_2 = 9 \quad y_3 = 8, \\
y_0 = 1 \quad y_1 = 3 \quad y_2 = 9 \quad y_3 = 8, \\
y_0 = 1 \quad y_1 = 3 \quad y_2 = 9 \quad y_3 = 8, \\
y_0 = 1 \quad y_1 = 3 \quad y_2 = 9 \quad y_3 = 8, \\
y_0 = 1 \quad y_1 = 3 \quad y_2 = 9 \quad y_3 = 8, \\
y_1 = 1 \quad y_1 = 3 \quad y_2 = 9 \quad y_3 = 8, \\
y_1 = y_3 \quad 0 \quad (x_1 - x_1) \quad (x_1 - x_3) \quad (x_1 - x_3) \quad y_3 \\
+ (x_1 - x_0) \quad (x_1 - x_1) \quad (x_1 - x_3) \quad y_1 \\
+ (x_1 - x_0) \quad (x_1 - x_1) \quad (x_1 - x_3) \quad y_2 \\
+ (x_1 - x_0) \quad (x_1 - x_1) \quad (x_1 - x_3) \quad y_3 \\
y_1 = y_3 \quad (x_3 - x_1) \quad (x_3 - x_3) \quad y_3 \\
y_1 = y_3 \quad (x_3 - x_1) \quad (x_3 - x_3) \quad y_3 \\
y_1 = y_3 \quad (x_3 - x_1) \quad (x_3 - x_3) \quad (x_3 - x_3) \quad y_3 \\
y_1 = y_3 \quad (x_3 - x_1) \quad (x_3 - x_3) \quad (x_4 - x_4) \quad (x_4 - x_3) \quad (x_4 - x_4) \quad (x_4 - x_4$$

+
$$(0+2\circ)(0+13)(0-18).(38)$$

+ $(0+3\circ)(0+13)(8-19)$
+ $(0+3\circ)(0+13)(8-3)$
(18+30) (18+13) 18-3)
= $31\cdot 23.$
(3) Find the value of 0 guien $F(0) = 0.3887$
where $f(0) = \int \frac{do}{do}$ using the table
 $0 \sqrt{1-\frac{1}{5}\sin^{2}\theta}$ using the table
 $\sqrt{1-\frac{1}{5}\sin^{2}\theta}$
 $\boxed{0}$ $\frac{21^{\circ}}{23^{\circ}}$ $\frac{25^{\circ}}{25^{\circ}}$
 $\boxed{1}$ $\frac{1}{160}$ 0.3706 0.4068 0.4433 .
 $3eln$ Let $0 = \pi$
 $f(0) = F(\pi) = y$
 $\boxed{\frac{\chi}{2}}$ $\frac{21^{\circ}}{23^{\circ}}$ $\frac{25^{\circ}}{25^{\circ}}$
 $\boxed{\frac{\chi}{9}}$ 0.3706 0.4068 0.4433 .
 $\chi = f(y) = (\frac{y-y_{1}}{y}, (\frac{y-y_{2}}{y}), \pi_{0} + (\frac{y-y_{0}}{y}, (\frac{y-y_{2}}{y}), \pi_{1})$
 $+ (\frac{y-y_{0}}{y}, (\frac{y-y_{1}}{y}), \pi_{2} + (\frac{y-y_{0}}{y}, (\frac{y-y_{1}}{y}), \pi_{2})$
 $\Re t$ $y = 0.3887$ $(\frac{y-y_{1}}{y}, (\frac{y-y_{1}}{y})$ $(0.3887-0.4433)$ (21)
 $\frac{1}{0.3766}$ -0.37061 $(0.3887-0.4433)$ (25)
 $\frac{1}{0.4688}$ $-0.37062(0.03887-0.4433)$ (25)

$$\frac{\text{Newton's divided digerence formula: (unequal)}}{y = \beta(x) = y_0 + (x-x_0) \ \Delta\beta(x_0) + (x-x_0)(x-x_1) \ \Delta\beta(x_0) + (x-x_0)(x-x_1) \ \Delta\beta(x_0) + \cdots$$

(0) Using Newton's divided digerence formula find $\beta(x)$
 $p(x)$ and $\beta(b)$ from the following data:
 $\frac{x}{|f(x)|: 1|} \frac{1}{|5|} \frac{2}{|5|} \frac{x_1}{|5|} \frac{1}{|5|} \frac{x_2}{|5|} \frac{x_3}{|5|}$

Solution $\frac{x}{|f(x)|: 1|} \frac{1}{|5|} \frac{5}{|5|} \frac{x_1}{|5|} \frac{1}{|5|} \frac{x_2}{|5|} \frac{x_3}{|5|} \frac{x_3}{|5|} \frac{x_3}{|5|} \frac{x_3}{|5|} \frac{x_3}{|5|} \frac{x_4}{|5|} \frac{x_5}{|5|} \frac{x_5}$

$$= x^{3} \begin{bmatrix} \frac{1}{14} \end{bmatrix} + x^{2} \begin{bmatrix} -\frac{1}{6} \end{bmatrix} -\frac{3}{14} - \frac{7}{14} \end{bmatrix} + x \begin{bmatrix} 4 + \frac{12}{6} + \frac{2}{16} \end{bmatrix} + \frac{21}{16} \end{bmatrix} + \begin{bmatrix} -\frac{1}{6} - \frac{8}{6} - \frac{14}{14} \end{bmatrix} + x \begin{bmatrix} 4 + \frac{12}{6} + \frac{2}{16} + \frac{21}{16} \end{bmatrix} + \begin{bmatrix} -\frac{1}{6} - \frac{8}{6} - \frac{14}{14} \end{bmatrix} + x \begin{bmatrix} 6 + \frac{12}{6} + \frac{2}{16} + \frac{21}{16} \end{bmatrix} + \begin{bmatrix} -\frac{1}{6} - \frac{8}{6} - \frac{14}{14} \end{bmatrix} + \begin{bmatrix} \frac{1}{6} \end{bmatrix} + \frac{3}{6} \end{bmatrix} = \frac{1}{14} \begin{bmatrix} 6 \end{bmatrix}^{3} - \frac{39}{24} \begin{bmatrix} 6 \end{bmatrix}^{2} + \begin{bmatrix} 07(6) - 1\frac{169}{24} \end{bmatrix} + \frac{16}{16} \end{bmatrix} = \frac{1}{16} \begin{bmatrix} 6 \end{bmatrix}^{3} - \frac{39}{24} \begin{bmatrix} 6 \end{bmatrix}^{2} + \begin{bmatrix} 07(6) - 1\frac{169}{24} \end{bmatrix} + \frac{16}{36} = \frac{16}{16} \end{bmatrix} + \frac{16}{14} + \frac{16}{36} = \frac{16}{16} + \frac{16}{14} + \frac{16}{36} = \frac{16}{16} + \frac{16}{24} + \frac{16}{14} + \frac{16}{36} = \frac{16}{36} + \frac{16}{16} + \frac{16}{24} + \frac{16}{36} + \frac{16}{36} + \frac{16}{16} + \frac{16$$

$$\begin{aligned} y = f(x_{0}) = f(y_{0}) + (x - x_{0}) \Delta f(x_{0}) + (x - x_{0})(x - x_{1}) \Delta^{2} f(x) \\ &+ (x - x_{0})(x - x_{1})(x - x_{2}) \Delta^{3} f(x) \\ &+ (x - x_{0})(x - x_{1})(x - x_{2}) \Delta^{4} f(x) \end{aligned} \\ = 1245 + (x + 4)(-404) + (x + 4)(x + 1)(94) \\ &+ (x + 4)(x + 1)(x - 0)(-4) + (x + 4)(x + 1)(x - 0)(x - 2)(3) \\ &= 1245 - 404x - 1616 + (x^{2} + 5x + 4) 94 \\ &+ (x^{2} + 5x + 4) \times (-44x_{0}) + (x^{2} + 5x + 4) 5x^{2} - 6x \times (-4x^{2} + 5x + 4) - 94 \\ &+ (x^{2} + 5x + 4) \times (-44x_{0}) + (x^{2} + 5x + 4) 5x^{2} - 6x \times (-4x^{2} - 50x + 3x^{2} + 15x^{3} + 12x^{2} - 6x^{2} - 30x^{2} - 30x^{2} - 24x \\ &= 1245 - 404x - 1616 + 94x^{2} + 470x + 876 \\ &= 1245 - 404x - 1616 + 94x^{2} + 470x + 876 \\ &= 1245 - 404x - 1616 + 94x^{2} + 470x + 876 \\ &= 1245 - 404x - 1616 + 94x^{2} + 470x + 876 \\ &= 1245 - 404x - 1616 + 94x^{2} - 16x^{2} + 3x^{2} + 12x^{3} + 12x^{2} - 6x^{2} - 30x^{2} - 24x \\ &= 1245 - 404x - 1616 + 94x^{2} + 64x^{2} + 94x^{2} + 20x^{2} + 230 + 20x^{2} + 23x^{2} + 12x^{2} + 12x^{2}$$

$$\frac{gg_{12}}{x} \frac{y = f(x)}{x} \frac{\Delta f(x)}{1 - o} \frac{\Delta^2 f(x)}{y} \frac{\Delta^2 f(x)}{\Delta^2 f(x)} \frac{\Delta^2 f(x)}{x} \frac{\Delta^2 f(x)}{y} \frac{\Delta^2 f(x)}$$

Solve
$$\bigcirc \varphi \oslash$$

 $M_{1} = -12$ $M_{2} = 48$
The cubic gpline polynomial is
 $S(x) = \frac{1}{b} \int (x_{1}, -x)^{3}M_{1-1} - (x_{1-1}, -x)^{3}M_{1}$
 $g(x) = \frac{1}{b} \int (x_{1}, -x) \int y_{1-1} - \frac{1}{b} M_{1-1}$
 $+ (x_{1}, -x) \int y_{1-1} - \frac{1}{b} M_{1-1}$
 $- (x_{1-1}, -x) \int y_{1} - \frac{1}{b} M_{1}$
Case(i) $-1 < x < 0$
Put $i = 1$
 $S(x) = \frac{1}{b} \int (x_{1}, -x) M_{0} - (x_{0} - x)^{3}M_{1}$
 $+ (x_{1}, -x) \int y_{0} - \frac{1}{b} M_{0} - (x_{0} - x) \int y_{1-\frac{1}{b}} M_{1}$
 $= \frac{1}{b} \int -(-1 - x) \int (-12) \int +(0 - x) (-1) -(-1 - x) \int 1 + \frac{12}{b} \int 1$
 $= \frac{1}{b} \int -12 (1 + x)^{3} \int +x + (1 + x) (3)$
 $= -2 \int 1 + x^{3} + 3x + 3x^{2} \int +x + 3 + 3x$
 $= -2 - 2x^{3} - 6x^{2} - 3x + 1 - 1 < x < 0$
Case (ii) $0 < x < 4$
Put $i = 2$

$$\begin{split} & S(x) = \frac{1}{6} \int (x_2 - x_1)^3 M_1 - (x_1 - x)^3 M_2 \\ & + (x_2 - x) \int y_1 - \frac{1}{6} M_1 \int \\ & - (x_1 - x) \int y_2 - \frac{1}{6} M_2 \int \\ & = \frac{1}{6} \int (1 - x)^3 (-12) - (0 - x)^3 (48) \int \\ & + (1 - x) \int 1 - \frac{1}{6} (-12) \int - (0 - x) \\ & + (1 - x) \int 1 - \frac{1}{6} (-12) \int - (0 - x) \\ & = \frac{1}{6} \int -12 (1 - x)^3 + 48 x^3 \int + 3(1 - x) - 5x \\ & = \frac{1}{6} \int -12 (1 - x^3 - 3x + 3x^2) + 48 x^3 \\ & + 3 - 3x - 5x \\ & = \frac{1}{6} \int -12 + 12x^3 + 36x - 36x^2 + 48x^3 \\ & + 3 - 3x - 5x \\ & = \frac{1}{6} \int -12 + 12x^3 + 36x - 36x^2 + 48x^3 \\ & = \frac{1}{6} \int -12 + 12x^3 + 36x - 36x^2 + 48x^3 \\ & = \frac{1}{6} \int -12 + 12x^3 + 36x - 36x^2 + 48x^3 \\ & = \frac{1}{6} \int -12 + 12x^3 + 36x - 36x^2 + 48x^3 \\ & = \frac{1}{6} \int -12 + 12x^3 + 36x - 36x^2 + 48x^3 \\ & = \frac{2 + 3}{1 - 3x - 5x} \\ & = \frac{-2 + 3}{1 - 5x} \\ \hline & Gwe(iii) \quad 1 < x < 2 \\ Pat \quad i = S \\ S(x) &= \frac{1}{6} \int (x_3 - x)^3 M_2 - (x_2 - x)^3 M_3 \int \\ & + (x_3 - x) \int y_2 - \frac{1}{6} M_2 \int -(x_3 - x)^3 M_3 \\ & = \frac{1}{6} \int (2 - x)^3 H_8 \int +(2 - x) \int S -\frac{1}{6} x + 8 \\ \end{bmatrix}$$

$$= 8 (2-x)^{3} + (2-x) (-5) - 35^{-}(1-x)$$

$$= 8 [8-x^{2} - 12x + 6x^{2}] - 10 + 5x - 35 + 35,$$

$$= 64 - 8x^{3} - 96x + 48x^{2} - 10 + 5x - 35 + 35x$$

$$\boxed{S(x) = -8x^{3} + 48x^{2} - 56x + 19, 1 - x < 2}$$

$$\boxed{Re \ cubie \ Spline \ Polynomial \ is}$$

$$\int -2x^{3} - 6x^{2} - 2x + 1 + 0 < x < 1$$

$$\int -8x^{3} + 48x^{2} - 56x + 19, 1 < x < 2$$

$$\boxed{S(x) = \int 10x^{3} - 6x^{2} - 2x + 1 + 0 < x < 1}$$

$$\boxed{-8x^{3} + 48x^{2} - 56x + 19, 1 < x < 2}$$

$$\boxed{S(x) = \int 10x^{3} - 6x^{2} - 2x + 1 + 0 < x < 1}$$

$$\boxed{\frac{x}{1} + \frac{1}{x_{0}} - \frac{2x}{1} + \frac{3x_{2}}{1}}$$

$$\boxed{Gmpute \ y(1.5) \ and \ y'(1) \ using \ abie \ bline.}$$

$$\boxed{S60}$$

$$\boxed{Take \ M_{0} = M_{2} = 0., \ F_{0} = 1$$

$$Wik T \ M_{i-1} + 4M_{i} + M_{i+1} = 6[y_{0} - 2y_{i} + y_{i} + 1]$$

$$\boxed{Put \ i = 1}$$

$$M_{0} + 4M_{1} + M_{2} = 6[y_{0} - 2y_{i} + y_{2} - 3x_{0} + 18]$$

$$\frac{4M_{1} = 72}{1M_{1} = 18}$$

The cubic Spline Polynomial is

$$S(x) = \frac{1}{b} \left[(x_{1} - x)^{3} M_{1-1} - (x_{1-1} - x)^{3} M_{1} \right] + (x_{1} - x) \left[y_{1-1} - \frac{1}{b} M_{1-1} \right] - (x_{1-1} - x) \left[y_{1-1} - \frac{1}{b} M_{1-1} \right] - (x_{1-1} - x) \left[y_{1-1} - \frac{1}{b} M_{1-1} \right] \right] + (x_{1} - x) \left[y_{1} - \frac{1}{b} M_{1} \right] \\ Case (i) \quad 1 < x < 2 \\ Put \quad i = 1 \\ S(x) = \frac{1}{b} \left[(x_{1} - x)^{3} M_{0} - (x_{0} - x)^{3} M_{1} \right] + (x_{1} - x) \left[y_{0} - \frac{1}{b} M_{0} \right] \\ - (x_{0} - x) \left[y_{1} - \frac{1}{b} M_{1} \right] \\ = \frac{1}{b} \left[(a - x)^{3} (a) - (1 - x)^{3} (a) e \right] \\ + (a - x) \left[x - 8 - \frac{1}{b} (a) \right] \\ - (1 - x)^{2} (1 - x)^{3} (a) - (1 - x)^{3} (a) e \right] \\ = \frac{1}{b} \left[- (1 - x)^{3} (1e) + (2 - x) (-8) \right] \\ = -18 (1 - x)^{3} - 8 (2 - x) + 4 (1 - x) \\ - 18 (1 - x)^{3} - 16 + 8x + 4 - 4x \right] \\ \overline{S(x)} = -18 (1 - x)^{3} + 4x - 12 , 1 < x < 2 \\ Put \quad x = 1 \cdot 5 \\ y(1 \cdot 5) = S(1 \cdot 5) = -18 (1 - 1 \cdot 5)^{3} + 4 (1 \cdot 5) - 12 \\ = -5 \cdot 625 - 3$$

$$y'(1) = 9(0) + 4 = 4$$

$$y'(1) = 4$$

$$y'(1) = 4$$

$$y'(1) = 4$$

$$y'(1-5) = -5-625$$

$$y'(1) = 4$$

$$y'(1-5) = -5-625$$

$$y'(1) = 4$$

$$y'(1-5) = -5-625$$

$$y'(1$$

$$\begin{aligned} \begin{bmatrix} (a-b)^{2} \\ = a^{2}-3 \end{bmatrix} &= \frac{1}{6} \left[\left[-(1-x)^{3} \left(\frac{3}{27} \right) \right] + (2-x) \left[2 \right] \right] \\ &= \frac{1}{6} \left[\left[-\frac{3}{27} \left((1-x)^{3} + (2-x) \right) + \frac{5}{7} \left((1-x) \right) \right] \right] \\ &= \frac{1}{6} \left[\left[-\frac{3}{27} \left(1 \right]^{3} - x^{3} - 3x + 3x^{2} \right] + 2 - x \\ &+ \frac{5}{7} - \frac{5}{7} x \right] \\ &= -\frac{5}{7} \left[1 + \frac{5}{7} x^{3} + \frac{15}{7} x + \frac{15}{7} x^{2} + 2 - x \\ &+ \frac{5}{7} - \frac{5}{7} x \right] \\ &= -\frac{5}{7} \left[x^{3} + \frac{15}{7} x^{2} + x \left(\frac{15}{7} - \frac{3}{7} - \frac{5}{7} \right) \right] \\ S(x) &= \frac{5}{7} x^{3} + \frac{15}{7} x^{2} + \frac{3}{7} x + 2 \\ &= \frac{5}{7} x^{3} + \frac{15}{7} x^{2} + \frac{3}{7} x + 2 \\ S(x) &= \frac{1}{6} \left[\left(\frac{3}{2} - x \right)^{3} \frac{M_{1}}{7} - \left(\frac{x}{7} - x \right) \right] \\ &= \frac{1}{6} \left[\left(\frac{3}{2} - x \right)^{3} \frac{M_{1}}{7} - \left(\frac{x}{7} - x \right) \left[\frac{y}{2} - \frac{1}{6} \frac{M_{2}}{7} \right] \\ &= \frac{1}{6} \left[\left(\frac{3}{2} - x \right)^{3} \frac{39}{7} - \left(2 - x \right) \left(-\frac{36}{7} \right) \right] \\ &= \frac{1}{6} \left[\left(\frac{3}{2} - x \right) \frac{39}{7} - \left(2 - x \right) \left(-\frac{36}{7} \right) \right] \\ &= \left(2 - x \right) \left[1 - \frac{1}{6} \left(-\frac{36}{7} \right) \right] \end{aligned}$$

$$= \frac{1}{6} \left[\frac{29}{7} (3-x)^{3} + \frac{36}{7} (2-x) \right] + (3-x) \left(-\frac{5}{7} \right) - (2-x) \int 1 + \frac{5}{7} \right]$$

$$= \frac{5}{7} \left[27 - 27x + 9x^{2} - x^{3} \right] + \frac{6}{7} \int 4 + x^{2} - 4x \right] - \frac{15}{7} + \frac{5x}{7} - \frac{36}{7} + \frac{13x}{7} \right]$$

$$= x^{3} \int -\frac{5}{7} \int + x^{2} \int 4\frac{5}{7} + \frac{6}{7} + \frac{5}{7} + \frac{5}{7} \right]$$

$$+ x \int -135 - \frac{24}{7} + \frac{5}{7} + \frac{6}{7} + \frac{5}{7} + \frac{18}{7} \right] + \frac{135}{7} + \frac{24}{7} - \frac{57}{7}$$

$$+ x \int -135 - \frac{24}{7} + \frac{5}{7} + \frac{18}{7} + \frac{13}{7} + \frac{135}{7} + \frac{24}{7} - \frac{57}{7}$$

$$= \frac{-26}{7} + \frac{2}{7} + \frac{51}{7} + \frac{2}{7} + \frac{118}{7} + \frac{125}{7} + \frac{24}{7} - \frac{57}{7} + \frac{-26}{7} + \frac{118}{7} + \frac{125}{7} + \frac{24}{7} - \frac{57}{7} + \frac{24}{7} + \frac{118}{7} + \frac{22}{7} + \frac{24}{7} + \frac{5}{7} + \frac{24}{7} + \frac{5}{7} + \frac{5$$

$$= \frac{1}{6} \int -\frac{36}{7} \int \frac{64}{64} - \frac{48}{8} + \frac{12}{12} x^2 - x^3 \int \frac{36}{7} \int \frac{27}{7} - \frac{27}{8} + \frac{9}{8} x^2 - \frac{27}{7} x^3 \int \frac{1}{7} + \frac{1}{7} + \frac{1}{7} (1 + \frac{6}{7}) - (3 - x) \left(-\frac{5}{7}\right)$$

$$= \int \frac{38}{7} \frac{38}{7} + \frac{13}{7} x^3$$

$$= \frac{1}{7} \int -\frac{38}{7} + \frac{288}{7} x - \frac{7}{2} x^2 + \frac{6}{8} x^3 - \frac{810}{7} + \frac{810}{7} x + \frac{270}{7} x^2 + \frac{30}{3} x^3,$$

$$+ 52 - 13x + 15 - 5x \int \frac{1}{7} + \frac{1}{8} \int \frac{36}{7} x^3 \int \frac{30}{6} + \frac{810}{7} + \frac{1}{2} - \frac{72}{7} - \frac{270}{7} \int \frac{1}{7} + x \int \frac{288}{7} + \frac{810}{7} - \frac{1}{3} - \frac{77}{7} - \frac{2770}{7} \int \frac{1}{7} \int \frac{36}{7} x^3 \int \frac{30}{7} + \frac{1}{7} \int \frac{36}{7} x^3 - \frac{342}{7} x^2 + \frac{1080}{7} x - \frac{1127}{7}, \frac{32}{7} - \frac{32}{7} + \frac{1}{6} \int \frac{36}{7} x^3 - \frac{342}{7} x^2 + \frac{1080}{7} x - \frac{1127}{7}, \frac{32}{7} - \frac{2}{7} x^2 + \frac{1}{6} \int \frac{1}{6} \int \frac{1}{7} \int \frac{36}{7} x^3 - \frac{1}{7} \int \frac{3}{7} \frac{3}{7} + \frac{1}{7} \int \frac{3}{7} \frac{3}{7} - \frac{1}{7} \int \frac{3}{7} \frac{3}{7} - \frac{1}{7} \int \frac{3}{7} \frac{3}{7} + \frac{1}{7} \int \frac{3}{7} \frac{3}{7} - \frac{1}{7} \int \frac{3}{7} \frac{3}{7} + \frac{1}{7} \int \frac{3}{7} \int \frac{3}{7} + \frac{1}{7} \int \frac{3}{7} + \frac{1}{7}$$

$$= \frac{1}{6} \left[(2-x)^{3} (0) + (x-1)^{3} (18) \right] + (2-x) \left[-6 - \frac{1}{6} (0) \right] + (x-1) \left[-1 - \frac{1}{5} (18) \right] = \frac{1}{6} \left[(x-1)^{3} (18) \right] + (2-x) (-6-6) + (x-1) (-1-3) \\= 3 (x^{3} - 3x^{2} + 3x - 1) - 12 + 6x - 4x + 4 g(x) = 3x^{3} - 9x^{2} + 11x - 11 Gase (ii) 2 \le x \le 3 Pat i = 2 . g(x) = \frac{1}{6} \left[(x_{2} - x)^{3} M_{1} - (x_{1} - x)^{3} M_{2} \right] + (x_{3} - x) \left[y_{1} - \frac{1}{6} M_{1} \right] - (x_{1} - x) \left[y_{2} - \frac{1}{6} M_{2} \right] \\= \frac{1}{6} \left[(3 - x)^{3} 18 - (2 - x)^{3} (0) \right] + (3 - x) \left[-1 - \frac{1}{6} (18) \right] - (x - 2) \left[16 - \frac{1}{7} (0) \right] = \frac{18}{6} \left[27 - 27x + 9x^{2} - x^{3} \right] - (2 + 4x) + 16x - 32$$

$$g(x) = -3x^{3} + 27x^{2} = 61x + 37$$

$$y = g(x) = \int 3x^{2} - 9x^{2} + 11x - 11, \quad 1 \le x \le 2$$

$$\int -3x^{3} + 27x^{2} - 61x + 37, \quad 2 \le x \le 3$$

To gived $y(1:5)$

$$g(1:5) = g(1:5)^{2} - 9(1:5)^{2} + 11(1:5) - 11$$

$$= -4 - 625^{-1}$$

Neutoris jorward interpolation jornula
(equal intervals).

$$y = p(x) = y_0 + \frac{u}{11} \Delta y_0 + \frac{u(u-1)}{2} \Delta^2 y_0 + \frac{u(u-1)(u-2)}{3!} \Delta^2 y_0 + \frac{u(u-1)(u-2)$$

The Newton's forward interpolation form.
is

$$y = y_0 + \frac{u}{1!} \Delta y_0 + \frac{u(u-1)}{2!} \Delta \frac{v}{y}_0 + \frac{u(u-1)(u-2)}{3!} \int_{y+1}^{y} \int_{y+1}^{y} \int_{y}^{y} \int_{y}^{y}$$

$$\begin{split} & \frac{\overline{x} + \overline{y} + \overline$$

$$\begin{split} y - 4 & = 250 + (\frac{\pi}{20} - 40) + 120 + (\frac{\pi}{20} - 40) (\frac{\pi}{20} - 1) (\frac{\pi}{$$

Newton's Backword Interpolation formula

$$y = 40 + \frac{1}{11} \nabla y_{n} + \frac{1}{2} \nabla (y+1) \nabla^{2} y_{n} + \frac{1}{2} \frac{1}{31} \nabla y_{n}$$
Where $V = \frac{1}{R}$
Where $V = \frac{1}{R}$
(1) Use Newton's backword dyjenence formula to
Construct an interpolating polynomial q degree 3
for the data
f(-0.15) = -0.07181250 f(-0.5) = -0.024750
f(-0.25) = 0.32493750, f(0) = 1.10100.
Hence find $f(-\frac{1}{3})$.
Solo.

$$V = \frac{1}{R} - \frac{1}{R} + \frac{1}{R} = 0.25$$

$$V = \frac{1}{R} - \frac{1}{R} + \frac{1}{R} = \frac{1}{0.25}$$

$$\frac{1}{2} + \frac{1}{2} + \frac{1}{2}$$

The Newton's backward interpolation zormule.
is

$$y = y_{0} \pm \frac{v}{1!} \quad \forall y_{0} \pm \frac{v(v+1)}{2!} \quad \forall^{2}y_{1} \pm \frac{v(v+1)(v+2)}{3!} \quad \forall^{2}y_{1}^{*}$$

= 1.10100 $\pm \left(\frac{\pi}{0.25}\right) (0.7660625)$
 $\pm \left(\frac{\pi}{0.25}\right) \left(\frac{\pi}{0.25} \pm 1.\right) (0.406375)$
 $\pm \left(\frac{\pi}{0.25}\right) \left(\frac{\pi}{0.25} \pm 1.\right) \left(0.406375\right)$
 $\pm \left(\frac{\pi}{0.25}\right) \left(\frac{\pi}{0.25} \pm 1.\right) \left(0.09375\right)$
 31
= 1.10100 $\pm (-1.33333) (0.7660625)$
 $\pm \left(-1.33333\right) (-0.33333) (0.90637)$
 $\pm \left(-1.33333\right) \left(-0.33333\right) (-0.46663)$
 $= 1.10100 - 1.021414 \pm 0.05030442.6$
 $\pm 0.00462935^{-1}$
 $y(-1/3) = 0.165260$.
(2) The amount A g a Substance remaining
in a greating System ayter an interval
g vine t in a contain chemical experiment

$$y = 45 \cdot 1 - 6 \cdot 2 \left(\frac{x_{1} - 11}{2}\right) + \left(\frac{x_{1} - 11}{8}\right) \left(\frac{x_{1} - 8}{8}\right) \frac{x_{0} \cdot y_{1}}{8}$$

$$+ \frac{(x_{1} - 11)(x_{1} - 8)(x_{1} - 5)}{162} - x_{0} \cdot 1$$

$$P_{ut} = x_{2} \cdot 9$$

$$y(9) = 45 \cdot 1 - 6 \cdot 2 \left(\frac{9 - 11}{3}\right) + \left(\frac{9 - 11}{19}\right) \left(\frac{9 - 8}{18}\right) \frac{x_{0} \cdot y_{1}}{182}$$

$$+ \frac{(9 - 11)(9 - 8)(9 - 5)}{162} - x_{0} \cdot 1$$

$$= 45 \cdot 1 + 6\frac{1}{15} - \frac{2}{75} - \frac{2}{403} - \frac{2}{95} - \frac{2}{403} - \frac{2}{95} - \frac{2}$$

Questions The numerical method of solving linear equations is of two types one is direct, other is	opt1	opt2	opt3	opt4	opt7
method.	iterative	elimination	Newton	none	iterative
In Gauss –Jordan method the coefficient matrix is transformed into matrix	scalar	unit	diagonal	column	unit
The convergence in Gauss -Jacobi method can be achieved only when coefficient of thematrix is			8		
dominant	row wise	column wise	diagonally	none	diagonally
Gauss -Elimination and Gauss -Jordan are direct methods while Gauss -Jacobi and Gauss -					
Seidal are methods	iterative	elimination	interpolation	none	iterative
The convergence of Gauss – Seidal method is times as fast as in Jacobi's method	1	2	3	4	3
The power method will work satisfactorily only if A has a Eigen value In power method the element in vector in each iteration will become very large, to avoid this we	small	large	equal	dominant	dominant
divide each vector by its component	smallest	largest	positive	negative	largest
Gauss – Jordan method is method	direct	indirect	iteration	interpolation	direct
Gauss – Jacobi method is method	direct	indirect	iteration	interpolation	indirect
Gauss – Jacobi method is method	direct	indirect	iteration	interpolation	iteration
Gauss – Seidal method is method	direct	indirect	iteration	interpolation	indirect
Gauss – Jordan method fails if the element in top of first column is	0	1	2	3	0
The successive approximations are called	interpolation	elimination	iterates	approximation	iterates
method is a self - correcting method.	interpolation	elimination	iterates	approximation	iterates
In Gauss - Jacobi and Gauss - Seidal methods the co-efficient matrix must bedominant.	row wise	column wise	none	diagonally	diagonally
The matrix is if the numerical value of the leading diagonal element in each row is					
greater than or equal to the sum of the numerical value of other element in that row.	orthogonal Gauss	symmetric	diagonally dominant	singular	diagonally dominant
The Gauss – Jordan method is the modification of method.	-Elimination	Gauss – Jacobi	Gauss – Seidal	interpolation	Gauss -Elimination
The iterative procedure for finding the dominant Eigen value of the matrix is called Power method.	D 1 1 1	o :	N		D 1 11
	Rayleigh's	Gaussian	Newton's	inverse	Rayleigh's
$x^2 + 5x + 4 = 0$ is a equation.	algebraic	transcendental	wave	heat	algebraic
$a + b \log x + c \sin x + d = 0$ is a equation.	algebraic	transcendental	wave	heat	transcendental
In Gauss – Jordan method, the augmented matrix is reduced intomatrix	upper triangular	lower triangular	diagonal	scalar	diagonal
The 1st equation in Gauss – Jordan method, is called equation.	pivotal	dominant	reduced	normal	pivotal
The element in Gauss – Jordan method is calledelement.	Eigen value	Eigen vector	pivot	root	pivot
Power method generally gives the largest Eigen value of A provided the Eigen values are The system of simultaneous linear equation in n unknowns $AX = B$ if A is diagonally Dominant	equal	negative	positive	real and distinct	real and distinct
then the system is said to be system	dominant	diagonal	scalar	singular	diagonal
The convergence of Gauss - Seidal method is roughly that of Gauss - Jacobi method	twice	thrice	once	4times	twice
In power method iterative process is repeated until becomes negligibly small.	X_r-X_(r-1)	X_(r-1)- X_r	$X_r-X(r+1)$	$X_{(r+1)} - X_r$	X_r-X_(r-1)
Cholesky's method is used for finding the of a matrix.	determinant	value	inverse	rank	determinant
The smallest eigen value of A is the reciprocal of the dominant eigen value of	A^(-1)	det A	A^T	А	A^(-1)
Choleskey's method is used only when the matrix is	symmetric	skew-symmetric	singular	non-singular	symmetric
The Power method is used for finding eigen value	dominant	least	central	positive	dominant
The Inverse Power method is used for findingeigen value	dominant	least	central	positive	dominant
Jacobi's method is used only when the matrix is	symmetric	skew-symmetric	singular	non-singular	symmetric
Crout's method is a method to solve simultaneous linear equations.	Direct	Indirect	real	inverse	Direct
In Crout's method, if AX=B, then	LX=B	UX=B	L=B	LUX=B	LUX=B
,,				LOA D	Lost D

UNIT - 3 8015290573 Numerical Differentiation and Integration Numerical differentiation It is the Process of Finding the Values of dy, dy + dy, for some particular value q x. find the first derivatures of f(x) at x=2for the data f(-1) = -21, f(1) = 15, f(2) = 120 F(3) = 3 using Newton's divided difference formula. Poln 3 2 X -1 y -21 15 12 3 The Newton's divided diggenence formula is $y = y_0 + (n - x_0) + y_0 + (n - n_0) (x - x_0) + y_0^2$ +(x-x0)(x-x,)(x-x,) \$ 43/ +

The neuton's divided difference formula is $y = p(x) = y_0 + (x - x_0) \neq y_0 + (x - x_0) (x - x_1) \neq y_0$ +(x-x0)(x-x,)(x-x2) 43/0+ 4 ==== (x) (4===) AFIX) FIX) X 3 -13 18 16 23 5 146 0 899 40 11 1026 69 27 17315 2613 35606 34 y = f(x) = -13 + 18(x - 3) + 16(x - 3)(x - 5)+ (x-3)(x-5)(x-11) $= -13 + 18 \times -54 + 16 [x^2 + 8x + 15]$ $= -13 + 18x - 54 + 16x^{2} - 128x + 240$ +x3-11x2-8x2+88x +15x-165 $f(x) = x^3 - 3x^2 - 7x + 8$ $f(x) = 3x^2 - 6x - 7$ f (10) = 233.

Neuton's forward formula for derivatives $y = p(x) = y_0 + \frac{u}{1!} \Delta y_0 + \frac{u(u-1)}{2!} \Delta y_0 + \frac{u(u-1)(u-2)}{3!} \delta y_0 + \frac{u(u-1)(u-2)(u-3)}{4!} \Delta^4 y_0 + \cdots$ with 1 in $y' = \frac{1}{5} \left[\Delta y_0 + \frac{(2u-1)}{2!} \Delta^2 y_0 + \frac{(3u^2 - 6u + 2)}{2!} \Delta^2 y_0 + \cdots \right]$ (4u3-18u2+22u-6) 24y,+....] $y'' = \frac{1}{p^2} \left[\Delta^2 y_0 + \frac{(6u-6)}{3!} \Delta^3 y_0 + \frac{(12u^2 - 36u + 22)}{4!} \Delta^3 y_{1} \cdots \right]$ $y'' = \frac{1}{\beta^3} \int \Delta^3 y_0 + (244 - 36) \Delta^4 y_0 + \cdots]$ O Find the first three derivatives of Find the first three derivatives of Find at x = 1.5 & at x = 4.0 using Newlon's forward interpolation formula to the data given below. x 1.5 2 2.5 3 3.5 4 Y 3.375 7 13.625 24 38.875 59 solo $f(x) = \frac{1}{6} \left[\Delta y_0 + \frac{(2u-1)}{2!} \Delta y_0 + \frac{Bu^2 - 6u + 2}{2!} \Delta^3 y_0 \right]$ + (4u³-18u²+22u-6) D⁴y, +...]

 $F''(x) = \frac{1}{h^2} \left[\Delta_{y_0}^2 + (\frac{6u-6}{3!}) \Delta_{y_0}^3 + (\frac{12u^2-36u+22}{4!}) \Delta_{y_0}^4 + \frac{12u^2-36u+22}{4!} \Delta_{y_0}^4 + \frac{12u+36u+22}{4!} \Delta_{y_0}^4 + \frac{12u+36u+22}{4!} \Delta_{y_0}^4 + \frac{12u+36u+22}{4!} \Delta_{y_0}^2 + \frac{12u+36u+22}{4!} \Delta_{y_0}^4 + \frac{12u+36u+22}{4!} \Delta_{y_0$ $F''(y) = \frac{1}{p^3} \int \Delta^3 y_0 + (\frac{24y - 36}{4!}) \Delta^4 y_0 + \cdots$ $u = \frac{\chi - \chi_0}{E} = \frac{\chi - 1.5}{0.5}$ when $\chi = 1.5$ $\int u = 0$ x y Δy Δy Δy Sy sy 1.5 3.375 (3.625) 3 6.625 0.75 2 0 2.5 13.625 3.75 10.375 0.75 4.5 3 24 14.875 0.75 0 5-25-3.5 38.875 20.125 4 59

$$\begin{aligned} f'_{(1,5)} &= \frac{1}{0.5} \int 3.625 + (0-1) \cdot \frac{3}{2} + \frac{3}{6} (0.75) \\ &= \frac{1}{0.5} \int 3.625 - 1.5 + 0.25 \\ &= \frac{1}{0.5} \int 3.625 - 1.5 + 0.25 \\ &= \frac{1}{0.5} \int 3.625 - 1.5 + 0.25 \\ &= \frac{1}{0.5} \int 3.625 - 1.5 \\ &= \frac{1}{0.5} \int 3.65 - 1.5 \\ &= \frac{1}{0.5} \int 3.65$$

 $F''(x) = \frac{1}{R^2} \left[\Delta_y^2 + (\frac{6u-6}{3!}) \Delta_y^3 + (\frac{12u^2 - 36u+22}{4!}) \Delta_y^4 + \frac{12u^2 - 36u+22}{4!} \Delta_y^4 + \frac{12u+22}{4!} \Delta_$ $u = \frac{\chi - \chi_0}{R} = \frac{\chi - 1.5}{0.5}$ When $\chi = 1.5$ $\int u = 0$ y sy sy sy Sy x 1.5 3.375 (3.625) 3 0.15 2 6.625 0 3.75 13.625 0 0.75 10:375 4.5 0 24 3 14.875 0.75 5.25 3.5 38.875 20.125 4 59

y = 1 20.125 + 1×5.25 + 2×0.75] $y'' = \frac{1}{0.5^2} \left[5.25 + 6 \times \frac{0.75}{6} \right] = 24$ $y''' = \frac{1}{0.53} \int 0.75 \int = 6$. For the given data, find the first two desirvatives at x = 1.1x 1.0 1.1 1.2 1.3 1.4 1.5 1.6 y 7.989 8.403 8.781 9.129 9.451 9.750 10.031 $\begin{aligned} y' &= \frac{1}{R} \left[\Delta y_0 + (\frac{2u-1}{2!}) \Delta^2 y_0 + (\frac{3u^2 - 6u + 2}{3!}) \Delta^2 y_0 \right] \\ &+ (\frac{4u^3 - 18u^2 + 22u - 6}{3!}) \Delta^4 y_0 + \cdots \end{aligned}$ $y'' = \frac{1}{R^2} \left[\Delta^2 y_0 + \frac{(6u-6)}{31} \Delta^3 y_0 + \frac{(12u^2 - 36u + 22)}{4} \Delta^3 y_$ $u = \frac{\chi - \chi_0}{h} = \frac{\chi - 1.0}{0.1}$ At $x = 1 \cdot 1$ $u = \frac{1 \cdot 1 - 1 \cdot 0}{0 \cdot 1} = 1$.

=-36 + 0.00016 = -35 - 9998 - 3.5843 find the first two derivatives $9 \times \frac{1}{3}$ at x = 50 and x = 56 for the given data 56 51 52 53 54 155 y=x"3 3.6840 3.7084 3.7325 3.7563 3.7798 3.8030 × 3-8259 545 55 1 1º Solo D D ry. x 3-6840 SD 0.0244 -0.0003 51 3-1084 C 0.0241 0 -0.0003 3.7325 52 0.0238 6 0 -0.0003 3.7563 0 53 0 0.0235 0 0 - 0.0003 3.7198 0 54 0 0.0232 -0.0003 3 8036 55 0.0229 3.8259 56 Neuton's Jonward Jornula: $y' = \frac{1}{R} \left[\Delta y_0 + \frac{(2u-1)}{2!} \Delta^2 y_0 + \frac{(2u^2 - 6u + a)}{2!} \Delta^3 y_0 + \frac{(2u^2 - 6u + a)}{2!} \Delta^3 y_0 + \frac{(4u^3 - 18u^2 + 22u - 6)}{2!} \Delta^4 y_0^2 + \frac{(2u^2 - 6u + a)}{2!} \Delta^3 y_0 + \frac{(2u$ 41

=-36 + 0.00016 = -35 - 9998 - 3.5843 find the first two derivatives 9×3 at x = 50 and x = 56 for the given data 2 50 51 52 53 54 55 y=x^{1/2} 3.6840 3.7084 3.7325 3.7563 3.7798 3.8030 56 3-8259 545 55 1 1º Solo A xryro 3-6840 50 0.0244 -0.0003 51 3.7084 00241 0 -0.0003 3.1325 52 0.0238 3.7563 0.0235-6 0 -0.0003 0 0 53 0 0 - 0.0003 0 3.7198 54 0 0.0232 -0.0003 55 3 8036 0.0229 3.8259 56 Neutonis Jonward Jornula: $y' = \frac{1}{R} \left[\Delta y_0 + \frac{(2u-1)}{2!} \Delta^2 y_0 + \frac{(2u^2 - 6u + a)}{2!} \Delta^3 y_0 + \frac{(2u^2 - 6u + a)}{2!} \Delta^3 y_0 + \frac{(2u^2 - 18u^2 + 28u - 6)}{2!} \Delta^4 y_0 + \frac{(2u^2 - 18u^2 + 28u - 6)}{2!} \Delta^4 y_0 + \frac{(2u^2 - 18u^2 + 28u - 6)}{2!} \Delta^4 y_0 + \frac{(2u^2 - 6u + a)}{2!} \Delta^3 y_0 + \frac{(2u^2 - 6u + a)}{2!} \Delta^4 y_0 + \frac{(2u^2 - 6u + a)}{2!}$ 41

$$\begin{split} y'' &= \frac{1}{R^{2}} \left[A^{2}y_{0} + \left(\frac{6u-6}{2i} \right) A^{3}y_{0} + \left(\frac{i_{2}u^{2}-36u+2i}{4i} \right) A^{4}y_{0} + \cdots \right) \\ u &= \frac{v-v_{0}}{R} = \frac{50-50}{1} = 0 \\ y' &= \frac{1}{R} \left[0 \cdot 02414 + \frac{(-1)}{2} \right] \left(-0.0003 \right) \\ &= 0.0244 + 0.0002 \\ &= 0.0244 \\ y'' &= \frac{1}{R} \left[-0.0003 \right] = -0.0003 \\ &, \\ Neulon's Backward Intempolation formula \\ y' &= \frac{1}{R} \left[\nabla y_{0} + \frac{(2v+1)}{2i} \nabla^{2}y_{0} + \frac{(3v^{2}+6v+3)}{3i} \nabla^{2}y_{0} \\ &+ \left(\frac{3v^{2}+18v^{2}+22v+6}{3i} \right) \nabla^{4}y_{0} + \frac{(-1)v^{2}+26v+22}{4i} \nabla^{4}y_{0} \right] \\ y'' &= \frac{1}{R^{2}} \left[\nabla^{2}y_{0} + \frac{(6v+6)}{3i} \nabla^{3}y_{0} + \frac{(-1)v^{2}+26v+22}{4i} \nabla^{4}y_{0} \right] \\ \psi'' &= \frac{1}{R^{2}} \left[\nabla^{2}y_{0} + \frac{(6v+6)}{3i} \nabla^{3}y_{0} + \frac{(-1)v^{2}+26v+22}{4i} \nabla^{4}y_{0} \right] \\ \psi'' &= \frac{v-x_{0}}{R} = \frac{v-56}{0.5} \\ y' &= \frac{1}{0.5} \left[0.0299 + \frac{(0+1)}{2i} (-0.0003) + \frac{2}{3i} (0) + 0 \right] \\ &= \frac{1}{0.5} \left[0.0299 + \frac{0.0003}{2} + 0 \right] \\ y''' &= \frac{1}{0.5} \left[-0.0008 \right] = -0.0012. \end{split}$$

Numerical Integration
Trapensidal suble

$$T = \int_{a}^{b} F(x) dx = \frac{h}{2} \int_{a}^{b} (\beta um q) first and last
ordinate) + 2(\beta um q)
R = \frac{b-a}{n}$$
Simpsions 1/3 suble

$$I = \int_{a}^{b} F(x) dx = \frac{h}{3} \int_{a}^{b} (2jinst + last) + h(\beta um q) odd
ordinates) + 2(\beta um q) even
ordinates)]
R = \frac{b-a}{n} - [nutliples q 2]$$
Simpsions 3/0 suble

$$T = \frac{3h}{8} \int_{a}^{b} (jinst + last) + 2(\beta um q) nutliples q 3)$$

$$R = \frac{b-a}{n} - [nutliples q 2]$$

$$R = \frac{b-a}{n} \int_{a}^{b} (jinst + last) + 2(\beta um q) nutliples q 3)$$

$$R = \frac{b-a}{n} \int_{a}^{b} (linst + last) + 2(\beta um q) nutliples q 3)$$

$$R = \frac{b-a}{n} \int_{a}^{b} (linst + last) + 2(\beta um q) \int_{a}^{b$$

$$\begin{split} \frac{Soln}{h} & h = \frac{b-a}{n} = \frac{1+i}{8} = \frac{2}{8} = 0.25^{\circ} \\ \frac{x}{y} & -1 & -0.75 & -0.5 & -0.25 & 0 & 0.27 & 0.5 & 0.77 & 1 \\ \frac{y}{y} & 0.5^{\circ} & 0.65 & 0.8 & 0.94i2 & 1 & 0.94i0 & 0.8 & 0.64i & 0.57 \\ \hline I & = \frac{R}{2} \left[\left(y_0 + y_0 \right) + 2 \left(y_1 + y_2 + y_3 + y_4 + y_5 + y_6 + y_7 \right] \\ & = \frac{0.25}{2} \left[(0.57 + 0.5^{\circ}) + 2 \left(0.67 + 0.8 + 0.94i2 + 1 + 0.94i2 + 0.8 + 0.64i \right) \right] \\ & = \frac{0.25}{2} \left[12.5248 \right] \\ & = 1.5656 \\ \hline 2) Evaluale \int_{0}^{1} \frac{1}{1+x^2} dx \quad with \quad h = V_6 \quad by \\ Trapeopoidal \quad 5nule \\ & \frac{30in}{p(x)} = \frac{1}{1+x^2} \quad h = \frac{1}{8} \\ & \frac{9}{1} \quad 0 \quad \frac{1}{22} \frac{2}{6} \quad \frac{3}{2} \quad \frac{41}{6} \quad \frac{5}{6} \quad 1 \\ & \frac{3}{3} \quad \frac{3}{37} \quad \frac{9}{16} \quad \frac{4}{7} \quad \frac{7}{3} \quad \frac{3}{61} \quad \frac{1}{2} \end{split}$$

By actual Integration

$$I = \int_{0}^{1} \frac{1}{1+x^{2}} dx = \int \tan^{-1}x \int_{0}^{1} \frac{1}{2} = \tan^{-1} 6 - \tan^{-1} 6$$

$$I = \int_{0}^{1} \frac{1}{1+x^{2}} dx = \int \tan^{-1}x \int_{0}^{1} \frac{1}{2} = \tan^{-1} 6 - \tan^{-1} 6$$

$$= 1 \cdot 40564745^{2}$$
Evaluate $\int \frac{1\cdot 3}{\sqrt{x}} dx = \tan \pi \frac{1}{2} + \frac{1}{2$

$$\begin{aligned} \mathbf{T} &= \frac{h}{2} \left[\left(y_{0} + y_{1} \right) + 2 \left(y_{1} + y_{2} + y_{3} + y_{4} + y_{5} \right) \right] \\ &= \left(\frac{h}{2} \right) \left[\left(1 + \frac{h}{2} \right) + 2 \left(\frac{36}{374} + \frac{9}{10} + \frac{h}{5} + \frac{9}{13} + \frac{36}{61} \right) \right] \\ &= \frac{1}{12} \left[\frac{3}{2} + 2 \left(3 \cdot 9554 \right) \right] \\ &= \frac{1}{12} \left[\frac{3}{2} + 7 \cdot 9108 \right] \\ &= 0.78 + 2. \end{aligned}$$

$$(3) Evaluate \int \frac{6}{1 + x^{2}} dx \quad by \quad Trapemoidal stule \\ Also \quad check \quad up \quad Ke \quad grenults \quad by \quad actual \\ Trategration \\ \\ koin \\ \mathbf{F}(\pi) = \frac{1}{1 + \pi^{2}}, \quad \mathbf{h} = \frac{b - \alpha}{\alpha} = \frac{6 - \Theta}{6} = \mathbf{E} \mathbf{1} \\ &\times \quad \mathbf{0} \quad \mathbf{1} \quad \mathbf{2} \quad \mathbf{3} \quad \mathbf{h} \quad \mathbf{5} \quad \mathbf{6} \\ &y \quad 1.00 \quad \mathbf{0} \cdot 500 \quad \mathbf{0} \cdot 200 \quad \mathbf{0} \cdot 100 \quad \mathbf{0} \cdot 0584 + \mathbf{0} \cdot 038446 \quad \mathbf{0} \cdot 27026 \\ \mathbf{T} = \frac{R}{2} \int \left((y_{0} + y_{6}) + 2 \left(y_{1} + y_{2} + y_{3} + y_{4} + y_{5} \right) \right) \\ &= \frac{1}{2} \int (1 + \mathbf{0} \cdot \mathbf{0} \cdot 7037) + 2(\mathbf{0} \cdot \mathbf{5} + \mathbf{0} \cdot 2 + \mathbf{0} \cdot 1 \\ &+ \mathbf{0} \cdot \mathbf{0} \cdot 58824 + \mathbf{0} \cdot 038462 \right) \mathbf{T} \\ &= 1 \cdot 41079 \, 950 \end{aligned}$$

By actual Integration

$$I = \int_{\delta} \frac{1}{1+x^{-}} dx = \int tan^{-1}x \int_{0}^{\delta} = tan^{-1} \delta - tan^{-1} \delta$$

$$I = \int_{\delta} \frac{1}{1+x^{-}} dx = \int tan^{-1}x \int_{0}^{\delta} = tan^{-1} \delta - tan^{-1} \delta$$

$$= 1 + h0 5 6 h7 4 5^{-}$$
Evaluate
$$\int \frac{1 \cdot 3}{1 \cdot 0} dx taking h = 0.05 \quad by$$

$$trapenyoidal = 5 nale$$
Soln
$$f(x) = \sqrt{x}$$

$$h = \frac{b-\alpha}{n} = 0.0J^{-}$$

$$x = 1 \cdot 0 + 05 \quad 1 \cdot 1 + 15 \quad 1 \cdot 2 + 124^{-} + 1.3$$

$$y = 1 + 0247 + 10 h84 + 10724 + 10754 + 1180 + 14622$$

$$I = \frac{\beta}{2} \left[(t_{0} + y_{0}) + 2(y_{1} + y_{2} + y_{3} + y_{4} + y_{5}) \right]$$

$$= 0.05 \quad \left[(1 + 1 \cdot h\alpha^{2}) + 2(1 \cdot 0247 + 1 \cdot 0488 + 1 \cdot 07244 + 1 \cdot 0954 + 1 \cdot 1186) \right]$$

$$= 0.1 \quad \left[2 \cdot 1402 + 10 \cdot 7186 \right]$$

$$= 0.1 \quad \left[2 \cdot 1402 + 10 \cdot 7186 \right]$$

$$= 0.1 \quad \left[2 \cdot 1402 + 10 \cdot 7186 \right]$$

$$= 0.1 \quad \left[2 \cdot 1402 + 10 \cdot 7186 \right]$$

(5) Dividing the range into 10 equal parts find the value of 5 The dx by Simpsons 1/3 sule. Solo $f(x) = \sin x$ $f_{h} = \frac{b-q}{n} = \frac{\pi}{20} = \frac{\pi}{20}$ 20 0 T1/20 2T1/20 3T1/20 4T1/20 5T1/20 6T5/20 TT1/20 8T1/20 F1X1 0 0.1564 0.3070 0.4540 0.5818 0.7071 0.8070 0.8910 0.9511 . $I = \frac{h}{3} \left[(y_0 + y_8) + 4 (y_1 + y_3 + y_5 + y_7) \right]$ +2(4,+4,+4,)] $= \frac{11}{20} \int (0+1) + 4 (0.1564 + 0.4540 + 0.7071 + 0.8910)$ +2(0.3090+0.5878+0.8090)] = 11/0 × 19.0986 = 1 The velocity 2° 9° a particle at a distance 3° prom a point on its path is gn by the table below. S 0 10 20 30 40 50 60 V 47 58 64 65 61 52 38 Estimate the time taken to travel bo meters by simpsons 1/3 oule.

COURSE MATERIAL(NOTES)

Velouty = distance time $v = \frac{ds}{4t}$ $dt = \int \frac{1}{60} ds = 10$ $t = \int \frac{1}{5} ds = 10$ $T = \int_{V}^{60} \frac{1}{4s} = \frac{h}{3} \left[(y_0 + y_6) \right]$ $+q(y_1 + y_3 + y_5) + q(y_2 + y_4)]$ V 47 58 64 65 61 52 38 V 0.02127 0.01724 0.015625 6.01828 0.01625 0.01923 0.026311 $\begin{aligned} \overline{I} &= \frac{10}{3} \left[(0.02127 + 0.026316) \\ &+ 4 (0.07124 + 0.01538 + 0.0923) \\ &+ 2 (0.015625 + 0.01639) \right] \\ &+ 2 (0.015625 + 0.01639) \right] \end{aligned}$ (F) Compute J^{T/2} Sinx dx using Simpson's 3/6 th orule of numerical integration

 $\frac{Solo}{I} = \int \frac{\pi}{2} \sin x \, dx$ $F(x) = \sin x$ $h = \frac{\pi}{2} = \frac{\pi}{18}$ 91 0 TT /18 2TT /18 3TT/18 4TT/18 5TT/18 F(M) 0 0.1193.4 0.3420 0.50 0.6428 0.7660 617/18 TU118 817/18 977/18 0.8610 0.9397 0.9848 1 $I = \frac{3R}{8} \int (y_0 + y_9) + 3(y_1 + y_2 + y_4 + y_5 - + y_7 + y_9)$ +2(4,+46)) $=\frac{317}{8\times18}\int(0+1)+3(0.1736+0.3428+0.6428)$ +0.7660+0.9397+0.9848) + 2 (0:5-+0.8660)] I=0.99998541 I~1 1 102 12 + 0 FID 1 = .

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Romberg Merrod $I = I_2 + \left(\frac{I_2 - I_1}{2}\right)$ sule with h = 1/4, 1/8, 1/16 and then Rombergs Method $\frac{Soln}{I} = \int_{0}^{1/2} \frac{\pi}{\sin x} dx$ $f(\pi) = \frac{\pi}{\sin x}$ i) Take R = 1/4 I1 = 0.507075

(1) Take h= \$ 500 1/8 0 1/8 2/8 3/8 1/8 1 1-0026 1.0105 1-0238 1-0429 4 4 4 4 4 x f(x)
$$\begin{split} I_{2} &= \frac{R}{3} \Big[\left(y_{0} + y_{4} \right) + 4 \left(y_{1} + y_{3} \right) + 2 \left(y_{2} \right) \Big] \\ &= \frac{1}{24} \Big[\left(1 + 1 \cdot 0429 \right) + 4 \left(1 \cdot 0026 + 1 \cdot 0236 \right) \\ &\quad + 2 \left(1 \cdot 010 51 \right) \Big] \\ I_{2} &= 0 \cdot 5070625 \end{split}$$
(iii) Take R = 1/1 $T_{3} = \frac{h}{3} \left[(y_{0} + y_{8}) + 4 (y_{1} + y_{3} + y_{5} + y_{7}) \right]$ +2(42+44+46)] $= \frac{1}{48} \int (1+1.0429) + 4(1.0007+1.0059) + 1.0165 + 1.0326) + 2(1.0026)$ + 1.0105 + 1.0238)] I3 = 0.5070729.

for
$$\overline{I}_{1}$$
, \overline{I}_{2}
Romberg formula is
 $\overline{I}_{4} = \overline{I}_{2} + \left(\frac{\overline{I}_{3}-\overline{I}_{1}}{3}\right)$
 $= 0.5070625 + \left(\frac{0.5070625-0.507075}{3}\right)$
 $\overline{I} = 0.5070558$
for \overline{I}_{3} , \overline{I}_{3}
 $\overline{I}_{5} = \overline{I}_{3} + \left(\frac{\overline{I}_{5}-\overline{I}_{2}}{3}\right)$
 $= 0.5070729 + \left(\frac{0.5070729 - 0.5070(2)}{3}\right)$
 $= 0.507076566$.
Romberg for $\Re \cdot \overline{I}_{4} \neq \overline{I}_{5}$
 $\overline{I} = \overline{I}_{5} + \left(\frac{\overline{I}_{5}-\overline{I}_{4}}{3}\right)$

T Evaluate $I = \int_{1+x^2}^{1} \frac{dx}{1+x^2}$ by using Rombergs method. Hence deduce an approximate value 9^{-11} . a=0; b=1 Solo $f(x) = \frac{1}{1+x^2}$ $I h = \frac{b-a}{2} = \frac{1-a}{2} = 0.5^{-1}$ x 0 0.5 1 P(M) 1 0.8 0.5-
$$\begin{split} I_{1} &= \frac{h}{2} \left[(y_{0} + y_{1}) + 2(y_{1}) \right] \\ &= 0.5 \left[(1 + 0.5) + 2 \times 0.8 \right] \end{split}$$
I, = 0.7750

Stratuate $I = \int_{1+x^2}^{1} \frac{dx}{1+x^2}$ by using Rombergs method. Hence deduce an approximate value q = 11. a = 0; b = 1Solo $f(x) = \frac{1}{1+x^2}$ $Th = \frac{b-a}{2} = \frac{1-0}{2} = 0.5$ ж 0 0.5- 1 Р(м) 1 0.8 0.5-
$$\begin{split} I_{1} &= \frac{h}{2} \left[(y_{0} + y_{1}) + 2(y_{1}) \right] \\ &= \frac{0.5}{2} \left[(1 + 0.5) + 2 \times 0.8 \right] \end{split}$$
I, = 0.7750

COURSE MATERIAL(NOTES)

$$\begin{split} I_{2} &= \frac{0.25}{2} \int (1+0.5) + 2(0.94/2+0.8 + 0.64) J \\ \overline{I_{2}} &= 0.7828 \\ R &= \frac{b-a}{8} \frac{J-a}{8} = 0.125 \\ \hline R &= \frac{b-a}{8} \frac{J-a}{8} = 0.125 \\ \hline \frac{x}{9} &= 0.12 \frac{0.375}{0.9046} \frac{0.375}{0.94/2} \frac{0.5}{0.8} \\ \hline \frac{0.625}{0.7191} \frac{0.77}{0.84} \frac{0.8757}{0.8} \\ \hline \frac{0.625}{0.7191} \frac{0.77}{0.84} \frac{0.8757}{0.8} \\ + 0.94/2 + 0.8767 + 0.8 \\ + 0.7191 + 6.64 + 0.5644 \end{pmatrix} J \\ \hline \overline{I_{3}} &= 0.7848 \\ \hline \overline{I_{3}} &= 0.7848 \\ \hline Romberg \quad Jox \quad \overline{I_{1}} , \overline{I_{2}} \\ \hline I_{4} &= \overline{I_{2}} + \left(\frac{\overline{I_{2}}-\overline{I_{1}}}{3}\right) = 0.7854 \end{split}$$

Romberg for
$$\overline{J}_{2}$$
, \overline{T}_{3}
 $\overline{L}_{5-} = \overline{J}_{3} + \left(\frac{\overline{J}_{3} - \overline{J}_{4}}{3}\right) = 0.7855$
Romborg for \overline{L}_{4} , \overline{L}_{5-}
 $\overline{I} = \overline{I}_{5-} + \left(\frac{\overline{L}_{5-} - \overline{L}_{4}}{3}\right) = 0.7855$
 $\overline{I} = \int_{0}^{1} \frac{dN}{1 + x^{2}}$
 $0.7855 = \int \tan^{-1}N \int_{0}^{1}$
 $= \tan^{-1}(1) - \tan^{-1}(0)$
 $\overline{L}_{4-} = 0.7855^{-}$
 $\overline{H}_{4-} = 3.1420$.
(2) Using Romberg Integration, evaluate
 $\int_{0}^{1} \frac{dx}{1 + x}$
Solon
Here $a = 0$, $b = 1$

$$\frac{7}{10} 0 0.125 0.25 0.375 0.5}{0.467} 0.5}{\frac{7}{10} 1 0.8889 0.8 0.7273 0.467}{0.625 0.75 0.875} 1}{0.6154 0.5714 0.5333 0.5}$$

$$T_3 = \frac{0.125}{2} \int (1+0.5) + 2(0.8889 + 0.8 + 0.7273 + 0.6674 + 0.6154 + 0.5714 + 0.5333)]$$

$$T_5 = 0.69714 + 0.5333)]$$

$$T_5 = 0.69714 + 0.5333)]$$

$$T_4 = T_2 + (\frac{T_2 - T_1}{3})$$

$$= 0.6970 + (0.6970 - 0.7084)$$

$$T_4 = 0.6932$$

$$Romberg for T_1, T_3$$

$$T_5 = T_3 + (\frac{T_3 - T_2}{3})$$

 $= 0.6941 + \left(\frac{0.6941 - 0.6970}{8}\right)$ $\overline{I_5} = 0.6931$ Romberg for I_4, I_5 $I_{6} = I_{5} + \left(\frac{I_{5} - I_{4}}{2}\right)$ $\int I_{6} = 0.6931$ Grauss Quadrature Jornula Quadrature The process of finding a depinite integral prom a tabulated values q a Jundion is known as Quadralione. Graussian two point Quadrature formula Let $I = \int_{a}^{b} f(x) dx$. Take $\chi = \left(\frac{a+b}{2}\right) + \left(\frac{b-a}{2}\right)t$ $dx = \left(\frac{b-a}{2}\right) dt$

By using this transformation

$$I = \int_{-1}^{1} g(t) dt = g(-\frac{1}{\sqrt{3}}) + g(\frac{1}{\sqrt{3}})$$
() Evaluate $\int_{-1}^{1} e^{-x^{2}} \cos x dx$ by Gauss two
Point Quadrative formula:
Sola

$$I = \int_{-1}^{1} e^{-x^{2}} \cos x dx$$

$$F(x) = e^{-x^{2}} \cos x$$

$$I = f(-\frac{1}{\sqrt{3}}) + f(\frac{1}{\sqrt{3}})$$

$$= e^{-\frac{1}{\sqrt{3}}} \cos(-\frac{1}{\sqrt{3}}) + e^{-\frac{1}{\sqrt{3}}} \cos(\frac{1}{\sqrt{3}})$$

$$= e^{-\frac{1}{\sqrt{3}}} \cos(-\frac{1}{\sqrt{3}}) + e^{-\frac{1}{\sqrt{3}}} \cos(\frac{1}{\sqrt{3}})$$

$$= e^{-\frac{1}{\sqrt{3}}} \left[\cos(-\frac{1}{\sqrt{3}}) + \cos(\frac{1}{\sqrt{3}}) \right]$$

$$I = 1 \cdot 2008$$
(2) Apply Gauss two point formula
to evaluate $\int_{-1}^{1} \frac{1}{1+x^{2}} dx$

$$I = \int_{-1}^{1} \frac{1}{1+x^{2}} dx$$

$$f(x) = \frac{1}{1+x^{2}}$$

$$T = F\left(\frac{1}{\sqrt{3}}\right) + F\left(\frac{1}{\sqrt{3}}\right)$$

$$= \frac{1}{1+\left(\frac{1}{\sqrt{3}}\right)^{2}} + \frac{1}{1+\left(\frac{1}{\sqrt{3}}\right)^{2}}$$

$$= \frac{3}{4} + \frac{3}{4}$$

$$= \frac{6}{4}$$

$$= \frac{1}{4}$$

$$= \frac{6}{4}$$

$$= \frac{1}{1+x^{4}}$$

$$T = \int_{1}^{2} \frac{2x}{1+x^{4}} dx$$

$$f(x) = \frac{2x}{1+x^{4}}, \quad a = 1, \quad b = 2$$

$$x = \frac{a+b}{2} + \left(\frac{b-a}{2}\right)t$$

$$x = \frac{3}{2} + \frac{1}{2}t$$

$$dx$$

÷

$$\begin{split} \overline{L} &= \int \frac{A'\left(\frac{3}{2} + \frac{1}{2}t\right)}{1 + \left(\frac{3}{2} + \frac{1}{2}t\right)} + \frac{dt}{A'} \\ &= \int \frac{1}{1 + \left(\frac{3}{2} + \frac{1}{2}t\right)} dt \\ = \int \frac{1}{1 + \left(\frac{3+t}{2}\right)} dt \\ g(t) &= \frac{3+t}{1 + \left(\frac{3+t}{2}\right)} dt \\ \overline{T} &= g(\frac{1}{\sqrt{3}}) + g(\frac{1}{\sqrt{3}}) \\ &= \frac{3-\frac{1}{\sqrt{3}}}{1 - \left(\frac{3-\frac{1}{\sqrt{3}}}{2}\right)} + \frac{3+\frac{1}{\sqrt{3}}}{1 + \left(\frac{3+\frac{1}{\sqrt{3}}}{2}\right)} \\ &= \frac{1\cdot 2^{11}3}{3\cdot 1530} + \frac{1\cdot 7887}{11\cdot 2359} \\ &= 0\cdot 5434. \end{split}$$

$$= \frac{1}{74} \left[0 \cdot 3259 + 0 \cdot 9454 \right]$$

= 0 \cdot 9985
Graussian Three Point Quadrature pormula:
$$T = \int_{a}^{b} f(x) dx$$

$$Take \quad \chi = \left(\frac{a+b}{2}\right) + \left(\frac{b-a}{2}\right) t$$

$$dx = \left(\frac{b-a}{2}\right) dt$$

$$T = \int_{a}^{b} g(t) dt = \frac{5}{9} \left[g\left(-\sqrt{3}\right) + g\left(\sqrt{3}\right) \right] + \frac{8}{9} g(0)$$

O Evaluate
$$\int_{0}^{t} \frac{dx}{1+x^{2}} \quad using \quad 3 \text{ point Quadrature}$$

formula
Solo
$$T = \int_{0}^{t} \frac{dx}{1+x^{2}}, \quad q = 0, \quad b = 1$$

$$Take \qquad \chi = \left(\frac{a+b}{2}\right) + \left(\frac{b-a}{2}\right)t$$

 $dx = \left(\frac{b-a}{2}\right) dt$ =) x= - + - t $dx = \frac{1}{2} dt$ $T = \int \frac{\frac{1}{2} dt}{1 + (\frac{1+t}{2})^2} = \frac{1}{2} \int \frac{dt}{1 + (\frac{t+t}{2})^2}$ $g(t) = \frac{1}{1 + \frac{1+t}{2}}$ $I = \frac{1}{2} \left[\frac{5}{3} \left[\frac{9(-\sqrt{3})}{2} + \frac{9(\sqrt{3})}{2} \right] + \frac{8}{3} \frac{9(0)}{2} \right]$ $=\frac{1}{2}\left[\frac{5}{9}\left(\frac{1}{1+\left(\frac{1+(\sqrt{3}r)}{2}\right)^{2}}+\frac{1}{1+\left(\frac{1+(\sqrt{3}r)}{2}\right)^{2}}\right]$ + 8 [1+1/2)] $=\frac{1}{2}\int \frac{5}{9}\left(0.9875 + 0.5595 + 0.7111\right)$ =0.7853.

(2) Apply three point Graundan Quadratione
yormula to evaluate
$$\int_{0}^{1} \frac{\sin n}{\pi} dn$$

 $T = \int_{\infty}^{1} \frac{\sin n}{\pi} dn$
 $p(n) = \frac{\sin n}{\pi}, a=0, b=1$
 $n = (\frac{b+a}{2}) + (\frac{b-a}{2}) t$
 $dn = (\frac{b-a}{2}) dt$
 $=) n = \frac{1}{2} + \frac{1}{2}t = \frac{1}{2}(1+t)$
 $dn = \frac{1}{2} dt$
 $T = \int_{-1}^{1} \frac{\sin k(1+t)}{\frac{1}{2}(1+t)} \cdot \frac{1}{2} dt$
 $= \int_{-1}^{1} \frac{\sin k(1+t)}{\frac{1}{2}(1+t)} dt$
 $i = g(t) = \frac{\sin k}{1+t} = 0.47943$
 $g(n) = \sin k = 0.47943$
 $g(n) = \sin k = 0.47943$
 $g(n) = \sin k = 0.47943$

$$\begin{split} \Im(-\sqrt{\frac{3}{5}}) &= \sin \left[\frac{-\sqrt{\frac{3}{5}} + 1}{2} \right] \\ = \frac{0 \cdot 1125}{0 \cdot 2254} = 0 \cdot 493 \\ \overline{I} &= \frac{5}{7} \left[\Im(-\sqrt{\frac{3}{5}}) + \Im(\sqrt{\frac{3}{7}}) \right] + \frac{8}{7} \Im(0) \\ &= \frac{5}{7} \left[0 \cdot 499 + 0 \cdot 4377 \right] + \frac{8}{7} (0 \cdot 47943) \\ &= 0 \cdot 52 + 0 \cdot 42616 \\ &= 0 \cdot 94616. \end{split}$$

$$= \sum_{i=1}^{n} \chi = \frac{1+i}{i}$$

$$dx = dt$$

$$\int = \int \frac{(x+i)^{2}}{(1+1)^{2} + \frac{3}{4}(2+i)+1} dx$$

$$g(t) = \frac{(x+i)^{2} + \frac{3}{4}(2+i)+1}{1+1(x+i)+1/4} dx$$

$$g(t) = \frac{(x+i)^{2} + \frac{3}{4}(2+i)+1}{1+((x+i))+1/4}$$

$$g(t) = \frac{x^{2} + \frac{9x+1}{4} + \frac{9x+2}{4} + 1}{1+((x+2))^{4}}$$

$$g(t) = \frac{4}{1+(x+2)^{4}}$$

Integration Double + 4 (Sum q interier Values)] Simpson's grule $I = \frac{kk}{9} \int Sum 9 four corners +$ 2 (Sum of odd position values) + 4 (Sum of even position values) Boundary + 4 (Sum q odd position values) + 8 (Sum q even position values) add mus +8 (Sum g odd position values) + 16 (Sum g even position values) even rours I = hk & Sylon of Jown com

$$\begin{aligned} \overline{T} &= \frac{0!x_{0}\cdot 1}{4} \left[0.5 + 0.4167 + 0.4545 + 0.3846 \\ &+ 2\left[0.4762 + 0.4545 + 0.4348 + 0.4762 \\ &+ 0.4 + 0.4348 + 0.4167 + 0.4 \right] \\ &+ 10.4545 + 0.4348 + 0.4167 \right] \\ &= \frac{0.1\times0.1}{4} \left[1.7558 + 6.9864 + 5.2246 \right] \\ &= \frac{0.1\times0.1}{4} \times 13.9662 = 0.0349 \\ &= \frac{0.1\times0.1}{4} \times 13.9662 = 0.0349 \\ &= \frac{1}{4} \int_{1}^{2} \frac{2}{x^{2}+y^{2}} dx dy, \quad \text{numerically using along y-direction and } k = 0.257 \\ &\text{along y-direction} \\ &\text{gills} \quad \overline{T} = \int_{1}^{2} \int_{1}^{2} \frac{2}{x^{2}+y^{2}} dx dy \\ &f(x, y) = \frac{1}{x^{2}+y^{2}} \\ &\text{By Traperpoidal} \\ &\overline{T} = \frac{f_{1}k}{4} \int 8um & g \text{ Jown Corners } + \\ &= 2(Sum & g \text{ remaining boundary}) \\ &+ 4(Sum & g \text{ intervious}) \end{bmatrix} \end{aligned}$$

1.6 1.8 100 1.2 1.4 2 x 0.4098 0.3378 0.2809 0.2359 0.2 0.5 0-3902 0-3331 0-2839 0-2426 0.2082 0-1798 1.25 0-30170-2710 0-2375 0-2019 0-1821 0.16 1.5 0.2462 0.222 0.1991 0.1779 0.1587 0.1416 1.75 0.2 0.1838 0.1679 0.1524 0.1381 0.125 2 $I = \frac{(0.2)(0.25)}{4} \int 0.5 + 0.2 + 0.2 + 0.125$ +2 (0.4098+0.3378+0.2809+0.2359 + 0.-1798+ 0-16 + 0-1416 + 0.1381+0.1524+0.1679+0.1838 +0.2462+0.2710+0.3331) +4(0.3331+0.2839+0.2426 +0.2082+0.2710+0.2375 +0.2079+0.1821+0.222) + 0.1991 + 0.1779 + 0.1587)] $\frac{(0\cdot 2)(0\cdot 25)}{4} \left[1\cdot 025 + 6\cdot 6642 + 10\cdot 8964\right]$ = 0.2323.

3. Evaluate
$$T = \int_{0}^{1/2} \int_{0}^{1/2} \frac{\sin(2y)}{1 + xy} dx dy using$$

Simpton's stude with $R = k = 2k_{y}$
Set
$$T = \int_{0}^{1/2} \int_{0}^{1/2} \frac{\sin(2xy)}{1 + xy} dx dy$$

$$F(x,y) = \frac{\sin xy}{1 + xy}$$
By Simpsons $\frac{1}{2}$ stude,

$$T = \frac{Rk}{9} \int Sum g \quad forus \quad corners + 2(\frac{2}{3} \frac{um g \quad odd \quad position} + H(3 EP) + H(3 EP) + H(\frac{30p}{2}) + 8(\frac{3EP}{2}) + H(\frac{30p}{2}) + 1H(S EP) + H(\frac{30p}{2}) + 1H(S EP) + \frac{1}{2} \frac{1}{2$$

 $T = \frac{0.1 \times 0.1}{9} \int 0.5 + 0.4167 + 0.3571 + 0.2976$ + 2 [0.4545+0.4167+0.3267+0.340] + 4/0.4762 + 0.4348 + 0.3788+ 0.3205-+ 0.3401+0.3106+0.4545+0.3846) +4(0.3788) +8 (0.3968+0.363) + 8 (0.4132+0.3497) + 6 (0.4329 + 0.3953 +0.3663+0.3344) 7 = 0.1x0 1.5714 + 3.0862 + 12.4004 +1.5152 +6.0728+6.1032 +24.4624] I=0.0613 5 Evaluate JJ 4xy dx dy using Simpsons suche by taking h= 1/4 + k= 1/2 Solo I = J J Havy dx dy Here f(x,y) = 4xy R=0.25 k=0.5

0.15 0.5 0.25 0 X 0 0 0 0 0 0.5 0.5 1.5 2 6971 0 2 3 4 0 6 1.5 3 4.5 1.5 6 O 8 4 2 2 0.25×0.5 [8+16+64+8+32+32 9 +128] F= I=4.

Questions	opt1	opt2	opt3	opt4	opt7
The process of computing the value of the function inside the given range is called	Interpolation	extrapolation	reduction	expansion	Interpolation
If the point lics inside the domain [x_0, x_n], then the estimation of f(y) is called	Interpolation	extrapolation	reduction	expansion	Interpolation
The process of computing the value of the function outside the given range is called	Interpolation	extrapolation	reduction	expansion	extrapolation
If the point lies outside the domain [x_0, x_n], then the estimation of f(y) is called	Interpolation	extrapolation	reduction	expansion	extrapolation
∆ is called difference operator.	forward	backward	central	none	forward
∇ is called difference operator.	forward	backward	central	none	backward
In the forward difference table yo is called element.	leading	ending	middle	positive	leading
In the forward difference table Δy_0 , $\Delta^2 y_0$, are called difference.	leading	ending	middle	positive	leading
The difference of first forward difference is called	divided difference	2nd forward difference	3rd forward difference	4th forward difference	2nd forward difference
Gregory – Newton forward interpolation formula is also called as Gregory – Newton forward formula. Gregory – Newton backward interpolation formula is also called as Gregory – Newton backward	Elimination	iteration	difference	distance	difference
formula Gregory – Newton backward interpolation formula is also called as Gregory – Newton backward	Elimination	iteration	difference	distance	difference
formula.	Elimination	iteration	difference	distance	difference
The divided differences are in their arguments.	constant	symmetrical	varies	singular	symmetrical
In Gregory – Newton forward interpolation formula 1st two terms of this series give the result for the					
interpolation. Gregory – Newton forward interpolation formula 1st three terms of this series give the result for the	Ordinary linear	ordinary differential	parabolic	central	Ordinary linear
interpolation.	Ordinary linear	ordinary differential	parabolic	central	parabolic
Gregory – Newton forward interpolation formula is mainly used for interpolating the values of y near the	Ordinary linear	ordinary differentiai	parabone	central	parabone
of the set of tabular values.	beginning	end	centre	side	beginning
Gregory - Newton backward interpolation formula is mainly used for interpolating the values of y near the of	0 0				0 0
the set of tabular values.	beginning	end	centre	side	end
From the definition of divided difference (u-u_0)/(x-x_0) we have=	(y, y_0)	(x, y)	(x_0, y_0)	(x, x_0)	(x_0, y_0)
If f(x) =0, then the equation is called	Homogenous	non-homogenous	first order	second order	Homogenous
The order of $y_{x+3} - 5 y_{x+2} + 7y_{x+1} + y_{x=10x}$ is	2	0	1	3	3
A function which satisfies the difference equation is a of the difference equation.	Solution	general solution	complementary solution	particular solution	Solution
The degree of the difference equation is	The highest powers of y's	erence between the argum	The difference between the constant	The highest value of x	The highest powers of y's
The degree of $(E2-5E+6)yx = e^x is$	2	0	1	3	1
The order of $y(x+3) - y(x+2) = 5x^{2}$ is	3	2	1	0	1
The difference between the highest and lowest subscripts of y are called of the difference equation	degree	order	power	value	order
E-1=	∇	Δ	μ	δ	Δ
Which of the following is the central difference operator?	∇	Δ	μ	δ	δ
1+Δ=	∇	E	μ	δ	E
μ is called the operator	Central	average	backward	displacement	average
The other name of shifting operator is operator	Central	average	backward	displacement	displacement
The difference of constant functions are	0	1	2	3	0
The nth order divided difference of xn will be a polynomial of degree	0	1	2	3	2
The operator Δ is	homogenous	heterogeneous	linear	a variable	linear

Unit - W Initial Value Psychlem for Ordinary dyperential Equation Merrid - 1 Taylor Series: The taylor Series formula $\begin{aligned} y &= y_0 + (x - x_0) \frac{y_0'}{11} + (x - x_0) \frac{y_0''}{21} \\ &+ (x - x_0)^3 \frac{y_0''}{3!} + \cdots \\ & 3! \end{aligned}$ is

1. Use raylor seves method is find

$$y(0,1)$$
 and $y(0,2)$. Given that $\frac{dy}{dx} = 3e^{2} + 2y$
 $y(0) = 0$;
 $3dn$: finen $\frac{dy}{dx} = y = 5e^{2} + 2y$; $y(0) = 0$;
 $The traylor sevies tormula is;
 $y = y_{0} + (2e^{-x_{0}})\frac{y_{0}}{dx} + (x - x_{0})^{2}\frac{y_{0}}{dx} + (2e^{-x_{0}})\frac{y_{0}}{dx} + (x - x_{0})^{2}\frac{y_{0}}{dx} + (x - x_{0})\frac{y_{0}}{dx} + (x - x_{0})\frac{y_{0}}{dx$$

Numerical Methods – MA6459

2 use taylor series method, solve
$$\frac{du}{dx} = x^{2} - y$$
,
 $y(b) = i$ at $x = 0.1 , 0.2, 0.3$.
solve $\frac{du}{dx} = x^{2} - y$,
 $y = y_{0} + (x - x_{0}) \frac{u}{dx} + (x - x_{0})^{2} \frac{u}{dy} + (x - x_{0})^{3} \frac{u}{dy} + \frac{1}{x^{2}}$
 $y' = x^{2} - y$; $\frac{1}{y} y(b) = 1$
 x $0 x_{0}$
 $y' = x^{2} - y$; $\frac{1}{y} y(b) = 1$
 $y' = x^{2} - y'$; $\frac{1}{y} y(b) = 1$
 $y'' = 2 - y''$; $\frac{1}{y} y''_{0}$
 $y''' = -y'''$; $\frac{1}{y} y''_{0}$
 $y'' = -y'''$; $\frac{1}{y} y''_{0}$
 $y'' = -y'''$; $\frac{1}{y} y''_{0}$
 $y' = 1 + (x - b) (\frac{1}{(1)}) + (x - b)^{2} \frac{1}{x^{2}} + (x - b)^{3} \frac{x}{x} + \frac{1}{x^{3}}$
 $(x - b)^{3} (\frac{-1}{x^{1}})$
 $y = 1 + x + 2y'_{2} + 2y'_{3} - \frac{x^{3}}{x^{3}}$
 $y(b, 1) = b + 0$

Numerical Methods – MA6459

$$= \frac{7}{16} \frac{x^{4} + \frac{1}{18} x^{3}}{y^{2} + x^{2} + x + 1}$$

$$y(0,1) = 1.1115$$

$$y(0,2) = 1.2525$$
A Obtain y by taylor solies method given
that y' = xy + 1; y(0) = 1; dox x = 0.1;
x = 0.2; convect to down desimal places.
Sola: The tornula ist
y = y_{0} + (x - x_{0})\frac{y_{0}}{1!} + (x - x_{0})^{2} \frac{y_{0}}{2!} + (x - x_{0})\frac{y_{0}y_{0}}{3!} + (x - x_{0})\frac{y_{0}y_{0

$$\begin{aligned} y &= 1 + (x_{-0}) \underbrace{o}_{11} + (x_{-0})^{2} \underbrace{d}_{2} + (x_{-0})^{3} \underbrace{o}_{2} + (x_{-0})^{3} \underbrace{d}_{3} \\ y &= 1 + \frac{x_{12}^{2} + \frac{x_{12}^{2}}{3}}{y_{1}(o, 1)} = 0.9950 \\ y &= 0.23 : 0.9950 \\ y &= 0.23 : 0.9560 \\ y &= 0.23 : 0.9560 \\ y &= 0.23 : 0.9560 \\ y &= 0.056 : y \\ y &=$$

Selnciven dy = x+y, y(0)=1 The Euler's formular is your yothyn' x 0 02 0.4 ý 1 1-2 7:48 y'= x+y 1 1.4 1.88 n=0= $y_1 = y_0 + h y_0' = 1 + (0.2xi) - 1.2.$ N=1=2 48=B1+K41, = 1.240.2×1.4)=1.48 3. Using Euler's method find the solution of the initial value problem (IVP) dy log(xy) y(0)= a at x=0.6 by assuming h=0.2. given y'= log (x+y); y(0)=2. solo. The fuleu's formula is ynti yn thyn' × 0 0.2 0.4 0.6 y 2 2.0602 2.1810 2.2114. y'elog (x+y) 0-3010 0-3541 0-4033 0-4490n=0=) y1=y0+hy0'= 2+(0.2×0.3010)= 2.0602. no1=) 42 = 41+ hy = 2.0602+ (0.2 ×0.3541)= 2.1810. n=2=) y3= y2+hy2 = 2-1810+ (0-2x0.4053)=2.2117. 2. Using Euler's method, find y (H.1) & y (W.0) if 5x dy + y2 = 2 = 0 ; y(4) = 1

80 hr:
4 iven
$$5 \frac{dy}{dx} + y^2 - 2 = 0$$
; $y(4) = 1$
 $\frac{dy}{dx} = -\frac{y^2 + 2}{5x}$.
The tellows formule is $y_{n+1} = y_n + hy_n'$
 $x + 4 + 1 + 4 \cdot 2$
 $y + 1 + 0050 + 00083$
 $y' = \frac{y^2 + 2}{7x} \cos 000483 + 00465 + 0.1(0.0463)$
 $= 1.0060$.
 $n = 1 = 1 \cdot y_2 = y_n + hy_1' = 1.005 + 0.1(0.0463)$
 $= 1.0098 h'$.
5 find $y(0, 2)$ for $y' = y + e^x$, $y(0) = 0$ by
Euler's mithind. Take $h = 0.1$
Bin:
 $q_i ven y' = y_n + e^x$, $y(0) = 0$
 $y_i = 0$, $0.1 = 0.2$
 $y = 0 = 0.1 = 0.2$

$$\begin{aligned} & n=0 = 3 \\ & y_1 = y_0 + hy_0' = 0 + 0 \cdot 1(1) = 0 \cdot 1 \\ & n=1 = 3 \\ & y_2 = y_1 + h \cdot y_1' = 0 \cdot 1 + 0 \cdot 1 \times (1 \cdot 2052) = 0 \cdot 3205 \\ \end{aligned}$$
Fowith code Range - kutta method.
Consider $g(\alpha, q, y, y') = 0$
 $y' = f(\alpha, y)$
 $k_1 = A \cdot f(\alpha, y)$
 $k_2 = A \cdot f(\alpha + y_2 + y' + \frac{1}{2})$
 $k_3 = A \cdot f(\alpha + y_2 + y' + \frac{1}{2})$
 $k_4 = A \cdot f(\alpha + y_4 + y' + \frac{1}{2})$
 $k_5 = A \cdot f(\alpha + y_4 + y' + \frac{1}{2})$
 $k_4 = A \cdot f(\alpha + h_4 + y' + \frac{1}{2})$
 $y = y_0 + 1/6 (x_1 + 2k_3 + 2k_3 + k_4)$
 $y = y_0 + 1/6 (x_1 + 2k_3 + 2k_3 + k_4)$
 f^{10} using Runge - kutta method & order h ;
And y value other $x = 1 \cdot 3in$ atops $0 \cdot 1$
given that $g' = \alpha^2 + y^{\circ}$, $y(1) = 1 \cdot 5$.
Soln:
The Runge - kutta formula i_4
 $k_1 = h \cdot f(\alpha + h_6) + y_1 + \frac{1}{2}$
 $k_5 = h \cdot f(\alpha + h_6) + y_1 + \frac{1}{2}$
 $k_5 = h \cdot f(\alpha + h_6) + y_1 + \frac{1}{2}$

$$k_{\mu} = h \cdot f(x+h, y+k_{3})$$

$$qiven \quad y' = x^{2} + y^{2}$$

$$hese, \quad f(x, y) = x^{2} + y^{2} \quad (k = 0, 1)$$

$$x \quad 1 \quad 1 \cdot 1 \quad 1 \cdot 2$$

$$y \quad 1 \cdot 5 \quad 1 \cdot 8975 \quad g_{1} \cdot 5 \cdot 4 = 0 \cdot 1$$

$$ro \quad find \quad y_{1}$$

$$x = 1 \quad y = 1 \cdot 5 \cdot 5$$

$$k_{1} = h \cdot f(x_{1}, y) = 0 \cdot 1x \quad f(1, 1 + 5) \cdot 5$$

$$= 0 \cdot 1x \quad 3 \cdot 45 = 0 \cdot 325 \cdot 5$$

$$\cdot k_{3} = h \cdot f(x+h_{3}x, y+k_{3}/2) = 0 \cdot 1x \quad f(1 \cdot 05, 1 \cdot 642)$$

$$= 0 \cdot 1x \quad 3 \cdot 866 h = 0 \cdot 3866 \cdot 5$$

$$k_{3} = h \cdot f(x+h_{3}x, y+k_{3}/2) = 0 \cdot 1x \quad f(1 \cdot 05, 1 \cdot 642)$$

$$= 0 \cdot 1x \quad 3 \cdot 866 h = 0 \cdot 3866 \cdot 5$$

$$k_{3} = h \cdot f(x+h_{3}x, y+k_{3}/2) = 0 \cdot 1x \quad f(1 \cdot 05, 1 \cdot 642)$$

$$= 0 \cdot 1x \quad 5 \cdot 666 h = 0 \cdot 39770 \cdot 5$$

$$k_{h} = A \cdot f(x+h_{3}y + k_{3}/2) = 0 \cdot 1x \quad f(1 \cdot 05, 1 \cdot 693)$$

$$= 0 \cdot 1x \quad 5 \cdot 6698 = 0 \cdot 39770 \cdot 5$$

$$k_{h} = A \cdot f(x+h_{3}y + k_{3}/2) = 0 \cdot 1x \quad f(1 \cdot 0, 1 \cdot 2976)$$

$$= 0 \cdot 14809 \cdot 5$$

$$y_{1} = y_{0} + \frac{1}{6} \cdot \left[k_{1} + k_{3} + 2k_{3} + k_{4}\right]$$

$$= 1 \cdot 5 + \frac{1}{6} \begin{bmatrix} 0 \cdot 325 + 9 \cdot 10 \cdot 3866 + 2 \times 0.59717 + 10 \cdot 42897 \end{bmatrix}$$

$$g_{1} = 1.8955$$

$$f(w, y) = x^{2} + y^{2}$$

$$f_{1} = 4n + 4(w_{1}y) = 0.1x + (1+4)(.0955)$$

$$f_{2} = 4n + 4(w_{1}y) = 0.1x + (1+4)(.0955)$$

$$f_{3} = -4n + 5f(x+1y_{2} + y + 1x_{1}y_{2}) = 0.4508$$

$$h_{2} = -4n + 5f(x+1y_{2} + y + 1x_{1}y_{2}) = 0.4508$$

$$h_{3} = -4n + 5f(x+1y_{3} + y + 1x_{1}y_{3}) = 0.4508$$

$$h_{4} = -4n + 5f(x+1y_{3} + y + 1x_{1}y_{3}) = 0.4508$$

$$h_{5} = -4n + 5f(x+1y_{5} + y + 1x_{1}y_{3}) = 0.4508$$

$$h_{5} = -4n + 5f(x+1y_{5} + y + 1x_{1}y_{3}) = 0.4508$$

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$$h_{5} = -4n + 5f(x+1y_{5} + y + 1x_{1}y_{3}) = 0.4508$$

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$$h_{5} = -4n + 5f(x+1y_{5} + y + 1x_{1}y_{3}) = 0.4508$$

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$$h_{5} = -4n + 5f(x+1y_{5} + y + 1x_{1}y_{3}) = 0.4508$$

$$h_{5} = -4n + 5f(x+1y_{5} + y + 1x_{1}y_{3}) = 0.4508$$

$$h_{$$

2. Find
$$y(0.7) \ge y(0.6)$$
 given that $y' = y - x'^{e}$
 $y(0.6) = 1.7879$ by using Rx method rds
 $y(0.6) = 1.7879$ by using Rx method rds
 $y(0.6) = 1.7879$
 $k_{0} = h \cdot f(r_{0} + h)_{2}$ $y + k_{2}/2$
 $k_{0} = h \cdot f(r_{0} + h)_{2}$ $y + k_{2}/2$
 $k_{0} = h \cdot f(r_{0} + h)_{2}$ $y + k_{2}/2$
 $k_{1} = h \cdot f(r_{1} + h)_{2}$ $y + k_{2}/2$
 $k_{1} = h \cdot f(r_{1} + h)_{2}$ $y + k_{2}/2$
Hease $f(x, y) = y - x^{2}$; $h = 0.1$
 $x = 0.6$ 0.4 0.8
 $y = 1.7879$ 1.8763 $x^{2.014}h^{2.01}$
 $r_{1} = 0.6$ $y = 1.7879$.
 $k_{1} = h \cdot f(r_{1} + y) = 0.1x + (0.6, 1.74379)$
 $k_{1} = h \cdot f(r_{1} + y) = 0.1x + (0.6, 1.74379)$
 $k_{2} = 40 \cdot 0.1x + f(r_{2} + h)^{2} t^{1}$
 $r_{1} = 0.1x + f(r_{2} + h)^{2} t^{1}$
 $r_{1} = 0.1x + f(r_{2} + h)^{2} t^{1}$

$$k_{4} = 0.0346 \quad 0.1384$$

$$k_{3} = 0.1 \times 4 \left[0.6 + \frac{0.1}{8} , 1.4849 + 0.1849_{4} \right]$$

$$= 0.1 \times 4 \left[0.655 + 1.8041 \right]$$

$$= 0.1585 + 0.1585 + 0.13844 + 0.18849_{4} + 0.18849_{4} + 0.18849_{4} + 0.18849_{4} + 0.18849_{4} + 0.18855_{4} + 0.1885_{4} + 0.18855_{4} + 0.18855_{4} + 0.18855_{4} + 0.188$$

8. Using R-K method to find
$$y(0,a)$$
,
 $y(0,h)$. Given by $\frac{dy}{dx} = \frac{y^2 - x^2}{y^2 + x^2}$, $y(0) = 1$
Soln:
 $y' = \frac{y^2 - x^2}{y^2 + x^2}$
Here, $f(x_1y_1) = \frac{y^2 - x^2}{y^2 + x^2}$; $h = 0.2$.
 $x = 0 = 0.2$ 0.4
 $y = 1$ (1960
To yind y, :
 $x = 0$; $y = 1$
 $k_1 = -h \cdot f(x_1y_1) = 0.4x + f(0, 1)$
 $= 0.3$
 $k_2 = 0.3x + (0.1, 1.1) = 0.1963$.
 $k_3 = 0.3x + (0.1, 1.1064) = 0.1863$.
 $k_3 = 0.3x + (0.1, 1.1064) = 0.1863$.
 $k_3 = 0.3x + (0.1, 1.1064) = 0.1863$.
 $k_3 = 0.3x + (0.3, 1.1867) = 0.1863$.
 $k_3 = 0.3x + (0.3, 1.1867) = 0.1863$.
 $k_3 = 0.3x + (0.3, 1.1867) = 0.1863$.
 $k_3 = 0.3x + (0.3, 1.1867) = 0.1863$.
 $k_3 = 0.3x + (0.3, 1.1867) = 0.1863$.
 $k_3 = 0.3x + (0.3, 1.1867) = 0.1863$.
 $k_3 = 0.1891$.

To find
$$y_3$$
:
 $x = 0.8$; $y = 1.1960$.
 $k_1 = 40.4x \pm (0.4, 1.1960) = 0.1891$.
 $k_2 = 0.4x \pm (0.4, 1.1960) = 0.198$.
 $k_3 = 0.4x \pm (0.4, 1.18942) = 0.198$.
 $k_4 = 0.4x \pm (0.4, 1.19753) = 0.1683$.
 $y_4 = 1.1960 \pm \frac{1}{6} \frac{1}{6.1891 \pm 2x} 0.1963 \pm 0.1993}{\pm 0.1683}$.
 $y_4 = 1.1960 \pm \frac{1}{6} \frac{1}{6.1891 \pm 2x} 0.1963 \pm 0.1993$.
 ± 0.1683 .

$$\begin{array}{c} y_{1} = y_{0} + y_{0} \left((k_{1} + 3k_{3} + 2k_{3} + k_{4}) \right) \\ & \cdot 0 + y_{0} \left(0 \cdot 0 + 2 \times 0 \cdot 0 + 9 + 4 \times 0 \cdot 0 + 85 + 0 \cdot 0 + 65 \right) \\ & \cdot 0 + 8 + 1 \\ & \cdot 0 \cdot 5 + y_{0} \left(-0 \cdot 15 - 4 \times 0 \cdot 125 - 4 \times 0 \cdot 1269 \right) \\ & -0 \cdot 1065 \right) \\ & \cdot 0 \cdot 3746 \\ \end{array}$$

$$\begin{array}{c} \chi_{1} = 0 \cdot 5 + y_{0} \left(-0 \cdot 15 - 4 \times 0 \cdot 125 - 4 \times 0 \cdot 1269 \right) \\ & -0 \cdot 1065 \right) \\ & \cdot 0 \cdot 3746 \\ \end{array}$$

$$\begin{array}{c} \chi_{1} = 0 \cdot 5 + y_{0} \left(-0 \cdot 15 - 4 \times 0 \cdot 125 - 4 \times 0 \cdot 1269 \right) \\ & -0 \cdot 1065 \right) \\ & \cdot 0 \cdot 5 + y_{0} \left(-0 \cdot 15 - 4 \times 0 \cdot 125 - 4 \times 0 \cdot 1269 \right) \\ & -0 \cdot 1065 \right) \\ & \cdot 0 \cdot 5 + y_{0} \left(-0 \cdot 15 - 4 \times 0 \cdot 125 - 4 \times 0 \cdot 1269 \right) \\ & \cdot 0 \cdot 5 + y_{0} \left(-0 \cdot 15 - 4 \times 0 \cdot 125 - 4 \times 0 \cdot 1269 \right) \\ & \cdot 0 \cdot 0 \cdot 5 + y_{0} \left(-0 \cdot 15 - 4 \times 0 \cdot 125 - 4 \times 0 \cdot 1269 \right) \\ & \cdot 0 \cdot 0 \cdot 5 + y_{0} \left(-0 \cdot 15 - 4 \times 0 \cdot 125 - 4 \times 0 \cdot 125 - 4 \times 0 \cdot 1269 \right) \\ & \cdot 0 \cdot 0 \cdot 5 + y_{0} \left(-0 \cdot 15 - 4 \times 0 \cdot 125 - 4 \times 0 \cdot 12$$

$$\begin{aligned} x' = -xxz-y'. \\ x = 0 = 0.1 \\ y = 1 = 0.09950 \\ \hline Z_{\Xi}y' = 0 = -0.0995. \\ ch_{\Xi} = 0.1 \\ \hline \frac{f(x_1y_1x) = x}{h_1 \equiv 0.1} \\ \hline \frac{f(x_1y_1x) = -xx - y}{h_1 \equiv 0.1} \\ \hline \frac{f(x_1y_1x) = -xx - y}{h_1 \equiv 0.1} \\ \hline \frac{f(x_1y_1x) = -xx - y}{h_1 \equiv 0.1} \\ \hline \frac{f(x_1y_1x) = -xx - y}{h_1 \equiv 0.1} \\ \hline \frac{f(x_1y_1x) = -xx - y}{h_1 \equiv 0.1} \\ \hline \frac{f(x_1y_1x) = -xx - y}{h_1 \equiv 0.1} \\ \hline \frac{f(x_1y_1x) = -xx - y}{h_1 \equiv 0.1} \\ \hline \frac{f(x_1y_1x) = -xx - y}{h_1 \equiv 0.1} \\ \hline \frac{f(x_1y_1x) = -xx - y}{h_1 \equiv 0.1} \\ \hline \frac{f(x_1y_1x) = -xx - y}{h_1 \equiv 0.1} \\ \hline \frac{f(x_1y_1x) = -xx - y}{h_1 \equiv 0.1} \\ \hline \frac{f(x_1y_1x) = x}{h_1 \equiv 0.1} \\ \hline \frac{f$$

$$y_{1} = y_{0} + \frac{1}{6} \left(k_{1} + 2k_{2} + 2k_{3} + k_{4} \right)$$

$$= 1 + \frac{1}{4} \left(0 - \frac{1}{6} \times 0.005 - \frac{1}{6} \times 0.0091}{0.0091} - \frac{1}{6} \times 0.0991} \right)$$

$$= 0.99450 \text{ M}.$$

$$2_{1} = 0 + \frac{1}{4} \left(-0.1 - \frac{1}{6} \times 0.0094 + \frac{1}{6} \times 0.0991}{0.0040} \right)$$

$$= -0.0995 \text{ M}.$$

$$(\text{ensider fix and order initial value})$$

$$y_{1}^{0} = -0.6 \text{ using } \text{ R ath order } \text{ R.k. matricel}$$

$$y_{1}^{0}(0) = -0.6 \text{ using } \text{ R ath order } \text{ R.k. matricel}$$

$$y_{1}^{0}(0) = -0.6 \text{ using } \text{ R ath order } \text{ R.k. matricel}$$

$$y_{1}^{0}(0) = -0.6 \text{ using } \text{ R ath order } \text{ R.k. matricel}$$

$$y_{1}^{0}(0) = -0.6 \text{ using } \text{ R ath order } \text{ R.k. matricel}$$

$$y_{1}^{0}(0) = -0.6 \text{ using } \text{ R ath order } \text{ R.k. matricel}$$

$$y_{1}^{1}(0) = -\frac{1}{6} \times \frac{1}{9} + \frac{1}{6} \times \frac{1}{9} \text{ sinx}$$

$$y_{1}^{1} = \frac{1}{6} \times \frac{1}{9} \text{ sinx}$$

$$y_{1}^{1} = \frac{1}{6} \times \frac{1}{9} \text{ sinx}$$

$$y_{1}^{1} = \frac{1}{6} \times \frac{1}{9} \text{ sinx} - \frac{1}{6} + \frac{1}{9} \times \frac{1}{6}$$

$$y_{1}^{1}(0) = -\frac{1}{6} \times \frac{1}{9} \text{ sinx} - \frac{1}{6} + \frac{1}{9} \times \frac{1}{6} \times \frac{1}{9} \text{ sinx}$$

$$y_{1} = y_{0} + \frac{1}{6} \left(k_{1} + 2k_{2} + \frac{1}{6}k_{3} + \frac{1}{$$

Shi. The Nulleve's productor connector
formula is ,
P:
$$4_{n+1} = 4_{n-3} + \frac{h}{3} \int e^{4} y_{n-2}^{\prime} - y_{n-1}^{\prime} + e^{4} y_{n}^{\prime} \int - 0$$

 $c: 4_{n+1} = 4_{n-3} + \frac{h}{3} \int e^{4} y_{n-2}^{\prime} - y_{n-1}^{\prime} + e^{4} y_{n}^{\prime} \int -0$
 $\frac{2}{3} \frac{0}{2n} \frac{0}{2n} \frac{0}{2n} \frac{1}{2n} \frac{0}{2n} \frac{1}{2n} + \frac{1}{2n} \frac{1}{2$

$$y = \frac{2}{2} + \frac{2}{2} +$$

$$dn:$$

$$(x,y) = x(y+y^{2})$$

$$($$

Milks & formula is,
p:
$$y_{n+1} = y_{n-3} + \frac{h}{3} \int y_{n-2} - y_{n-1} + 2y_n^{T} \int (1 + y_{n+1} - y_{n-1} + \frac{h}{3} \int y_{n-1} + \frac{h}{3} y_{n-1} + \frac{h}{3$$

4 Given that
$$y'' + xy' + y = 0$$
, $y(b) = 1$; $y'(b) = 0$
suites method and Aind the soin to suites method.
50(0-7) by suither's method.
51n:
The souldon sames is:
 $y = y_0 + (x - x_0) \frac{y_0}{y_1!} + (x - x_0)^2 \frac{y_0''}{y_1!} + (x - x_0)^3 \frac{y_1''}{y_1!}$
 $y'' = -xy'' - y$.
 $y'' = -xy'' - y$.
 $y'' = -xy'' - y'' -$

 $y = 1 - \frac{x^{2}}{2} + \frac{x^{4}}{8}$ $y' = -\frac{x^{4}}{2} + \frac{x^{2}}{8} = 3y' = -x + \frac{x^{5}}{2}$ y(0.1) = 0.9950y(0.2) = 0.980 2 y(0.3) = 0.9560 1 100 miger 11 The Neilne's formula in, P: yn+1 = yn-3 + 4h [2yn-2 - yn-1 +2 yn.] c: $y_{n+1} = y_{n-1} + \frac{h}{3} \left[y_{n-1} + h y_n' + y_{n+1} \right]$ sols/m-×7 0.4 x. v. 0.1 0.2 10.3 0 x 0.9980 0.9802 0.9560 0.9232 0.9252 101 y -0.0995 -0.1960 -0.2865. -0.366 -0.56 0 y'======= put n= s; p: $y_{4} = y_{0} + \frac{hx_{0}}{3} \left[ay_{1}' - y_{2}' + ay_{3}' \right]$ = 1+ 0.4 [ax(-0.0995)+0.1960+ax(-0.2 0-9282. 4 put n= 3; c: y= y2 + 1/3 [y2 + 443 + 44]

$$= 0.9803 + \frac{0.1}{3} \left[-0.1960 - hx - 2865 + \frac{0.3880}{4.9832} \right]$$

Adam's Dashforth Predictor Corrector Formula:

$$P: Y_{n+1} = Y_n + \frac{h}{24} \left[5\pi y_n - 59 y_{n-1} + 37 y_{n-2} - 9 y_{n-3}^{*} \right]$$

a: $y_{n+1} = y_n + \frac{h}{24} \left[19 y_n - 5 y_{n-1} + y_{n-2} + 9 y_{n+3} - 1 \right]$
b) $y_n = \frac{1}{2} \left[19 y_n - 5 y_{n-1} + y_{n-2} + 9 y_{n+3} - 1 \right]$
b) $y_n = \frac{1}{2} \left[2(1+y) - y_n + y_n + 9 y_{n+3} - 1 \right]$
 $y_{(1+2)} = 1.5 \pi 8 \times y_n (1+3) = 1.919$
 $y_{(1+2)} = 1.5 \pi 8 \times y_n (1+3) = 1.919$
 $y_{(1+2)} = 1.5 \pi 8 \times y_n (1+3) = 1.919$
 $y_{(1+2)} = 1.5 \pi 8 \times y_n (1+3) = 1.919$
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 $y_{(1+2)} = 1.919$
 $y_{(1+2$

$$x = 0 \qquad 0.45 \qquad 1.1 \qquad 1.5 \qquad x = 2$$

$$y = \frac{3}{2} \qquad \frac{3}{2} \qquad \frac{3}{2} \qquad \frac{5}{2} \qquad \frac{5}{$$

$$c: y_{n+1} = y_n + \frac{1}{2n} \left[1ay_n' - sy_{n-1} + y_{n-2} + ay_n + \frac{1}{2n} + ay_n + ay_n + \frac{1}{2n} + ay_n + \frac{1}{2n} + ay_n + ay_n + \frac{1}{2n} + ay_n + ay_n + \frac{1}{2n} + ay_n + ay_n + ay_n + \frac{1}{2n} + ay_n + ay_n + ay_n + ay_n + \frac{1}{2n} + ay_n + ay_n$$

unit-IV

Numerical differentiation and Integration

Questions Formula can be used for interpolating the value of $f(x)$ near the end of the tabular values.	opt1 Newton's forward	opt2 Newton's backward	opt3 Lagrange	opt4 stirling	opt5	opt6	Answer Newton's backward
Formula can be used for interpolating the value of $f(x)$ near the beginning of the tabular values.	Newton's forward	Newton's backward	Lagrange	stirling			Newton's forward
In Numerical integration, the length of all intervals is in distances.	Greater than the other	less than the other	equal	not equal			equal
When the function is given in the form of table values instead of giving analytical expression we use	numerical differentiatio n	numerical elimination	approximation	addition			numerical differentiation
is the process of computing the value of the definite integral from the set of numerical values of the integrand.	numerical differentiatio n	numerical integration	Simpsons rule	Trapezoidal rule			numerical integration
Numerical integration is the process of computing the value of a from a set of numerical values of the integrand.	indefinite integral	definite integral	expression	equation			definite integral
Numerical evaluation of a definite integral is called	integration	differentiation	interpolation	triangularisat on	i		integration
What is the value of h if a=0,b=2 and n=2.	1	2	3	4			1
Integral $(f(x) dx)=(h/2)$ [Sum of the first and last ordinates + 2(sum of the remaining ordinates)] is called	Constant rule	Simpsons rule	Trapezoidal rule	Rombergs rule			Trapezoidal rule
If the given integral is approximated by the sum of 'n' trapezoids, then the rule is called as	Newton's method	Trapezoidal rule	simpson's rule	none			Trapezoidal rule
What is the formula for finding the length interval h in trapezoidal tule?	h=(b-a)/n	h=(b/a)/n	h=(b*a)/n	h=(b+a)/n			h=(b-a)/n

The accuracy of the result using the Trapezoidal rule can be improved by	Increasing the interval h	Decreasing the length of the interval h	Increasing the number of	altering the given function	Decreasing the length of the interval h
The order of error in Trapezoidal rule is	h	h^2	h^3	h^4	h^2
Simpson's rule is exact for a even though it was derived for a Quadratic.	cubic	less than cubic	linear	quadratic	linear
The order of error in Simpson's rule is	h	h^2	h^3	h^4	h^4
For what type of functions, Simpsons rule and direct integration will give the same result?	parabola	hyperbola	ellipse	cardiod	parabola
Simpson's rule gives exact result if the entire curve $y=f(x)$ itself is a	parabola	hyperbola	ellipse	cardiod	parabola
To apply Simpsons one third rule the number of intervals must be	odd	even	equally spaced	unequal	even
The end point coordinates y_0 and y_n are included in the Simpsons 1/3 rule, so it is called formula.	Newton's	open	closed	Gauss	closed
Simpson's one-third rule on numerical integration is called a formula.	closed	open	semi closed	semi opened	closed
The order of error in Simpson's formula is	1	2	3	4	4
In two point Gaussian quadrature Formula n =	1	2	3	4	2
In Simpsons 1/3 rd rule, the number of ordinates must be	odd	even	0	3	odd
In three point Gaussian quadrature Formula n =	1	2	3	4	3
Two point Gaussian quadrature Formula requires only functional evaluations and gives a good estimate of the value of the integral.	1	2	3	4	2
formula is based on the concept that the accuracy of numerical integration can be improved by choosing the sampling wisely, rather than on the basis	Newtons	elimination	Gauss quadrature	hermite	Gauss quadrature

Gauss Quadrature formula is also called as	Newton's	Gauss-Legendre	Gauss-seidal	Gauss-Jordan	Gauss-Legendre
The 2 point Gauss-quadrature is exact for the polynomial up to degree	1	2	3	4	3
The 3 point Gauss-quadrature is exact for the polynomial up to degree	1	5	3	4	5
Integrating $f(x)=5x^4$ in the interval [-1,1] using Gaussion two point formula gives	1/2	9/5	10/9	5/9	10/9
The modified Eulers method is based on the of points	sum	multiplication	average	subratction	average
prior values are required to predict the next value in Milne's method	1	2	3	4	4
prior values are required to predict the next value in Adams method	1	2	3	4	3
The Eulers method is used only when the slope at point in computing is y(n+1)	z (x(n), y)	(x, y(n))	(x(n), y(n))	(0, 0)	(x(n), y(n))
The Runge Kutta method agrees with Taylor series solution upto the terms	h^2	h^3	h^4	h^r	h^r
Runge Kutta method agree with solution upto the terms h^4	Taylor Series	Eulers	Milnes	Adams	Taylor Series
method is better than Taylor's series	Runge Kutta	Milnes	Adams	Eulers	Runge Kutta
Taylors series method belongs to method	Single step	multi step	step by step	limination	Single step
If all the n conditions are specified at the initial point	Initial value	final value	boundary value	e semi defined	Initial value
only then it is called a problem The problem $dy/dx = f(x,y)$ with the initial condition y(x(0)) = y(0) is problem	initial value	final value	boundary value	e multistep	initial value

The solution of an ODE means finding an explicit expression for y, in terms of a number of	finite	infinite	positive	negative	finite
The solution of an ODE is known as solution	infinite	open-form	closed-form	negative form	closed-form
The differential equation of the 2 nd order can be solved by reducing it to a differential equation	lower order	higher-order	partial	simultaneous	lower order
The Eulers method is used only when the slope at point $(x(n), y(n))$ in computing is	y(n+1)	y(n-1)	(dy/dx)(n+1)	(dy/dx)(n-1)	y(n+1)
The Eulers method is used only when the slope at point in computing is y(n+1)	(x(n),y)	(x, y(n))	(x(n), y(n))	(0, 0)	(x(n), y(n))
The modified Eulers method is a method of predictor-corrector type	Self- correcting	Self-starting	Self-evaluating	Self-predicting	Self-starting
The modified Eulers method has greater accuracy than method	Taylor's	Picard's	Euler's	Adam's	Taylor's
The formula $y(n+1) = y(n) + hf(x(n), y(n))$ is formula	Euler's	modified Euler's	Picard's	Taylor's	Euler's
Modified Eulers method is the Runge-kutta method of order	1 st	2^{nd}	3 rd	4 th	2^{nd}
Modified Eulers method is same as the method of 2 nd order	Eulers	Taylors	Picards	Runge Kutta	Runge Kutta
The process used in Eulers method is very slow and to obtain reasonable accuracy we need to take a value of h	Smaller	Larger	negative	Positive	Smaller
The process used in Eulers method is very slow and to obtain reasonable accuracy we need to take a smaller value of	h	h^2	h^3	h^4	h
The formula is given by $y(i+1) = y(i) + hf$ (x(i), y(i))	Taylors	predictor	Corrector	Eulers	Eulers
The predictor formula and formula are one and the same	Taylors	Eulers	Modified Eulers	Eulers	Eulers
The formula is given by $y(i+1) = y(i) + h/2[f(x(i), y(i)) + f(x(i+1), y(i+1))], i = 1,2,3$	Taylors	predictor	Corrector	Picards	Corrector
The formula is used to predict the value $y(i+1)$ of y at x(i+1)	Predictor	Corrector	Corrector	Picards	Predictor

The formula is used to improve the value of	Predictor	Corrector	Taylors	Picards	Corrector
y(i+1)					
In predictor corrector methods, prior values of y	1	2	3	4	4
are needed to evaluate the value of y at $x(i+1)$					
In methods, 4 prior values of y are needed to	Taylor's	predictor	Predictor-	Euler's	Predictor-corrector
evaluate the value of y at $x(i+1)$			corrector		
In predictor corrector methods 4 prior values of	у	y^2	y^3	y^4	у
are needed to evaluate of values of are					

needed to evaluate of value of y at x(i+1)

UNIT-V
BOUNDARY UNLUE PROBLEM IN ORDINARY
AND PARTIAL DIFFERENTIAL EQUATION.
Functe difference Method:
Applace x by
$$x_k$$

y by $y_{k+1} - y_k + y_{k+1}$
y' by $y_{k+1} - y_k + y_{k+1}$
where, $h = \frac{b-a}{h}$
1. Selve $y'' = x_{k+1}y$ with the boundary
conduction $y(e) = y(1) = 0$.
Seth:
 $x = 0 = 0.45$ 0.5 0.7 n
 $y = 0 = -0.034q$ -0.0564 -0.05 0
 $h = \frac{b-a}{h} = \frac{1-0}{h} = 0.45$.
 $y'' = x_{k}y$.
 $y'' = x_{k}y$.

$$y_{k+1} - ay_{k} + y_{k+1} = h^{2}y_{k} + h^{2}y_{k}$$

$$y_{k+1} - ay_{k} + y_{k+1} = h^{2}y_{k} = h^{2}x_{k}$$

$$y_{k+1} - y_{k}(-a-h^{2}) + y_{k+1} = h^{2}y_{k}$$

$$y_{k+1} + y_{k}(-a-h^{2}) + y_{k+1} = 0.062\pi n$$

$$y_{k-1} - a.062\pi y_{k} + y_{k} = 0.066\pi x,$$

$$y_{2} - a.062\pi y_{2} + y_{3} = 0.066\pi x,$$

$$y_{3} - a.062\pi y_{2} + y_{3} = 0.062\pi x,$$

$$y_{3} - a.062\pi y_{4} + y_{5} = 0.062\pi x,$$

$$y_{3} - a.062\pi y_{4} + y_{5} = 0.062\pi x,$$

$$y_{3} - a.062\pi y_{4} + y_{5} = 0.062\pi x,$$

$$y_{3} - a.062\pi y_{4} + y_{5} = 0.062\pi x,$$

$$y_{3} - a.062\pi y_{4} + y_{5} = 0.062\pi x,$$

$$y_{3} - a.062\pi y_{4} + y_{5} = 0.062\pi x,$$

$$y_{3} - a.062\pi y_{3} + y_{5} = 0.062\pi x,$$

$$y_{3} - a.062\pi y_{3} + y_{5} = 0.062\pi x,$$

$$y_{3} - a.062\pi y_{3} + y_{5} = 0.062\pi x,$$

$$y_{3} - a.062\pi y_{3} + y_{5} = 0.062\pi x,$$

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$$y_{3} - a.062\pi y_{3} + y_{5} = 0.062\pi x,$$

$$y_{3} - a.062\pi y_{3} + y_{5} = 0.062\pi x,$$

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$$y_{3} - a.062\pi y_{3} + y_{5} = 0.062\pi x,$$

$$y_{3} - a.062\pi y_{3} + y_{5} = 0.062\pi x,$$

$$y_{3} - a.062\pi y_{3} + y_{5} = 0.062\pi x,$$

$$y_{3} - a.062\pi y_{3} = 0.064\pi y,$$

$$y_{3} = -0.054\pi y,$$

$$y_{3} = -0.$$

2. Using a finite difference mutical compute
y(cons). Given
$$y'' = 6hy + (0 = 0, y(0) = y(1) = 0$$
.
We dividing the interval inter(y) to equal parts.
i) a equal parts.
soln:
yiven $y'' = 6hy + 10 = 0$
 $y'_{K-1} = ay'_{K} + y'_{K-1} = 6hy'_{K} + 0 = 0$.
 $y'_{K-1} = ay'_{K} + y'_{K-1} = 6hy'_{K} + 0 = 0$.
 $y'_{K-1} = ay'_{K} + y'_{K-1} = 6hy'_{K} + 0 = 0$.
 $y'_{K-1} = ay'_{K} + y'_{K-1} = 6hy'_{K} + 0 = 0$.
 $y'_{K-1} = ay'_{K} + y'_{K-1} = 6hy'_{K} + 0 = 0$.
 $y'_{K-1} = ay'_{K} + y'_{K-1} = 6hy'_{K} + 0 = 0$.
 $y'_{K-1} + y'_{K} (-3 - 6hy'_{K})^{0} + y'_{K-1} = -10h^{0}$
() subdiving into honors.
 $h = \frac{b - a}{h} = \frac{1 - 0}{h} = 0.62h$
 $y''_{K} = 0$ or $ab = 0.62h$ or a'_{K}
 $y''_{K} = 0$ or $ab = 0.62h$ or a'_{K}
y''_{K} = 0 or $ab = -0.62h$ or a'_{K}

Put
$$k = 3$$
,
 $y_1 = 4y_2 + y_3 = -0.625$, $--0$
Put $k = 3$;
 $y_2 = 6y_3 + 4y_4 = -0.625$.
 $y_2 = 6y_3 + 4y_4 = -0.625$.
 $y_2 = 6y_3 + 4y_4 = -0.625$.
 $y_2 = 6y_3 + 6y_4 = 0.625$.
 $y_1 = 0.1887$; $y_2 = 0.1471$, $y_3 = 0.1207$.
1) Sub dividing de 8 pauls.
 $f = \frac{b-a}{a} = \frac{1-0}{3} = 0.5$.
 $x = 0$, 0.1853 . 0 .
 $f = b + 5$. Eqn O bacemes.
 $y_{2-1} = y_{3-1} + y_{3-2}$.
 $f = 1 + \frac{y_{3-1}}{2} + \frac{y_{3-1}}{2}$.
 $f = 1 + \frac{y_{3-1}}{2} + \frac{y_{3-1}}{2} = -4.5$.
 $y_{3-1} = 18y_3 + 4y_5 = -4.5$.
 $y_{1-2,0.1589}$.

solve by finite difference multiply, the ENP

$$y'' - y = 0$$
 where $y(0) = 0; y(1) = 1$; take
 $4x = 0.45$
 $y_{k-1} - 2 y_k + y_{k+1} - y_k = 0$
 $\frac{y_{k-1} - 2 y_k + y_{k+1} - y_k h^2}{h^2} = 0.$
 $y_{k-1} - 4y_k + y_{k+1} - y_k h^2$
 $y_{k-1} - 4y_k + y_{k+1} - y_k h^2$
 $y_{k-1} + y_k (-2 - h^2) + y_{k+1} = 0.$
 $y_{k-1} + y_k (-2 - h^2) + y_{k+1} = 0.$
 $y_{k-1} + y_k (-2 - h^2) + y_{k+1} = 0.$
 $y_{k-1} + y_k (-2 - h^2) + y_{k+1} = 0.$
 $y_{k-1} + y_k (-2 - h^2) + y_{k+1} = 0.$
 $y_{k-1} + y_k (-2 - h^2) + y_{k+1} = 0.$
 $y_{k-1} + y_k (-2 - h^2) + y_{k+1} = 0.$
 $y_{k-1} + y_k (-2 - h^2) + y_{k+1} = 0.$
 $y_{k-1} + y_k (-2 - h^2) + y_{k-1} = 0.$
 $y_{k-1} + y_k (-2 - h^2) + y_{k+1} = 0.$
 $y_{k-1} + y_{k-1} + y_{k-1} = 0.$
 $y_{k-1} + y_{k-1} + y_{k-2} = 0.$
 $y_{k-1} - 2.0625y_{k-1} + y_{k-2} = 0.$

$$I = S;$$

$$I_{2} = 9 \cdot 062 + I_{3} + I_{4} = 0;$$

$$I_{3} = 9 \cdot 0645 + I_{3} + I = 0;$$

$$I_{3} = 9 \cdot 0645 + I_{3} = -1 - -(S);$$
Solve by (B, B, AS)

$$I_{1} = 5 \cdot 8151 + I_{3} = 0.14154 + I_{3} + I_{3} = 0.7600$$
Antistration & pothal differential Equation
consider:

$$I_{3} = \frac{1}{2} \frac{1}$$

BI-HACSO-AXIXO. CANON DALE NOV D OF 1 . 02 The one dumensional heat egn is parabolic There are two methods to solve one dimensional head equations i) pender-schmidt formula (Exepticite) i) Crank - Mcolsion method (Implicit) Bender-schmidt formula: (i,1+i,) (i,i) (i,i) 0(2,41) uzisti = uzis + Uzis Mars in the second seco Hove, k-ah² solve Us = Usex in orn in, the given that 1. u(o,t)=0, $u(x_1,t)=0$, $u(x_1,o)=x^2(ax-x^2)$ Compute u. upto see. with Ax : 1 by Using Bendes Schmidt formula.

St-hat = 0- Arts 0 goln: cliven uterna 2 a=1 0 while a mile and longer in mounts $b = \frac{ah^2}{a} = \frac{1\pi}{a} = 0.5$ $U_{i}, j + i = \frac{bi - bi \dot{s}}{a} + \frac{bi + i \dot{s}}{a}$ $u_{i}, j + i = \frac{bi - bi \dot{s}}{a} + \frac{bi + i \dot{s}}{a}$ X 0 1 2 3 4 3 4 5 24 84 14A 14A 0 0 0 0.5 0 ha 84 114 72 0 1 0 42 78 78 57 0 हन् ० 67.5 89 0. 60 1.5 0 39 53.25 Ag.5 33.75 O 2.5 0 26.625 39.75 43.5 24.95 0 3 0 19.875 35.0625 32.25 2).75 0 adve Us - Ver to orx in the given mat 2. solve un = saut 1 h-0.25 for t >0, 01x211 with u(011)=0 u(x10)=0; ucert) E columnos internas present

soln:

$$u_{0xx} = 52.44$$
 a.s.s.
 $h= 0.45$.
 $k = \frac{ah^2}{a} = \frac{32.00.25}{a} = 1$
 $u_{i,j+1} = \frac{u_{2.1,i,j} + u_{2.41,i}}{a}$
 $\frac{x}{a} = \frac{0.0.35}{0.000} = 0.5$ 0.715 1
 $0 = 0 = 0.0$ 0 0 1
 $1 = 0 = 0.0$ 0 0 1
 $1 = 0 = 0.0$ 0 0 1
 $a = 0 = 0.0$ 0 0 1
 $a = 0 = 0.0$ 0 0 1
 $a = 0 = 0.0$ 0 0 5
 $a = 0 = 0.0$ 0 0.5 3
 $a = 0 = 0.0$ 0 0.5 3
 $b = 0.025$ 0.575 $b.85$ 5.
 $b = 5.0$ 0.875 $b.85$ 5.
 $b = 5.0$ 0.976 $c.875$ $b.85$ 5.
 $c = 0.875$ $c.875$ $c.875$ $b.85$ 5.
 $c = 0.875$ $c.875$ $b.85$ 5.
 $c = 0.875$ $c.875$ $c.875$

solut:
Solut: Crank - Nicolson's Method (Implicit method):
Consider
$$\frac{\partial u}{\partial x^2} = a \frac{\partial u}{\partial t}$$
 (one dimensional
head 49n).
 $\mathbf{x} = ah^2$
 $a + \frac{a}{b_{1,1}} = \frac{a}{b_{1,1}} = \frac{a}{b_{1,1}} + \frac{a}{b_{1,1}} = \frac{a}{b_{1,1}} + \frac{a}{b_{1,2}} + \frac{a}{$

$$\begin{aligned} \frac{4j_{x}}{2} & 0 & 0.4s & 0.5 & 0.4h \\ 0 & 0 & 0 & 0 & 0 & 0 \\ 1 & 0 & u & u_{x} & u_{x} & u_{x} \\ hu_{x} = u_{x} \\ hu_{x} = u_{x} \\ hu_{x} = u_{x} \\ u_{x} - hu_{x} = 0 \\ u_{x} = u_{x} + u_{y} \\ u_{y} = u_{x} + 00 \\ u_{x} + hu_{y} = 00 \\ u_{x} = 1.70644 \\ u_{y} = u_{x} + 00 \\ u_{y} = 1.71644 \\ u_{y} = u_{x} + 0.544 \\ u_{y} = u_{y} + 0.544 \\ u_{y} = u_{x} + 0.544 \\ u_{y} = u_{y} + 0.544 \\ u_{y} = u_{x} + 0.544 \\ u_{y} = u_{y} + 0.544 \\ u_{y} = u_{x} + 0.544 \\ u_{y} = u_{y} + 0.5$$

80 80 1

$$\frac{\partial^{2} u}{\partial x^{2}} = \frac{\partial u}{\partial t}$$

$$\frac{\partial^{2} u}{\partial x^{2}} = \frac{\partial u}{\partial t}$$

$$\frac{\partial u}$$

Sub () in ()

$$u_{2} - 4u_{3} + u_{4} = -1.5389.$$

 $u_{2} - 4u_{3} + \frac{u_{3}}{4} + 0.2578 = -1.57887.$
 $u_{2} - 4u_{3} + \frac{u_{3}}{4} + 0.2578 = -1.57887.$
 $u_{2} - 1.575u_{3} = -1.47469.$
 $u_{2} - 3.775u_{3} = -1.47469.$
 $u_{2} - 3.775u_{3} = -1.47469.$
Solve eq. (), (), (), ().
Solve eq. (), (), (), ().
 $u_{1} = 0.5993.$
 $u_{3} = 0.56461.$
 $u_{4} = 0.5993.$
Solve by crane nicoloon's method,
eq. Use u_{4} Subjected & u(u_{10})=0;
 $u(0, e) = 0; u(1, e) = e dor two time
 $Stop.$$

$$\begin{aligned} & \chi_{n} : \\ & u_{nx} = u_{k} : \\ & a_{\pm 1} \\ & h : \frac{b - a}{n} = \frac{1 + 0}{h} = 0 \cdot d^{25} : \\ & k : a h^{2} = 1 x 0 \cdot a s^{2} = 0 \cdot 0 6 2 5 : \\ & k : a h^{2} = 1 x 0 \cdot a s^{2} = 0 \cdot 0 6 2 5 : \\ & \frac{1}{2} \frac{\sqrt{3}}{2} = 0 = 0 \cdot \frac{1}{2} \frac{\sqrt{3}}{2} = 0 \cdot 0 6 2 5 : \\ & \frac{1}{2} \frac{\sqrt{3}}{2} = 0 = 0 \cdot \frac{1}{2} \frac{\sqrt{3}}{2} = 0 \cdot$$

$$hu_{5} = u_{4}+u_{5} + 0.0198.$$

$$hu_{5} = u_{5} + u_{5} + u_{5} + 4u_{5} + u_{5} = 0.0198 - 0.0198 - 0.0198 - 0.0198 - 0.0198 - 0.0191 + 4u_{5} = 0.0191 + 4u_{5} = 0.0191 + 4u_{5} = 0.00191 + 4u_{5} = 0.00088$$

$$u_{5} = 0.00059 + u_{5} = 0.0191 + 4u_{5} = 0.00191 + 4u_{5} = 0.00088$$

$$u_{5} = 0.00059 + u_{5} = 0.0191 + 4u_{5} = 0.00188$$

$$u_{5} = 0.00059 + u_{5} = 0.0191 + 4u_{5} = 0.00088$$

$$u_{5} = 0.00059 + u_{5} = 0.0191 + 4u_{5} = 0.00188$$

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The formula is,

$$U_{0} = U_{0} + U_{0} - U_{0}$$
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$$U_{0} = U_{0} + U_{0} - U_{0}$$

$$U_{0} = U_{0} + U_{0} + U_{0} + U_{0}$$

$$U_{0}(x_{1}, 0) = 0; \quad \partial U_{0}(x_{1}, 0) = 0; \quad U(0, 1, 0) = 0;$$

$$u(x_{1}, 0) = 100 \text{ sin}(x_{1}) \cdot \text{ compute } U(x_{1}, 0) = 0;$$

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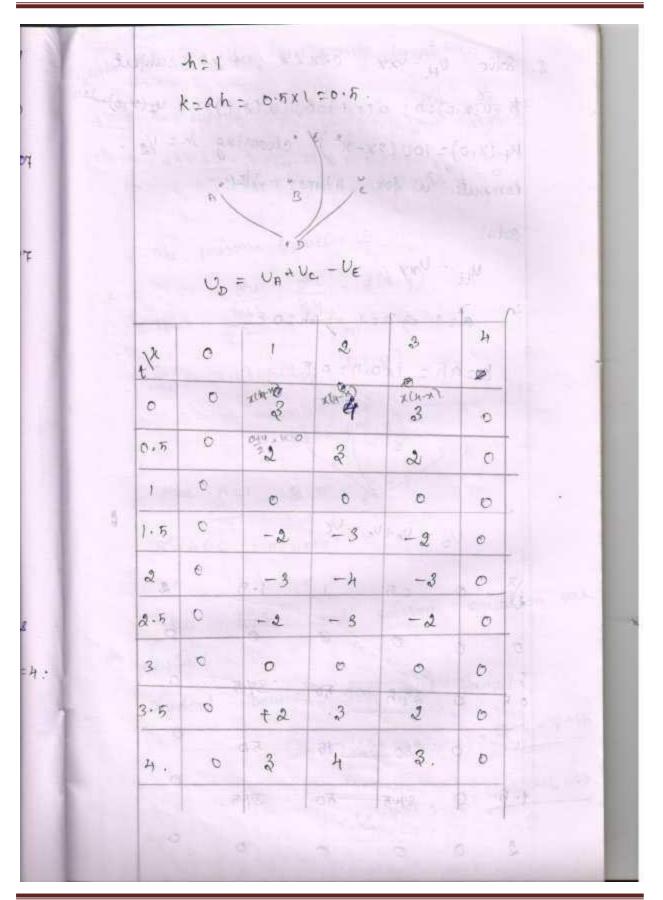
$$u(x_{1}, 0) = 100 \text{ sin}(x_{1}) \cdot \text{ compute } U(x_{1}, 0) = 0;$$

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$$u(x_{1}, 0) = 100 \text{ sin}(x_{1}) \cdot \text{ compute } U(x_{1}, 0) = 0;$$

$$get n;$$

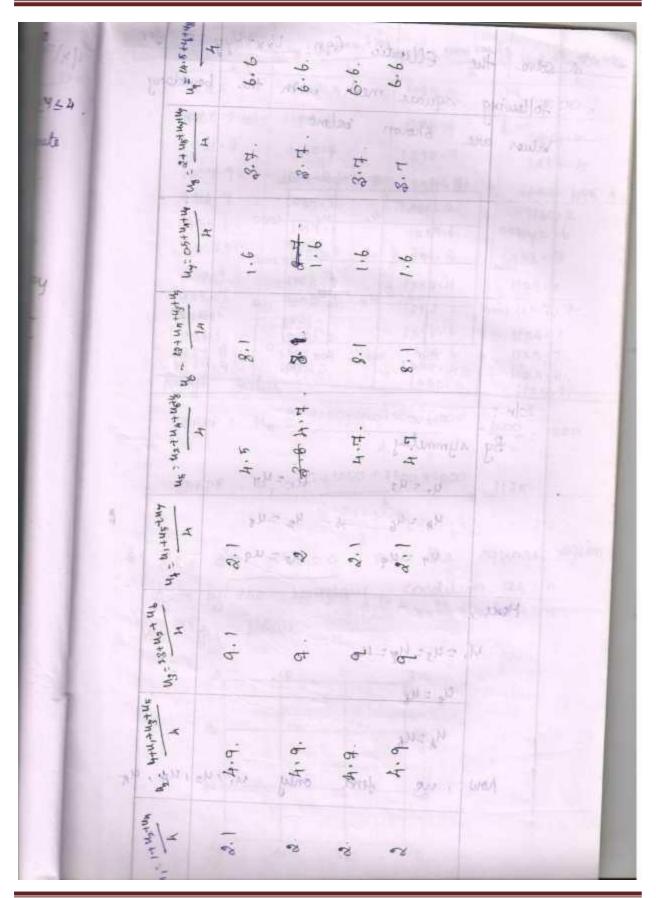
$$\frac{\partial U_{0}}{\partial t^{2}} = \frac{\partial^{2} U_{0}}{\partial x^{2}} - \frac{\partial^{2} U_{0}}{\partial t^{2}} - \frac{\partial^{2} U_{0}}$$



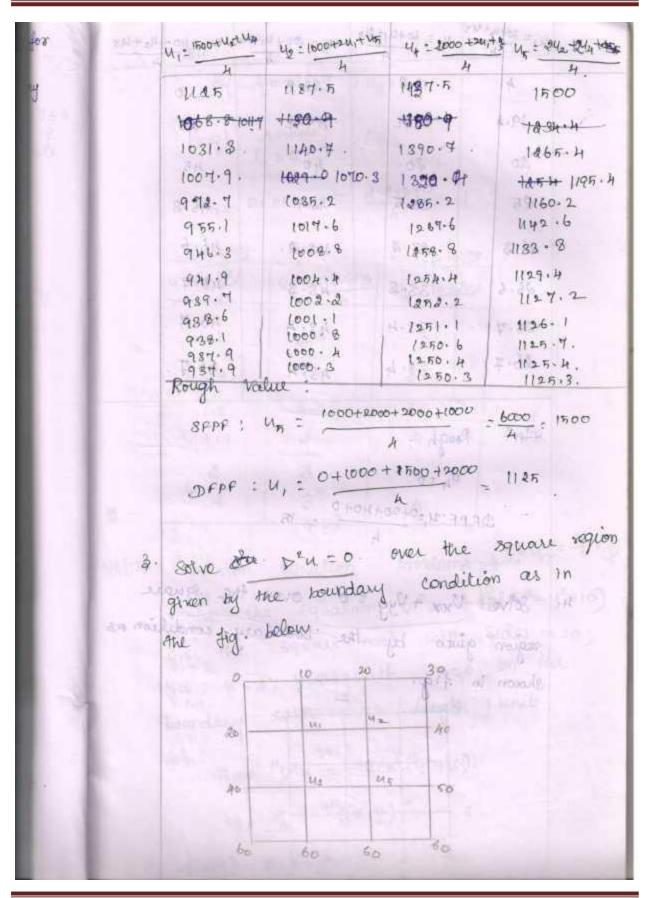
8. Solve
$$0_{44} = 0xx + 0xx \lambda a ; 6 > 0 . subject
15. $u(x, 0) \ge 0; u(0, t) \ge 0; u(ta), t) \ge 0; u_{4}^{t} + 1 = 0; (x_{1}, 0) \ge 100 (9x - x^{2}) choosing h = 1/2
compute 'u' for hitmes step .
solvi:
 $u_{44} = 0 = 0 = 0.7$.
 $u_{5} = 0 = 1 ; h \ge 0.7$.
 $u_{5} = 0 = 1 ; h \ge 0.7$.
 $u_{5} = 0 = 0 = 0.7$.
 $u_{5} = 0.7$$$$

1/200 1/2011
The Suplace and poisson Equation.
The Suplace Equation is
$$\frac{2^{4}u}{2^{4}x^{2}} + \frac{2^{4}u}{2^{4}y^{2}} = 0$$
.
 $\frac{1}{14}u^{4} + \frac{1}{14}u^{4} + \frac{1}{14}u^{4}$

By bebrann iteration method she want by 1. over the surface square region of side 4 Satisfying ulory)=0 0 = y = 4; ulary)=8+2y U(x10)=x2/2 01×14 1 U(x14)=x2101×14. Con the values at the interior points with h= k= Soln ! in micharph amazin (0, 4) = y=A u(4,y)= X=A. Ц(HA) = 97 - A + 1 - 1 - K Kepti BLANC 10 Juni 0 05 2 Silgella Rough values: $SFPF: U_{5} = \frac{0+4+12+2}{4} = 4.5$ DFPF: U1 = 0+4+0+45 = 8.1 $DAPF: u_3 = \frac{1}{2} + \frac{16}{12} + \frac{115}{2} = 9.1$ $DFPF = u_{y} = \underbrace{0 + u_{y} + 0 + 2}_{i} = 1.6$ DEPF = Up = 645+12+2+8 - 5.6



2. Solve the Ellipstic Egn Unx+Uyy=0 following square mesh with the bounda Values are shown below 500 1000 500 0 U.a (000) 1000 Un-45-2000 2000 UN UR 1000 1000 500 1000 500 0 Soln : By symmetry 4, c 43 4, = 44 4x = 46 38 42 = 48 un - un us - un Hence, M, = us = Uy = ug Cla = Ug Masub Now, we find only 142144, u,



30-14+43 43 = 60 + Urt. UA U3 = 100+ U1+144 U4 = 110-4 18.8 28.8 0 P.19.9 29.9. 19.4 40 11ADEC ao 30. 40 45 71.4.1-42.5. 46.8 30% 38.5 1-1101 46.6 26.3 33.2 43.2. 26.6 38-8 48.3 H6.4 46.4 · 33.4 26.7 48.4 1.900 46.7 33.4 26.7. 43.4 ASU a) 1001-0000-0008-0001 Soln Rough : UH =0. 1145 DEFF DFPF:4, 50+ 20+ 40+ 0 199100 sult ways h Solve Uxx + Vyy gua over 4. boundary condil region given by the shown in fig. 16 WE 199. 4 100 il.p. 2 5

10 (1x + 4 + 10) Nº G(x,y) ч A same y=3 (2,2) = (5,2) 0136 10.3)2 112 12 Em 100) 4440 (0,1)0 (31) (1.0) (2.0) (3,0) (010 4=01+0 -64810 By symmetry, 4,= 44 alt ant Ro 42 41= U2+U3+150 4 241+180 A 0 . .0 0 68.8 48.8 37-5 -62.9 77.9.0 65.9 66 - 4 81.4 67.3 82.8 14.5 SIG. M.L. 67.5 84.5 74.9 tions 1 Mignal 67.5 danga. shi w 67.5. 82.5 7501+82+81201-(or shink & Vot = (Howster

so solve
$$\frac{y^2u}{y^2} = \frac{9x^2y^2}{16x^2}$$
 our the square
bounded by the lines $x = -3$; $x = 2$, $y = -2$;
 $y = 3$ with $u = 0$ on the boundary and
megh dength $=1.497$
Solve $y^2u = 8x^2y^2$
 $wk = 7$ $y^2u = -f(x_1y_1)$
 $-f(x_1y_1) = -8x^2y^2$ (..., $h = 1$)
 $\frac{10}{16x^2}$
 $\frac{10}{16x^2}$

41= 42+U4+8 Un = 42+44+46+ 242-8 42 = 4+HS + HB QUITUS H Un = U2 houldow 0 2/1 1/20 0 2 14 -1 - April-1 diput -2 -1+5 MB - 8.5. -1.5 -1-8 - 2.8 -1.8 -1.9 1-0 - 2.9 - = (h 2 -2 -2 -2. - 3 harming by $\gamma_{\rm p} M < 12$ With the start was a start with the start and a start and a start a start a start a pline wit ALL HALKS HAL 10 - 11 = 11 - 12

Questions	opt1	opt2	opt3	opt4	Answer
If $B^2-4AC = 0$, then the differential equation is said to be	parabolic	elliptic	hyperbolic	equally spaced	parabolic
If $B^2-4AC > 0$, then the differential equation is said to be	parabolic	elliptic	hyperbolic	equally spaced	hyperbolic
If $B^2-4AC < 0$, then the differential equation is said to be	parabolic	elliptic	hyperbolic	equally spaced	elliptic
(f(x+h)-f(x))/h is known as the	difference quotient	average	derivative	f(x)	difference quotient
The equation $del^2(u) = 0$ is equation.	Laplace	Poisson	Heat	Wave	Laplace
One dimensional heat equation is the example of equation.	Laplace	Poisson	Parabolic	Hyperbolic	Parabolic
One dimensional wave equation is the example of equation.	Laplace	Poisson	Parabolic	Hyperbolic	Hyperbolic
The differential equation is said to be parabolic, if	B^2-4AC		B^2-4AC < 0	B^2-4AC =0	B^2-4AC
The differential equation is said to be elliptic, if	B^2-4AC		$B^2-4AC < 0$	B^2-4AC =0	$B^2-4AC < 0$
The differential equation is said to be hyperbolic, if	B^2-4AC		B^2-4AC < 0	B^2-4AC =0	$B^2-4AC > 0$
[x f(xx)+yf(yy)]=0 x>0, y>0 is type of equation.	elliptic	Poisson	Parabolic	Hyperbolic	elliptic
[f(xx)-2f(xx)]=0, x>0, y>0 is type of equation.	elliptic	Poisson	Parabolic	Hyperbolic	Hyperbolic
process is used to solve two dimensional heat equations	Newtons	Gaussian	Laplace	Liebmanns iteration	Liebmanns iteration
The equation (\tilde{N}^2) u = 0 is known as equation	Laplace	Poisson	heat	wave	heat
	Euplace	1 0135011	neut	wave	neut
The formula is used to complete the improved value of u,	Newtons	elimination	Liebmanns iteratio	reduction	Liebmanns iteration
The value of u can be improved by process	Newtons	elimination	Liebmanns iteratio		Liebmanns iteration
The value of u is obtained at any lattice points which is					
the arithmetic mean of the values of u at 4 lattice points near to it	interior	exterior	positive	negative	interior
The value of $u_{i,j}$ in the difference equation are defined only at the					
points	equal	unequal	apex	lattice	lattice
The points of intersection of these families of lines are called					
points	equal	unequal	apex	lattice	lattice
If $B^2 - 4AC > 0$ then the given equation is	Parabolic	elliptic	hyperbolic	rectangular hyperbolic	hyperbolic
The differential equation is said to be in a region R if B^2					
4AC < 0 at all points of a region The differential equation is evid to be	Parabolic	elliptic	hyperbolic	rectangular hyperbolic	elliptic
The differential equation is said to be in a region R if $B^2 - 4AC = 0$ at all points of the region	Parabolic	allintia	humarhalia	raatangular hymorhalia	Parabolic
B 2-4AC = 0 at an points of the region	rarabolic	elliptic	hyperbolic	rectangular hyperbolic	rarabolic
If $(ka)/h < 1$, it is stable but the accuracy of the solution decrease with					
the increasing value of	k	a	(ka)/h	k/h	(ka)/h
If $(ka)/h < 1$, it is stable but the accuracy of the solution decrease with					
the increasing value of	k	a	k/h	(ka)/h	(ka)/h
The differential equation is said to be in a region R if					
$B^2 - 4AC = 0$ at all points of the region	Parabolic	elliptic	hyperbolic	rectangular hyperbolic	Parabolic
The differential equation is said to be in a region R if B^2					
4AC < 0 at all points of a region	Parabolic	elliptic	hyperbolic	rectangular hyperbolic	elliptic
The points of intersection of these families of lines are called points	aqual	unaqual	anov	lattice	lattice
points	equal	unequal	apex	lattice	lattice
Schmidt method belongs to type	explicit	implicit	elliptic	hyperbolic	explicit
The Poisson's equation belongs to type	explicit	implicit	elliptic	hyperbolic	hyperbolic
One dimensional heat flow equation belongs to type	explicit	parabolic	elliptic	hyperbolic	parabolic
Laplace equation in two dimensions belongs to type	explicit	parabolic	elliptic	hyperbolic	explicit
The error in solving Poisson equation by methods is of	1	1	1	51	1
order h^2	Difference	iteration	elimination	interpolation	Difference
The error in solvingequation by difference method is of order					
h^2	Newton's	Jacobi's	Poisson	Gaussian	Poisson
The error in solving Poisson's equation by difference methods is of					
order	h	h^2	h^3	h^4	h^2
The equation del ^{\land} 2(u) = f(x, y) is known as equation	Poisson	Newtons	Jacobis	Gaussian	Poisson
The value of ui,j is the average of its value at the neighbouring					
diagonal mesh points	2	3	4	5	4
The value of u(i,j) is the of its values at the four					
neighbouring diagonal mesh points	sum	difference	average	product	average
The value of u(i,j) is the average of its values at the four neighbouring					
mesh points	Square	rectangle	diagonal	column	diagonal
The mesh points are also called	grid point	starting point	Ending point	bisection	grid point
The points of intersection of the dividing lines are called	bisection	mesh points	vertex	end point	mesh points
The differential equation is said to be hyperbolic, if	$B^2-4AC = 0$	$B^2-4AC > 0$	$B^2-4AC < 0$	B^2-4AC <= 0	$B^2-4AC > 0$
The differential equation is said to be elliptic, if	$B^2-4AC = 0$	$B^2-4AC \ge 0$	$B^2-4AC \le 0$	B^2-4AC <=0	$B^2-4AC \le 0$
The differential equation is said to be parabolic, if	$B^2-4AC = 0$	$B^{2}-4AC \ge 0$	$B^2-4AC \le 0$	$B^2-4AC \le 0$	$B^2-4AC = 0$
One dimensional wave equation is the example of equation.	Laplace	Poisson	Parabolic	Hyperbolic	Parabolic
One dimensional heat equation is the example of equation.	Laplace	Poisson	Parabolic	Hyperbolic	Poisson
The equation $del^2(u) = 0$ is equation	parabolic	elliptic	hyperbolic	equally spaced	parabolic
If $B^2-4AC = 0$, then the differential equation is said to be	parabolic	elliptic	hyperbolic	equally spaced	parabolic
If $B^2-4AC > 0$, then the differential equation is said to be	parabolic	elliptic	hyperbolic	equally spaced	hyperbolic
If $B^2-4AC < 0$, then the differential equation is said to be	parabolic	elliptic	hyperbolic	equally spaced	elliptic
		-	-		-