

KARPAGAM UNIVERSITY KARPAGAM ACADEMY OF HIGHER EDUCATION

(Deemed to be University Established Under Section 3 of UGC Act 1956)

COIMBATORE-641 021

DEPARTMENT OF SCIENCE AND HUMANITIES FACULTY OF ENGINEERING

I - B.TECH - I Semester Syllabus

15BTBT102 OBJECTIVES:

MATHEMATICS I

3204

- 1. To impart analytical ability in solving mathematical problems of Physical or Engineering models.
- 2. To understand the concepts of Matrices, Theory of Equations, Differential Calculus and its application, Integral Calculus and its application, Ordinary differential equations.

INTENDED OUTCOMES:

- 1. This course equips students to have basic knowledge and understanding in the field of matrices, integral and differential calculus.
- 2. The students acquire the knowledge of techniques in solving ordinary differential equations that model engineering problems.

UNIT I MATRICES (12)

Fundamentals of Matrix- Inverse of a matrix- Rank of a Matrix – Consistency and Inconsistency of a system of 'm' linear equations in 'n' unknowns – Eigenvalues and Eigenvectors of a real matrix.

UNIT II THEORY OF EQUATIONS

(12)

(12)

Relations between coefficients and roots: Irrational and imaginary roots – symmetric functions of the roots – transformation of equations – reciprocal equations and formation of equations whose roots are given.

UNIT III DIFFERENTIAL CALCULUS AND ITS APPLICATION

Differentiation and Derivatives of simple functions – Successive Differentiation – Tangent and Normal-Radius of curvature – Velocity and acceleration.

UNIT IV INTEGRAL CALCULUS AND ITS APPLICATIONS (12)

Various types of integration - Reduction formula for $e^{ax}x^n$, $\sin^n x$, $\cos^n x$, $\sin^n x \cos^m x$ (Statement only). – Length, Area and Volume of solid revolution.

UNIT V ORDINARY DIFFERENTIAL EQUATIONS

(12)

Differential equations of first order and higher degree – higher order differential equations with constant coefficients- Euler's form of Differential equations.

TEXT BOOKS:

S.	AUTHOR(S)	TITLE OF THE	PUBLISHER	YEAR OF
NO.	NAME	BOOK		PUBLICATION
1	Grewal. B.S	Higher Engineering	Khanna Publications,	2013
		Mathematics	Delhi.	
2	B.V.Ramana	Uighar Engineering	Tata McGraw Hill	2010
\ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \	D. V.Kailialia	Higher Engineering		2010
		Mathematics	EducationPvt.Ltd, New	
			Delhi.	

REFERENCES:

S.	AUTHOR(S)	TITLE OF THE	PUBLISHER	YEAR OF
NO.	NAME	BOOK		PUBLICATION
1	Dass H.K.	Engineering	S.Chand& Co.,	2008
		Mathematics	New Delhi.	
2	Bali N.P.,	A text book of	Laxmi publications Pvt.	2014
	Manish Goyal	Engineering	Ltd, New Delhi.	
		Mathematics		
3	Michael D.	Advanced	Pearson Education, India	2006
	Greenberg	Engineering		
		Mathematics		

WEBSITES:

- 1. www.intmath.com
- 2. www.efunda.com
- 3. www.mathcentre.ac.uk



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DEPARTMENT OF SCIENCE AND HUMANITIES FACULTY OF ENGINEERING I - B.TECH - I Semester

LESSON PLAN

SUBJECT: Mathematics – I SUB CODE: 15BTBT102

S.NO	Topics covered		
	UNIT- I MATRICES	hours	
1.	Introduction of Matrix and its applications	1	
2.	Fundamentals of Matrix		
3.	Inverse of a matrix		
4.	Inverse of a matrix		
5.	Rank of a Matrix		
6.	Rank of a Matrix		
7.	Consistency and Inconsistency of a system of 'm' linear equations in 'n' unknowns		
8.	Consistency and Inconsistency of a system of 'm' linear equations in 'n' unknowns		
9.	Consistency and Inconsistency of a system of 'm' linear equations in 'n' unknowns		
10.	Characteristic Equation - Eigen values and Eigen vectors		
11.	Characteristic Equation - Eigen values and Eigen vectors		
12.	Characteristic Equation - Eigen values and Eigen vectors		
	Total	12	
	UNIT II THEORY OF EQUATIONS		
13.	Introduction about different types of equations	1	
14.	Relation between coefficients and roots of the equation	1	
15.	Relation between coefficients and roots of the equation		
16.	Solving an equation with irrational and imaginary roots		
17.	Solving an equation with irrational and imaginary roots		
18.	Symmetric functions of the roots	1	
19.	Symmetric functions of the roots	1	
20.	Transformation of equations	1	
21.			
22.	Reciprocal equations and formation of equations whose roots are given		
23.	Reciprocal equations and formation of equations whose roots are given		
	Total	11	
	UNIT III DIFFERENTIAL CALCULUS AND ITS APPLICATION		
24.	Introduction : Derivative and Differential equation	1	

25. Basics formulas in differentiation	1
	1 1
1	
27. Derivatives of simple functions	1
28. Successive Differentiation	1
29. Successive Differentiation	1
30. Tangent and Normal	1
31. Problems in Tangent and Normal	1
32. Curvature of a curve and Radius of curvature	1
33. Problems in Radius of curvature	1
34. Problems in Radius of curvature	1
35. Velocity and acceleration	1
36. Problems based on velocity and acceleration	1
Total	13
UNIT IV INTEGRAL CALCULUS AND ITS	
APPLICATIONS	
37. Introduction - Integral calculus and its applications	1
38. Basic concepts in integration	1
39. Various types of integration	1
40. Various types of integration	1
41. Problems in integration	1
42. Reduction formula for $e^{ax}x^n$, $\sin^n x$	1
43. Reduction formula for $\cos^n x \sin^n x \cos^m x$	1
44. Problems using Reduction formula	1
45. Length and Area	1
46. Problems in finding the Length and Area	1
47. Problems in finding the volume of solid of revolution	1
48. Problems in finding the volume of solid of revolution	1
Total	. 12
UNIT – V ORDINARY DIFFERENTIAL EQUATIONS	
49. Introduction - Ordinary differential equations	1
50. Applications of ordinary differential equations	1
51. Differential equations of first order and higher degree	1
52. Differential equations of first order and higher degree	1
53. Problems in differential equations of first order and higher degree	1
54. Higher order differential equations with constant coefficients	1
55. Higher order differential equations with constant coefficients	
56. Problems in differential equations of first order and higher degree	1
57. Problems in differential equations of first order and higher degree	
58. Euler's form of differential equations	1
59. Problems in Euler's form of differential equations	1
60. Question paper discussion	1
Total	12
TOTAL	60

Staff In charge HoD



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DEPARTMENT OF SCIENCE AND HUMANITIES FACULTY OF ENGINEERING

I - B.TECH - I Semester

OBJECTIVES OF THE COURSE

SUBJECT: Mathematics – I SUB CODE: 17BTBT102

- To impart analytical ability in solving mathematical problems of Physical or Engineering models.
- To understand the concepts of Matrices, Theory of Equations, Differential Calculus and its application, Integral Calculus and its application, Ordinary differential equations.

Unit -1

Matrices .

Definition of a Matrices.

A system of any mn mumbers arranged in a rectangular duray of m-rows and n- columns is called Matrices of order mxn and is denoted by

 $B = (a_{11})_{m \times n} = \begin{bmatrix} a_{11} & a_{12} & \dots & a_{1n} \\ a_{21} & a_{22} & \dots & a_{2n} \\ a_{m_1} & a_{m_2} & \dots & a_{m_n} \end{bmatrix}_{m \times n}$

where aij's are called the enteries or dements of the Matrices.

Types of Matrices.

A Materices having only one now is D Rows Matricus: Called as now Materices

eg: $\beta = \int_{1}^{2} 2 \frac{3}{1 \times 3}$.

Column's matrices! A Matrices having only one Column is Called as Column matrices.

eg:
$$A = \begin{bmatrix} 1 \\ 2 \\ 3 \end{bmatrix}$$
sx1

A Matine hering equal number of called asquare Market 189: pro 51 2 37 Diagonal Hatrix A Square Matrix having its entries along the leading diagonal and all other entries are your is latted diagonal $A = \begin{cases} 1007 \\ 020 \\ 003 \end{cases} 5x3$ n) scalar Mabin A diagonal Matrix whose leading diagonals are all Same is alled Ecalas Materix $A = \begin{bmatrix} 3 & 0 & 0 \\ 0 & 3 & 0 \\ 0 & 0 & 3 \end{bmatrix} \frac{3}{3} \times 3$ Unit Matrix: A scalar Matrix whose diagonal dements are one is called a Unit Matrix eg: A: [007] 000]3x3.

Triangular Malaix.

Types: Upper driangular Matrix:

Types: Upper driangular Matrix:

below the reading diagonal are yono is below the reading diagonal are yono is alled upper toriangular Matrix.

alled upper toriangular Matrix.

lower toriangular Matrix.

lower toriangular Matrix

A square Hatrix un which all the elements whose the deading diagonal are elements whose the deading diagonal are elements whose the deading of a govern Matrix gero is called a dower toriangular Matrix ger for a matrix.

Transpose of a Matrix.

The Matrix got from a given Matrix.

The Matrix got from a given Matrix.

Transpose of a Matrix.

The Natrix got from a given Matrix

by interchanging its rows and oblumns

is called Transpose of that Matrix.

is called Transpose of that Matrix.

A = \[\begin{pmatrix} 2 & 3 \\ 4 & 5 & 6 \\ 7 & 8 & 9 \end{pmatrix} \]

The Natrix got from a given Matrix.

By interchanging its rows and oblumns

is called Transpose of that Matrix.

Then
$$A^{T} = \begin{bmatrix} 7 & 4 & 7 \\ 2 & 5 & 8 \\ 3 & 6 & 9 \end{bmatrix} 3 \times 3.$$

square Matrix I us baid to be Symmetric if A=AT and Skew Symmetric if $A = A^T$.

Here $A = \begin{bmatrix} 14 & 5 \\ 4 & 2 & 6 \\ 5 & 6 & 3 \end{bmatrix} 3x3$ This $A^T = \begin{bmatrix} 1 & 4 & 5 \\ 4 & 2 & 6 \\ 5 & 6 & 3 \end{bmatrix} 3x3$ an Symmetric Matrix. Conjugate rol a Matrix. A Matrix a obtained by suplacing each clement of I by its Complex Conjugate is Called Conjugate of A and us denoted by A eg: Presquisat bollo : $A = \begin{bmatrix} 1+i & 2 & 3-i \\ 4 & 5+i & i \\ 7 & 8+3i & 9 \end{bmatrix} 3x3.$

1) Hermitian Matrices and Askens describer Herinistian of A= PT. A square Matrix A is said to be Skew Mennitian if 40-AT. Eg: P= \[1-4i \] 2 \[2x2. \] The AT = \[1 +4i \] AT = \[1 -4i \]
1-4i 2 \]
2x2 | 1+4i 2 \]
2x .. A is Mermetian. Eg: $B = \int_{-2+i}^{3i} \frac{2+i}{i} \Big|_{2\times 2}$ The $B^{T} = \begin{bmatrix} 3i & -2+i \\ 2+i & i \end{bmatrix}_{2\times 2}$ $B^{T} = \begin{bmatrix} -3i & -2-i \\ 2-i & -i \end{bmatrix}_{2\times 2}$ $\widehat{\beta^{T}} = - \begin{bmatrix} 3\hat{i} & 2+\hat{i} \\ -2+\hat{i} & \hat{i} \end{bmatrix} 2 \times 2$ $B = \overline{BT}$. A

Singular and non Sungular Matrices m of the main diagonal Singular Materices If determinant of A is your is, Intel eternents of a requare matrix A is Called then A is said to be a singular Miling thace sof A and is denoted by non singular matricus. 4 (A) to the A is said to be a trace (n) as to (A). non-singular Materia. Equal Matrix. Two matrices p and B au Said Coursement elements of B. B. of of The Trace (A) = 1+ 15+9 DAB have are of same order ta(A)=15. ii) Each element of A is equal to the deturninant of a Mathix. Determinant is Calculating the numerical Corresponding element of B. Value of a materix it is denoted by eg: 8 p = [1 2 3]
4 5 6
7 8 9 8 x 3 (A) or det (A) or s (A). 16) Sul Matrin!

A Matrix are obtained from A by elementary transmation is called LAI = 1 [6-8]-1[3+6] +1[-1-4] the sub matrix of A. = 3-9-5 = -1/7.

Adolition of two matrices.

Adolition of two matrices.

Adolition of two matrices.

Adolition of two matrices.

Adolition of two added and 8 are of Same if and only if A and 8 are of Same order.

Carrisponding element of A is added with the Carrisponding element of B.

B= \[1 & 2 & 3 \]

A = \[1 & 2 & 3 \]

A = \[1 & 2 & 3 \]

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A = \[1 & 2 & 3 \]

A = \[3 & 3 \

i) Commutative (ie) A+B=B+A.

ii) Associative (ie) (A+B)+C=A+(B+C).

iii) Scalas Multiplication (ie) (x+p)A

the soule material of the

Multiplications. Of two, Mathieus.

Two matrices A and B. can be multiplied only if the number of number of sow's of the second the number of sow's of the second matrices:

(ie) eg: $4 = \begin{bmatrix} 1 & 2 & 3 \\ 4 & 7 & 6 \end{bmatrix} ax3$ The PB = $\begin{bmatrix} 1+1+9 & 1+10+18 \\ 4+10+18 & 16+25+36 \end{bmatrix} 2x2$ $\begin{bmatrix} 14 & 32 \\ 32 & 7+ \end{bmatrix} 2x2$

Propertus:

- 1) Commutative (10) AB &BA.
- ii) Associative (ie) (AB)(=A(BC)
- iii) Scalas Multiplication (ic) $\alpha(A) = AA$.

Alpant Axapl-q

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The Co-factor of A is.

$$A_{3} = \begin{bmatrix} + & 2 & 3 \\ 1 & 3 & - & 2 & 3 \\ -2 & 3 & + & -2 & 1 \end{bmatrix}$$

$$- \begin{vmatrix} 1 & 1 & 1 & 1 \\ 13 & + & -2 & 3 \\ -2 & 3 & - & -2 & 1 \end{vmatrix}$$

$$+ \begin{vmatrix} 1 & 1 & 1 & 1 \\ -2 & 3 & - & -2 & 1 \\ -2 & 3 & - & -2 & 1 \end{vmatrix}$$

$$= \begin{bmatrix} -6 - 3 & -(3+6) & +(1-4) \\ -(3-1) & +(3+2) & -(1+2) \\ +(3+2) & -(3-1) & +(-2-1) \end{bmatrix}$$

$$\begin{bmatrix} -9 & -9 & -3 \\ -2 & 5 & -3 \\ 6 & -2 & -3 \end{bmatrix}$$

Inverse in Matrix.

> Invouse mating in also known as recipsocal of Matrix.

=> Inverse of a matrix can be obtained only for a square Matrix.

> Inverse of a Matrix is denoted by Fi and defined as

tind the Problem. Invent of the matrix

$$D = \begin{bmatrix} 1 & 2 \\ -1 & -1 \end{bmatrix}.$$

$$A^{-1} = \frac{1}{1A1} (adj A)$$

= $\frac{1}{-2} \left[\frac{-4}{1} \right]^{-2}$

$$A^{-1} = \begin{bmatrix} 2 & 1 \\ -\frac{1}{2} & -\frac{1}{2} \end{bmatrix}.$$

$$\begin{array}{c} \widehat{\mathbf{L}} \\ \widehat{\mathbf{L}} \end{array} \quad A = \begin{bmatrix} 1 & 2 \\ 2 & -2 \end{bmatrix}.$$

Adj
$$n = \begin{bmatrix} -2 & -2 \\ -2 & 1 \end{bmatrix}$$

$$|A| = -2 - 4 \text{ into } \text{ for smooth}$$

$$|A| = -6 - 6$$

$$|A| = \frac{1}{-6} \left[-2 - 2 \right]$$

$$|A| = \frac{1}{-6} \left[-2 - 2 \right]$$

$$|A| = \frac{1}{3} \left[-2 - 2 \right]$$

$$A = \begin{bmatrix} 3 & -2 \\ 7 & 8 \end{bmatrix}.$$

$$Ady^{\circ} A = \begin{bmatrix} 3 & +2 \\ -1 & 3 \end{bmatrix}$$

$$AA = \begin{bmatrix} 3 & +2 \\ -1 & 3 \end{bmatrix}$$

$$AA = \begin{bmatrix} -1 & -2 & -2 \\ -1 & 3 \end{bmatrix}$$

$$AA = \begin{bmatrix} -1 & -2 & -2 \\ -2 & 3 & -1 \\ -2 & 3 & -1 \end{bmatrix}$$

$$AA = \begin{bmatrix} -1 & -2 & -2 & -2 \\ -2 & 3 & -1 \end{bmatrix}$$

$$AA = \begin{bmatrix} -1 & -2 & -2 & -2 \\ -2 & 3 & -1 \end{bmatrix}$$

$$AA = \begin{bmatrix} -1 & -2 & -2 & -2 \\ -2 & 3 & -1 \end{bmatrix}$$

$$AA = \begin{bmatrix} -1 & -2 & -2 & -2 \\ -2 & 3 & -1 \end{bmatrix}$$

$$AA = \begin{bmatrix} -1 & -2 & -2 & -2 \\ -2 & 3 & -1 \end{bmatrix}$$

$$AA = \begin{bmatrix} -1 & -2 & -2 & -2 \\ -2 & 2 & -2 \end{bmatrix}.$$

$$AA = \begin{bmatrix} -1 & -2 & -2 & -2 \\ -2 & 2 & -2 \end{bmatrix}.$$

$$AA = \begin{bmatrix} -1 & 0 & -4 \\ -2 & 2 & 5 \\ -2 & 3 & -1 & 2 \end{bmatrix}.$$

$$= \begin{bmatrix} 1 & 2 & 5 \\ 1 & 1 & 2 \end{bmatrix} - \begin{bmatrix} -2 & 5 \\ 5 & 2 \end{bmatrix} + \begin{bmatrix} -2 & 2 \\ 5 & -1 \end{bmatrix}$$

$$= \begin{bmatrix} -4 & 1 & -4 \\ 1 & 2 & 2 \end{bmatrix} + \begin{bmatrix} 1 & 0 \\ 3 & 2 \end{bmatrix} - \begin{bmatrix} 1 & 0 \\ 3 & -1 \end{bmatrix}$$

$$= \begin{bmatrix} -4 & 15 \\ 2 & 5 \end{bmatrix} - \begin{bmatrix} -4 & -15 \\ -2 & 5 \end{bmatrix} + \begin{bmatrix} 2 & -6 \\ -2 & 5 \end{bmatrix}$$

$$= \begin{bmatrix} -4 & 15 \\ 8 & -(-4 - 15) \end{bmatrix} + \begin{pmatrix} 2 - 6 \\ -(-1) \\ 8 & -(5 - 8) \end{bmatrix} + \begin{pmatrix} 2 - 6 \\ 2 & 1 \end{bmatrix}$$

$$= \begin{bmatrix} 9 & -4 \\ 14 & 1 \\ 8 & 3 \end{bmatrix} - \begin{bmatrix} 9 & 4 & 8 \\ 19 & 14 & 3 \\ -4 & 1 & 2 \end{bmatrix}$$

$$= \begin{bmatrix} 9 & 4 & 8 \\ 19 & 14 & 3 \\ -4 & 1 & 2 \end{bmatrix}$$

$$= \begin{bmatrix} 9 & 4 & 8 \\ 19 & 14 & 3 \\ -4 & 1 & 2 \end{bmatrix}$$

$$= \begin{bmatrix} 9 & 4 & 8 \\ 19 & 14 & 3 \\ -4 & 1 & 2 \end{bmatrix}$$

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$$= \begin{bmatrix} 9 & 4 & 8 \\ 19 & 14 & 3 \\ -4 & 1 & 2 \end{bmatrix}$$

$$= \begin{bmatrix} 9 & 4 & 8 \\ 19 & 4 & 8 \\ 19 & 5 & 25 \end{bmatrix}$$

$$= \begin{bmatrix} 9 & 4 & 8 \\ 19 & 5 & 25 \end{bmatrix}$$

$$= \begin{bmatrix} 9 & 4 & 8 \\ 19 & 5 & 25 \end{bmatrix}$$

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$$= \begin{bmatrix} 9 & 4 & 8 \\ 19 & 5 & 25 \end{bmatrix}$$

$$= \begin{bmatrix} 9 & 4 & 8 \\ 19 & 5 & 25 \end{bmatrix}$$

$$\begin{aligned}
-A &= \begin{bmatrix} 5 & -6 & 1 \\ 7 & 4 & -3 \\ 2 & 1 & 6 \end{bmatrix}. \\
|A| &= 5 \begin{vmatrix} 4 & -3 \\ 1 & 6 \end{vmatrix} + \frac{1}{4} \begin{vmatrix} 7 & -3 \\ 2 & 6 \end{vmatrix} + \frac{1}{4} \begin{vmatrix} 7 & 7 \\ 2 & 6 \end{vmatrix} + \frac{1}{4} \begin{vmatrix} 7 & 7 \\ 2 & 6 \end{vmatrix} + \frac{1}{4} \begin{vmatrix} 7 & 7 \\ 2 & 6 \end{vmatrix} + \frac{1}{4} \begin{vmatrix} 7 & 7 \\ 2 & 6 \end{vmatrix} + \frac{1}{4} \begin{vmatrix} 7 & 7 \\ 2 & 6 \end{vmatrix} + \frac{1}{4} \begin{vmatrix} 7 & 7 \\ 2 & 6 \end{vmatrix} + \frac{1}{4} \begin{vmatrix} 7 & 7 \\ 2 & 6 \end{vmatrix} + \frac{1}{4} \begin{vmatrix} 7 & 7 \\ 2 & 6 \end{vmatrix} + \frac{1}{4} \begin{vmatrix} 7 & 7 \\ 2 & 6 \end{vmatrix} + \frac{1}{4} \begin{vmatrix} 7 & 7 \\ 2 & 6 \end{vmatrix} + \frac{1}{4} \begin{vmatrix} 7 & 7 \\ 2 & 6 \end{vmatrix} + \frac{1}{4} \begin{vmatrix} 7 & 7 \\ 2 & 6 \end{vmatrix} + \frac{1}{4} \begin{vmatrix} 7 & 7 \\ 2 & 6 \end{vmatrix} + \frac{1}{4} \begin{vmatrix} 7 & 7 \\ 4 & -3 \end{vmatrix} + \frac{1}{4} \begin{vmatrix} 7 & 7 \\ 7 & -3 \end{vmatrix} + \frac{1}{4} \begin{vmatrix} 7 & 7 \\ 7 & 7 \end{vmatrix} + \frac{1}{4} \begin{vmatrix} 7 & 7 \\ 4 & -3 \end{vmatrix} + \frac{1}{4} \begin{vmatrix} 7 & 7 \\ 7 & -3 \end{vmatrix} + \frac{1}{4} \begin{vmatrix} 7 & 7 \\ 7 & 7 \end{vmatrix} + \frac{1}{4} \begin{vmatrix} 7 & 7 \\ 4 & -3 \end{vmatrix} + \frac{1}{4} \begin{vmatrix} 7 & 7 \\ 7 & -3 \end{vmatrix} + \frac{1}{4} \begin{vmatrix} 7 & 7 \\ 7 & 7$$

$$A^{-1} = \frac{1}{|P|} \begin{cases} ady(A) & = A \\ -1 & = A \end{cases}$$

$$= \frac{1}{-1} \begin{cases} -1 & = A \\ -1 & = A \end{cases}$$

$$= \frac{27}{-48} \begin{cases} -17 & = A \\ -17 & = A \end{cases}$$

$$= \frac{27}{419} \begin{cases} -17 & = A \\ -17 & = A \end{cases}$$

$$= \frac{27}{419} \begin{cases} -17 & = A \\ -17 & = A \end{cases}$$

$$= \frac{17}{419} \begin{cases} -17 & = A \\ -17 & = A \end{cases}$$

$$= \frac{17}{419} \begin{cases} -17 & = A \\ -17 & = A \end{cases}$$

Rank of the Matrix

The Rank of the Nation Used to find of any highest non-vanishing minor the degree of the Matrix.

Eq:
$$A = \begin{bmatrix} 1 & 1 & 1 \\ 1 & 2 & 3 \\ 2 & 1 & 3 \end{bmatrix}$$

$$\sim \begin{bmatrix} 1 & 1 & 1 \\ 0 & 1 & 2 \\ 0 & 1 & 1 \end{bmatrix} R_2 \rightarrow R_2 - R_1$$

$$R_3 \rightarrow R_3 - \lambda R_1$$

$$\sim \begin{bmatrix} 1 & 1 & 1 \\ 0 & 1 & 2 \\ 0 & -1 & 1 \end{bmatrix}$$

$$\sim \begin{bmatrix} 1 & 1 & 1 \\ 0 & 1 & 2 \\ 0 & 0 & 3 \end{bmatrix}$$

$$\sim \begin{bmatrix} 1 & 1 & 1 \\ 0 & 1 & 2 \\ 0 & 0 & 3 \end{bmatrix}$$

$ A = \begin{bmatrix} A \\ 2 \\ 1 \end{bmatrix}$	3 2 1 -4 7 -1	arent a
~ [$ \begin{bmatrix} 1 & -7 & -1 \\ 2 & 1 & -4 \\ 4 & 3 & 2 \end{bmatrix} $	2 1 - 4 2 1 - 12 0 15 - 2
~	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	$R_2 - 2R_1 - (-8)$ $R_3 - 2R_2$
~ [$ \begin{bmatrix} 1 & -7 & -1 \\ 0 & 15 & -2 \\ 0 & 0 & 88 \end{bmatrix} P_3 \Rightarrow P_3 $	0 1 6
	e(a) = 3/1.	of the Metric
Consistent	e(A= e(A·B)= n e(A)= e(AB) €	Infinite need still
In Consistent		No solution.

$$A = \begin{bmatrix} 1 & 1 & 1 \\ 1 & 2 & 3 \\ 1 & 2 & \lambda \end{bmatrix}, \quad x = \begin{bmatrix} x \\ y \\ z \end{bmatrix}, \quad B = \begin{bmatrix} 6 \\ 10 \\ \mu \end{bmatrix}$$

$$\begin{bmatrix}
1 & 1 & 1 \\
1 & 2 & 3 \\
1 & 2 & \lambda
\end{bmatrix}
\begin{bmatrix}
x \\
y
\end{bmatrix}
=
\begin{bmatrix}
1 & 0 \\
10 \\
\mu
\end{bmatrix}$$

$$(A,B) = \begin{bmatrix} 1 & 1 & 1 & 6 \\ 1 & 2 & 3 & 10 \\ 1 & 2 & \lambda & \mu \end{bmatrix}$$

$$\sim \begin{bmatrix} 1 & 1 & 1 & 6 \\ 0 & 1 & 2 & 4 \\ 0 & 0 & \lambda^{-3} & \mu^{-10} \\ R_3 \rightarrow R_3 \stackrel{?}{\sim}_2 \\ \end{cases}$$

unconsistent and has no solution

Consistent 4 shas unique sola:

1) Test for consistency and solve if benistent

1)
$$4z+3y+2z+7=0$$
 $4z+3y+2z=-1$
 $2z+y-4z+1=0$ $2z+y-4z=-1$
 $z-7y-x=0$

$$A = \begin{bmatrix} 4 & 3 & 2 \\ 2 & 1 & -4 \\ 1 & -7 & -1 \end{bmatrix}, \quad x = \begin{bmatrix} x \\ y \\ Z \end{bmatrix}, \quad 8 = \begin{bmatrix} -7 \\ -1 \\ 0 \end{bmatrix}.$$

$$A \times = B$$

where,

$$\begin{bmatrix} 4 & 3 & 2 \\ 2 & 1 & -4 \\ 1 & -7 & -1 \end{bmatrix} \begin{bmatrix} X \\ Y \\ Z \end{bmatrix} = \begin{bmatrix} -7 \\ -1 \\ 0 \end{bmatrix}.$$

$$(A_18) = \begin{bmatrix} 4 & 3 & 2 & -7 \\ 2 & 1 & -4 & -1 \\ 1 & -7 & -1 & 0 \end{bmatrix}$$

PCA, B) = 37 = 1 + = 5 + y 5 + x + (1 4+2 T+2+- 1+2+- 1+2 Q(A) = Q(A)B) = n The soln is consistent and it has Origne Isoln. 2) 4x+3y+2x+1=0 2x+y-ax+1=0 x-7y-z=0. 4x +3y+2z=-7 2x +y-4z=-1 x-7y-7=0 $\beta = \begin{bmatrix} A & 3 & 2 \\ 2 & 1 & 4 \end{bmatrix} \times \begin{bmatrix} \times \\ Y \\ Z \end{bmatrix}, B = \begin{bmatrix} -7 \\ -1 \end{bmatrix}.$ $\begin{bmatrix}
A_{1}B_{3} = \begin{bmatrix}
1 & 3 & 2 & -1 \\
2 & 1 & -4 & -1 \\
1 & -7 & -1 & 0
\end{bmatrix}$

yer remutering and seize in

Q(h) = 3, Q(h) = 3 Q(h) = P(h|B) = n = 3.The system of equation u consistent Bhas a unique Ustr -608z = 296 $z = \frac{-296}{606}$ -2y - 20z = 10 $-2y - \frac{135}{76} = 10$ $y = \left(10 - \frac{135}{12}\right) \left(\frac{-1}{2}\right)$ $y = \frac{-5}{38}$ 4x + By + 2z = -7 $4x + 3\left(\frac{-5}{38}\right) + 2\left(\frac{-37}{76}\right) = -7$ $x = \frac{-107}{76}$

2+y+z=3

$$2+y+z=3$$

 $3x+3y^{-6}z=1$
Given $2+y+z=3$
 $3+y-z=1$
 $3x+3y-5z=1$

where
$$A \times = 8$$

$$A = \begin{bmatrix} 1 & 1 & 1 \\ 1 & 1 & -1 \\ 33 & -5 \end{bmatrix} \times \begin{bmatrix} x \\ y \\ z \end{bmatrix}, B = \begin{bmatrix} s \\ 1 \\ 1 \end{bmatrix}$$

$$(A_1B) = \begin{bmatrix} 1 & 1 & 3 \\ 1 & 1 & -1 & 1 \\ 3 & 3 & -5 & 1 \end{bmatrix}.$$

$$P(A) = 3$$
 $P(A|B) = 3$
 $P(A) = P(A|B) = n = 3$

The system is consistent and has

-82 =-8

3)
$$2x+3y-z=9$$

 $x+y+z=9$
 $3x-y-z=-1$
 $A = \begin{bmatrix} 2 & 3 & -1 \\ 3 & 1 & 1 \\ 3 & -1 & -1 \end{bmatrix}$
 $A = \begin{bmatrix} x \\ y \\ z \end{bmatrix}$
 $A = \begin{bmatrix} 2 & 3 & -1 & 9 \\ 9 & -1 \\ 3 & -1 & -1 \end{bmatrix}$

$$A = \begin{bmatrix} 2 & 3 & -1 & 9 \\ 1 & 1 & 1 & -1 \\ 3 & -1 & -1 & -1 \end{bmatrix}$$

$$A = \begin{bmatrix} 2 & 3 & -1 & 9 \\ 0 & -1 & 3 & 9 \\ 0 & -11 & 1 & -29 \end{bmatrix}$$

$$A = \begin{bmatrix} 2 & 3 & -1 & 9 \\ 0 & -1 & 1 & -29 \end{bmatrix}$$

$$A = \begin{bmatrix} 2 & 3 & -1 & 9 \\ 0 & -1 & 1 & -29 \end{bmatrix}$$

$$A = \begin{bmatrix} 2 & 3 & -1 & 9 \\ 0 & -1 & 1 & -29 \end{bmatrix}$$

$$A = \begin{bmatrix} 2 & 3 & -1 & 9 \\ 0 & -1 & 1 & -29 \end{bmatrix}$$

$$A = \begin{bmatrix} 2 & 3 & -1 & 9 \\ 0 & -1 & 1 & -29 \end{bmatrix}$$

$$A = \begin{bmatrix} 2 & 3 & -1 & 9 \\ 0 & -1 & 3 & 9 \\ 0 & 0 & -32 & -128 \end{bmatrix}$$

$$A = \begin{bmatrix} 2 & 3 & -1 & 9 \\ 0 & -1 & 3 & 9 \\ 0 & 0 & -32 & -128 \end{bmatrix}$$

$$\rho(A) = 3$$

 $e(A_1B) = 3$
 $e(A) = \rho(A_1B) = 0 = 3$

The system is consistent and that Origine Soln.

$$-32 z = -128$$

$$z = \frac{+128}{+32}$$

$$\overline{z} = 4$$

-ly +3(z) = 9 -14 +3(1)=9 -19+12=9 -1y = 9 - 122x +3y-1z = 9 4 2x +3(3)-1(4)=9 22+9-4=9 2x = 9-9+4 1) x+y+z=6 2x+3y+2 =11 $A = \begin{bmatrix} 1 & 1 & 1 \\ 1 & 2 & -2 \\ 2 & 3 & 1 \end{bmatrix}, x = \begin{bmatrix} 3 \\ 7 \\ 7 \\ 7 \end{bmatrix}, B = \begin{bmatrix} 6 \\ -3 \\ 1 \end{bmatrix}$

e (A) = 3 . (W) e (A) = 3 e(A) = 8(A1B)=3 The system is consistent and has Onique Solution 521-22=8H (0 mul. 21+y+x=6 x-21-4=6 25=6 2=6+25

122317.

Finding the rectord Values and region Vector The Characteristic agn In-AI =0 In other words Fas. 2x2 matrix CE 12-51+5 =0 where 3, - Time of the Matie S = 101. Fax 2x3 Matrix CE -> 23-52+51-53=0 S, - Trace of the Matrix. See sum of the minors of the main diagonals elements of A. 83 =/A/. To Find the Eigen Values Find the co. To find Eggen vector (A-NI)x=0 cohere X \$ 0. 75+J= X Tieter!

To find the roots: 09:0 12+91+4=0 (A+2) (A+2)=0 1=-2,-2. eg: 3 . 212+41+4=0. ax2 + bx + c=0 7=-b+ Vb2-4ac = -4± \-16 eg: 13+12+21-4=0 x2+22+4=0.

$$A = -2 \pm \sqrt{4-46}(4)$$

$$= -2 \pm \sqrt{4-16}$$

$$= -2 \pm \sqrt{-12}$$

$$= -2 \pm 2\sqrt{3} = + \sqrt{4+6}/2$$

$$\lambda = -1 \pm \sqrt{3} + \sqrt{2}$$

$$\lambda_1 = -1 + \sqrt{3} + \sqrt{2}$$

$$\lambda_2 = -1 + \sqrt{3} + \sqrt{2}$$

$$\lambda_3 = -1 + \sqrt{3} + \sqrt{2}$$

$$\lambda_4 = -1 + \sqrt{3} + \sqrt{2}$$

$$\lambda_4 = -1 + \sqrt{3} + \sqrt{2}$$

$$\lambda_5 = -1 + \sqrt{3} + \sqrt{2}$$

$$\lambda_6 = -1 + \sqrt{3} + \sqrt{2}$$

$$\lambda_7 = -1 + \sqrt{2} + \sqrt{2}$$

$$\lambda_7 = -1 + \sqrt{$$

The characteristic eg? of A is to-AI/=0

21214120-

ie, 13-812+51-5=0

Si = Trace of A = 2+3+2

where

Sz = Sum of the minors of the main diagonale élément 10, A. $= \frac{3}{2} \frac{1}{2} + \frac{1}{1} \frac{2}{2} + \frac{1}{1} \frac{2}{3} \frac{2}{3} = \frac{1}{1} \frac{2}{3}$ $= \frac{1}{2} \frac{2}{1} \frac{1}{1}$ $= \frac{1}{2} \frac{2}{1} \frac{1}{1} \frac{1}{1}$ $= \frac{1}{2} \frac{1}{2} \frac{1}{1} \frac{$ = 2(4)-2(1)+1(-1)=50 The characteristic con is 13-122 til 1- 5 =0 gr + grc To find the Sigen Wilnes . 10 -6 5 Lo

The Now Eigen Values are

$$[A=1]$$
, $[A_2=1]$, $[A_3=F]$

To find the stated vectors.

 $A=AT/X=0$, when $x \neq 0$.

ie,

 $\begin{bmatrix} 2-\lambda & 2 & 1 \\ 1 & 3-\lambda & 1 \\ 1 & 2 & 2-\lambda \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix} = 0$
 $x_1+2x_2+x_3=0$
 $x_1+2x_2+x_3=0$

Put $x_1=0$
 $2x_2=x_3$
 $x_1=\begin{bmatrix} 0 \\ 1 \end{bmatrix}$

Case(ii) $\lambda=1$

Put $x_2=0$
 $x_1+x_3=0$
 $x_1=x_3$
 $x_1=x_3$
 $x_1=x_3$
 $x_1=x_3$
 $x_2=x_3$
 $x_1=x_3$
 $x_2=x_3$
 $x_1=x_3$
 $x_2=x_3$
 $x_1=x_3$
 $x_2=x_3$
 $x_1=x_3$

Case (iii) A= 5 $\begin{bmatrix} -3 & 2 & 1 \\ 1 & -2 & 1 \\ 1 & 2 & -3 \end{bmatrix} \begin{bmatrix} 2 & 1 \\ 2 & 2 \\ 2 & 3 \end{bmatrix} = 0$ $\frac{\chi_1}{6^{-2}} = \frac{-\chi_2}{-3-1} = \frac{\chi_3}{2+2}$ $\frac{\chi_1}{4} = \frac{\chi_2}{4} = \frac{\chi_3}{4}$ $\frac{\chi_1}{4} = \frac{\chi_2}{4} = \frac{\chi_3}{4}$ The eigen Vactors Voaresponding to the Eigen values d=1,1,5.

are $X_1=\begin{bmatrix}0\\1\\2\end{bmatrix}$, $X_2=\begin{bmatrix}0\\1\end{bmatrix}$, $X_3=\begin{bmatrix}1\\1\end{bmatrix}$. respectively. Find the Eigen values and light rectors of the Materix:

Soln: Let The characteristic con of A is (A-TI)=0 i,e, 13-5,12+521-53=01. where, Si = Trace & A. 2 3+2+3 = 8.. Sz: Sur of the minare of the main diagonals dement of A. $= \begin{bmatrix} 2 - 1 \\ -1 & 3 \end{bmatrix} + \begin{bmatrix} 3 & 0 \\ 0 & 3 \end{bmatrix} + \begin{bmatrix} 3 & 1 \\ -1 & 2 \end{bmatrix}.$.=(6-1)+(9-0)+(6-D = 3(6-1) +1 (-3+0)+0 minutary = 15-3 = 12.

To donataite es il (2-3) =0 The Eigen values are :

To find the light vectors
$$|A-AI| = 0 \quad \text{where } x \neq 0$$

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$$|A-AI| = 0 \quad \text{where } x \neq 0$$

$$|A-$$

$$x_{1} = \begin{bmatrix} 1 \\ 2 \\ 1 \end{bmatrix}$$

$$x_{2} = x$$

$$\begin{bmatrix} 3-4 & -1 & 0 \\ -1 & 2-4 & -1 \\ 6 & -1 & 3-4 \end{bmatrix} \begin{bmatrix} x_{1} \\ x_{2} \\ x_{3} \end{bmatrix} = 0$$

$$\begin{cases} 1 + -1 & 0 \\ -1 & -2 & -1 \\ 0 & -1 & -1 \end{bmatrix} \begin{bmatrix} x_{1} \\ x_{2} \\ x_{3} \end{bmatrix} = 0$$

$$\begin{cases} x_{1} - x_{2} = 0 \\ -x_{1} - 2x_{2} - x_{3} = 0 \\ -x_{2} - x_{3} = 0 \end{cases}$$

$$\begin{cases} -x_{1} = -2x_{2} = -\frac{x_{3}}{1-0} \\ -\frac{x_{1}}{1-0} = -\frac{2x_{2}}{1-0} = -\frac{x_{3}}{1-0} \end{cases}$$

$$\begin{cases} -x_{1} = -2x_{2} = -\frac{x_{3}}{1-0} \\ -\frac{x_{1}}{1-0} = -\frac{x_{2}}{1-0} = -\frac{x_{3}}{1-0} \end{cases}$$

$$\begin{cases} 3-3 & -1 & 0 \\ -1 & 2-3 & -1 \\ 0 & -1 & 3-3 \end{cases} \begin{bmatrix} x_{1} \\ x_{2} \\ x_{3} \end{bmatrix} = 0$$

$$\begin{cases} 3-3 & -1 & 0 \\ -1 & 2-3 & -1 \\ 0 & -1 & 3-3 \end{cases}$$

Gadi)
$$\lambda = 1$$
 $\begin{bmatrix} 2-1 & 1 & 1 \\ 0 & 1-1 & 0 \\ 1 & 1 & 2-1 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix} = 0$
 $\begin{bmatrix} x_1 + x_2 + x_3 = 0 \\ x_1 + x_2 + x_3 = 0 \end{bmatrix}$
 $\begin{bmatrix} x_1 + x_2 + x_3 = 0 \\ x_2 + x_3 = 0 \end{bmatrix}$
 $\begin{bmatrix} x_1 + x_2 + x_3 = 0 \\ x_2 + x_3 = 0 \end{bmatrix}$
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 $\begin{bmatrix} x_1 + x_2 + x_3 = 0 \\ x_3 + x_3 = 0 \end{bmatrix}$

$$-x_1 + x_2 + x_3 = 0$$
 $-2x_2 = 0$
 $x_1 + x_2 - x_3 = 0$

$$\frac{71}{-1-1} = \frac{-3}{1-1} = \frac{3}{-1-1}$$

$$\frac{\chi_1}{-2} = \frac{\chi_2}{0} = \frac{\chi_3}{-2}$$

$$x_2 = \begin{bmatrix} -2\\ 0\\ -2 \end{bmatrix}$$

case:3 7=1

consider

$$\frac{\chi_1}{-1} = \frac{\chi_3}{1}$$

$$X_3 = \begin{bmatrix} -1 \\ 0 \\ 1 \end{bmatrix}$$

The Eigen values and Eigen vectors $\lambda_1 = 1$, $\lambda_2 = 3$, $\lambda_3 = 1$ and vectors

$$x_1 = \begin{bmatrix} 0 \\ -1 \end{bmatrix}, x_2 = \begin{bmatrix} -1 \\ 2 \end{bmatrix}, x_3 = \begin{bmatrix} -1 \\ 0 \end{bmatrix}$$

Application of Matri

Physical while application:

1) Electrical Circuits, Condon mechanical optics.

ii) calculation of battery power outputs, Conversion of electrical energy to Useful energy of runtors Properties of

ii) isolving posoblems of Kuichoff's law (voltage 90)

2) computer related applications.

Paojection 37 37 umage to 27, Oceating qualistic somening motion;

i) sokastie mati

io, used in nanking of web pages in Google seasch.

Matrixus Calculus!

Generalization of anatical notions like exponenties to higher Domenions.

(a) Coding are entaupting the musage. Water is all

1) Seismic servey of who it (8 ii) to plot graphs,

ii) statics and do scientific studies iv) sobotic and automortions ?) Used in Gaaph theory, qualater Mehan Computer Graphics, Solving Lavear Equato Cytrography. Properties of Eigen values: Sum of the Eigen Values is equal to Trace of the Matrix. 2) Protect of the Eigen Volues -[A). 3) 41 1 is the Eigen Values of A then is the Eigen value of A? If I is not liger Value the of A the Am is the eigen value of A 5) 91 1 is the eigen Value of A other k & is the eigen value of kiA. A and AT have the warne eigen values. 7) The eigen Values of a real Symmetric Mateux is all real number.

The eigen values of a triangular Matrin

are its elements in the main

Dimilar Matricus have othe Same Eigen introquipas 1413+18il= 3+1+2an If the Eigen values of a 3x3 materix 1, 3 and 1 Find the determinant of [A] without expending. Resoluct 101 the Eign Values = 191. 1x3x1 = (A) Te, 1/2/3=la) WET:

ie, A=BAB.

Proporties of Eigen Vectors-

1) Eigen vectors of a Hatrin A us not Unique

2) Two Eigen vectors X1 X2 are called

Outhogonal St x1 x2 = 0

3) Top. 1; 12 In vase edistirct Eigen Values of a nxn material other the Consusponding Eigen Vectors X, 1×2.... Xn. fram a climarally indespendent set.

30/c/14 Equations:

Relations between arithment and roots.

2 Equations with nationals Co.

and invationals scots.

Equations usith nationals Co- Efficient and invational isoots will roccurs in pairs. => Let +(x)=0 be a equation and Suppose that A+VD is a root of the Equation where att are national and Vb is resational, then a-Vb is also a root.

Problems:

Solve the oquation : x4-6x3+4x2+8x-8=0

Given that one of the root is

1-55

Soln!

we know that if 1-50 is a voot then 1+15 is also an iroot.

Therefore, The factors are (x-(1-16)][2-145) (x+x/6) (x + x) =0

n2-x(1+56)-(1-56)x+(1-56)(1+56)=0 x = x[1+5F+1-5F]+[1-F)=0 $\chi^2 - 2\chi - 4 = 0$

1-50 21+56

Sum of the roots = 1-55. +1+15 = d

Product of the acots = (1-VA)(1+VA)=1-1 =+

x2 - [Sum of the roots] n + product of the roots =0 $\chi^2 - 2x - 4 = 0$.

x4-5x3+4x3+8x-8=0

22-32 + 2

 χ^2 -3n+2 is also a factor. ·· x4-523+4x2+82-8= x2-dx-4)(2-3x [a - Ci-13][a- Ci+va)] [(x-2)(x-1)]=0

1-55) 1+55 /2; 1 as the add of the egn. or (A - va) (all shorts in) (= the eqn 323- 232+ 12x-70=0 having (3+5) as a soot. 9/ (3+(-5) is a root tuin (8=5-5) is also a soot. The a El Sum of the 200ts = 3+5/5. \$3 7/5 Product of the roots = (3+ 55) (3-5-5) = 9-5 x2-[Sum of the roots] x + product of thereots = c x2-6x+14=0. 323-23x2+72x -70=0 3x -23x +72x -70 323-1822+422

-522+30x+70

3x3-23x2+72x-70=0 => (x2-6x+14) (3x-5)=0 =) (37-15), (8-15), 7/3 are the acou of the above egni-5) Find the egn whose goots are. 43, 6+2F1. Journ & solo Sant de la The noots are 46, -453, 5+25, 5-257 (16x3) Sum of the 200ts = 453 -453 = 0 Product of the soots = (4/3) (-4/3) =-48. x2- [Sum of the goots]x + product of g=0 $\chi^2 - 78 = 0. -200$ The factor is 5+25, 5-25-1. Sum of the noots = 5+25-1+5-25 =0

Product of the 200ts = (5+25) (5-25) of - Eum of the goots Ix + product of the soots =0 x-10x+29=0 → ® 2-The egn is a store (5) 5 5 13x29 (2-48) (x2-10x+29) =0 (5-29) x = 10x + 29x - 48x2 + 480x 7392=0 x4-10x3-19x2+480x-1392=0. Find the egn with eastional Co-efficients whose mosts dere It 5 A and F- J-1. SIn? 0= Hotxod The Goods are then - In 1 d + 15 J-1 1 - 15 J-1 , 15 - Jtraining The factor is (1-)26 Repations before 1 1 1 1 1 1 1 1 1 1 Sum of the 200ts = 1+ 55 + 1-55 1+25 Product 101 the roots = (1+B5-1) (1-B5-1) 2 - [Sum of the noots]x+ Product & goo x - 2x +26=0, -30.

The factor is now on you to about Sum of the Hoots = 5-5-1+5+5-1. Product of the roots = (5-V-1) (5+F) 22- [Sum of the Boots]x + Product of x-10x+26=0,->@ $x^{2}-10x^{3}+26x^{2}-2x^{3}+20x^{2}-52x+26x^{2}$ -260x+676 =0 x4-12x3+72x2-312x+676=0. Relations between goots and lo efficients of egn! + it at + = stook wit formul Let the equ be xn+P1 xn-1+P2 xn-2 + --+ Pn-12+Pn=0. Harther Egn har roots al, 1 de 1 -- . . An.

thin Zx = Sum of the goots = Corp. P. -P Ex, x,= Sum of the the goots 4= (1) 72-1 taken & atatime 7 202 Zx, x, x, = Sum of the the adots 7=(1)3P3-R apr taken 3 at a time friage... on = Product of the about = (1) Pr. If K, B, & are the goots of the x3+px2+ 9x+r=0., express the Value 2 a2, 21, 2 2B 1+p+2= (-1)P=P

The Given egn. x3+px2+@x+R=0 The goots are x, B, 2. 2x= 2+18+ D= -P. Lap= xB+B 2+ x R = Q WBV =- PE 1) Ex 19 En=x+82+ 8 (x78+8)2=x2+82+8+2@B+2xy+282, -: = (x+B+y) = 2aB -2B9-2x8. = (-17)2-2(AB+BY+KD) $| = p^2 = 2(a)$. VIII) Zik = UB+dd + Br

iii) & L in ZxB 2 a 3 = a B + x 2 + B x + B 2 + 8 x + 1 B-= apfe+B]+av[a+v]+Bv[s+v] = 2B [2+13+7-3] + av[2+v+B-B]+. BP[3+2+2-2] = AB[A+B+v]-2BV+QV[Q+B+v]-KBV + B7 [x+B+ y] - KBY = [x+B+7] [xB+xx+Bx] -3xBx = -PQ+3R. 2. If a Bir be the goots of the egn x3-px2+Qx-R=0. Thin find. i) zia, ziz , ziz , ziz , zix s.

K+13+ N=60(7)=P April 1 + 2/2 - (4) a = 0 ... NBV = (-1)3 FR = R. = 2 2 2 2 = (atpty) - 2xp-2xx-2px = (x+B+v)=-2[= p+av+pv] ii) 2 + = 2+ 1 + 1 = 1 + 1 + 1 / BY $= \frac{y + B + x}{a p y}$ $= \frac{y}{R}$

=[aB+Bv+av]-2(aB(Bv)-2(aB)(av) = [\(\begin{align} | 3+ \beta \beta \end{align} = \begin{align} | \(\alpha \beta \end{align} + \beta \alpha \beta \end{align} = \beta \alpha \beta = [xp+ pv+ xv]2-2[B(xpv)+x(xpv]+x(xp) Q = 2 [apr) [at p+v]] $= (\alpha + \beta + \nu)^{3}$ (a+b+c) = a+b+c3 - 3[(a+b+c) (ab+bc+ &] (x+B+1)= 23+B3+23-3 [44B+8] @B+2B+27+34B7 (4+13+8)3 - 3 [PQ] +3R $= p^3 - 3pa + 3pa$ = P3-3 PQ +3e. (4) (4-) 5 & (3) + (4)

be the aoots of the egn x3+px2+Qx+R=0 find the Value of (B+1) + (2+x2) + (x2+x)2 X+B+V=(1)p=-P xB+B>+Px=(-1)2Q=Q 280=(1)3(2)=-R: B++2)+ (2+2) (2+2) (2+1) = (2+8+2-2-2) + (x+8+3-13)+(x+8+3-3)

BY

AB = (x2+B2+2) - x2 + (x2+2) B2 (223) 2 BY + XY XX XX XX XX XX = (2+8+8) [1 + 1 + 1] - 2 + 1 + 1 | BV XV aB | = (x+13+v)2-2(xB+13+xV) [x+13+v] [x3+13+x3] - [x3+13+x3] [x3+13+x] $= \left[(P)^2 - 2Q \right] \left(\frac{-P}{-R} \right) - \int_{-R}^{1} (x^3 + B^3 + y^3)$ Consider: 23+3+2=(ac+3+2)3+3x |32-3/2+8+2) (ap+8+2) =(-P)3+3(-P)(Q) = (-P) # 3 R + 3 PQ.

be the roots of x3+px2+px+12=0 find the 2 + 1 = 2 + 1 + 3 + 1 + 3 + 1 $= \lambda^2 + \beta^2 + y^2 + 3$. 213+79-2(2B+B+18+14x)+3 C-p)= 2(a)+> p2-2 @)+3

Reaparal Equation Conditions: Let the egn be. x+p,x++2xn-2+...+2=0.

1) If the Co-efficients have all like Sign. The (4) is a root.

1) (1) is a second then (x+1) is a factor.

1) 4) the Co-efficients of the itum equi * distance from the first and the last. have opposite sign. Then (+1) is a 200t. then (2-1) is a lactor.

(i) If the equation is of odd degree the (x-1) is a factor.

(ii) If the equation is of even degree than Galternah tor-) thr (2-1) is a factor.

Problems: find the acosts of the equation. x +1x1+3x3+3x2+4x+1=0. (6+1) Sofn All the Co-efficients are positive 1-D is the goot. (ie) Geti) is a factor. x +4x1+3x3+3x2+4x+1=0, 15+x4+3x4+3x4+3x+3x+3x+x+1=0 x9(x+1)+3=3(x+1)+3x(x+1)+(x+1)=0 (x+1) (x4+3x3+3x+1)=0 (x+1) x2-1 (x+1) => x=-1 is a abot ... The eqn is dividide by 2 $\frac{x^{2}}{x^{2}}$ $\frac{x^{4}}{x^{2}}$ $\frac{(x^{4} + 3x^{3} + 3x + 1)}{x^{2}}$ $\frac{7}{x^{2}}$ $\frac{7}{x^{2}}$ [x2+ 3x+2] =0. $\left(\begin{array}{c} 2 \\ \chi + 1 \\ \chi + 3 \\ \chi$ Let put x+1=2 n+2=2 (u+x)2=22

$$(x + \frac{1}{\sqrt{2}}) = x^{2}$$

$$x^{2} + 2x^{2} + \frac{1}{x^{2}} = x^{2}$$

$$x^{2} + 2x^{2} + \frac{1}{x^{2}} = x^{2}$$

$$x^{2} + 2x + \frac$$

x= (-3±517)± √(-3±517)2-4(2)(2) 91 = -3± (F3 ± (F3± (F1)2cere the goots of the above equation <u>53/n!</u> Therefore ox =1 us a goot. 6x 5-x4-43x3+43x2+x-6=0 (6x, 5-6x + Fx + Fx + - Fx 3 - 38 x 3+ 38 x + Fx 2 = 10 6x#(x-1)+5x3(x-1)=38x2(x-1)+15x(x-1) (x-1) (6x++5x3-38x2+5x+6)=0 (21-1)=7 x=1 uita 200t. The eqn is divide by of. 16x + 5x 3 - 38x2 + 5x + 57 =0

avel put x = 7. x2-なx+1=の1×18-(101)3 $91 = +(\frac{5}{2}) + \sqrt{\frac{25}{4}} + 1(1)(1)$ $= \frac{7}{5} \pm \frac{3}{2} = \frac{8}{2 \times 2} \cdot \frac{2}{2 \times 2}$ $= \frac{2}{7} \pm \frac{3}{2} \cdot \frac{2}{2 \times 2} \cdot \frac{2}{2 \times 2}$ Can(ii) put z= % 27+10/21-10 The required roots are, x=1,2, 2, 3, -3. Solve: 62 -37x5+66x4-56x2+35x6=0. Seni(x2-1) is the factor

6x 6-6-3525+35x + 56x 4-56x2 =0 6(x6-1) -35 x(x1-1) +56x2(x2-1) =0 Consider. $\chi^{6}-1=(\chi^{2})^{8}-1^{3}$ = (x2+1) (x1+x2+1). 24-1 = (x2)2-12 $=(x^2+1)(x^2+1)$ 6[(x2-1)[x4+x2+1)]-35x[(x2+1)(x2-1) + 76x2/22-1) =0 (x2-1) /6(x4+x2+1)-35x(x2+1)+56x2=0 6x46x2+6 -35x3+35x+56x2=2. 6x4-35x3+60x2=360+6=0. $-\frac{1}{x^2}\frac{6x^4}{x^2} - \frac{35x^3}{x^2} + \frac{6ax^2}{1x^2} + \frac{6}{x^2} = 0$ 6n²-35x 460+6 =0. 6 (x2+/22) - 35x+60=0. Let x = n+ note 2. 72 = x + 12

6(2-2) -35x+6d=0. 6x2-35x-12+60=0 6x4-35x3+62x2-35x+6=0. $- x^{2} \frac{6x^{4}}{x^{2}} - \frac{35x^{3}}{x^{2}} + \frac{62x^{2}}{x^{2}} - \frac{35x}{x^{2}} + \frac{6}{x^{2}} = 0$ 6x-35x+62-35+6=0 6(x+1/2) -35(x+1/2)+62=0. Let z= x+2 22-2= x2+2 6(22-2) = 35(2) +6Q=0 $6x^2-12-3hx+62=0$ 200×6 62-352+50=0. 7= 35 + \(\frac{1225-466}{260}\) = 35± \(\frac{1225-1200}{3d}\) = 3 5 ± 525 =35± 10 $Z = \frac{40}{12} \times \frac{30}{12}$ 7 = 3, 5/2

$$\begin{array}{llll}
\omega \times T & & & & & \\
\chi = \chi + \frac{1}{\chi} & & & \\
\chi = \chi^{2} + 1 & = 0 & \\
2 - \chi + 1 & = 0 & \\
2 - \chi^{2} - \frac{10}{3} & = \frac{10}{3} & = \frac{10}{3} \\
\chi = \frac{10}{3} + \sqrt{\frac{100}{3}} - 4(1)(1) & & \\
\chi = \frac{10}{3} + \sqrt{\frac{64}{9}} & & \\
\chi = \frac{18}{3} \times 1 & = \frac{12}{62}, \frac{2}{3} \times \frac{1}{2} & = \frac{2}{6} \\
\chi = \frac{3}{3} \times \frac{1}{3} \cdot \sqrt{\frac{1}{3}} \cdot \sqrt{\frac{1}} \cdot \sqrt{\frac{1}{3}} \cdot \sqrt{\frac{1}{3}} \cdot \sqrt{\frac{1}{3}} \cdot \sqrt{\frac{1}} \cdot \sqrt{\frac{1}{3}} \cdot \sqrt{\frac{1}{3}} \cdot \sqrt{\frac{1}{3}} \cdot$$

X= 3+ (25+(4)(1)(1)

= 7/27 59

$$\frac{1}{2} = \frac{1}{2} \cdot \frac{1}{2}$$
The arguind roots $\frac{1}{2} \cdot \frac{1}{2} \cdot \frac{1}{2}$.

The arguind roots $\frac{1}{2} \cdot \frac{1}{2} \cdot \frac{1}{2} \cdot \frac{1}{2}$.

$$\frac{1}{2} \cdot \frac{1}{2} \cdot \frac{1}{2}$$
The arguind roots $\frac{1}{2} \cdot \frac{1}{2} \cdot \frac{1}{2} \cdot \frac{1}{2}$.

$$\frac{1}{2} \cdot \frac{1}{2} \cdot \frac{1}{2} \cdot \frac{1}{2}$$

$$\frac{1}{2} \cdot \frac{1}{2} \cdot \frac{1}{2} \cdot \frac{1}{2}$$

$$\frac{1}{2} \cdot \frac{1}{2} \cdot \frac{1}{2} \cdot \frac{1}{2}$$
Consisdu:
$$\frac{1}{2} \cdot \frac{1}{2} \cdot \frac{1}{2} \cdot \frac{1}{2}$$

$$\frac{1}{2} \cdot \frac{1$$

$$6x^{4} - 26x^{2} + 37x^{2} - 26x + 6 = 0$$

$$6x^{4} - 26x^{3} + 37x^{2} - 26x + 6 = 0$$

$$6x^{2} - 26x + 37 - 26 + 6 = 0$$

$$6(x^{2} + \frac{1}{x^{2}}) - 26(x + \frac{1}{x}) + 37 = 0$$

$$6(x^{2} + \frac{1}{x^{2}}) - 26(x + \frac{1}{x}) + 37 = 0$$

$$6x^{2} - 26x + \frac{1}{x^{2}}$$

$$x^{2} - 2 = x^{2} + \frac{1}{x^{2}}$$

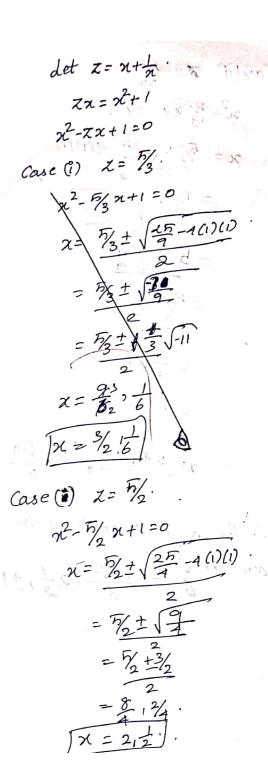
$$6x^{2} - 12 - 26x + 37 = 0$$

$$6x^{2} - 26x + 25 = 0$$

$$7 = 26x + \sqrt{226} + 46(2x)$$

$$7 = 26x + \sqrt{26}$$

$$7 =$$



Carelii) $\vec{x} = \frac{7}{3}$, x + 1 = 0. $x^2 - \frac{7}{3}x + 1 = 0$. $x = \frac{5}{3} \pm \sqrt{\frac{2\pi}{9}} - 4(1)(1)$ $= \frac{7}{3} \pm \sqrt{\frac{2\pi}{9}}$ $= \frac{7}{3} \pm \sqrt{\frac{2\pi}{9}}$ $= \frac{7}{3} \pm \sqrt{\frac{11}{9}}$ $= \frac{7}{3} \pm \sqrt{\frac{11}{9}}$ $= \frac{7}{3} \pm \sqrt{\frac{11}{9}}$

.'. The required roots of the eqn are $\frac{5+\sqrt{-11}}{6}$, $\frac{5-\sqrt{-11}}{6}$, $\frac{2}{2}$, $\frac{1}{2}$, $\frac{1}{2}$.

Б) volve x10-3x8+ Бх6- Бхд +3x2-1=0 x10-3x8+5x6-5x+3x2-1=0 (2-1) is a factor x10-x8-2x8+2x6+3x6-3x4-2x4+2x2+xx2-1=0 n8(22-1)-2n6(22-1)+3x4(22-1)-22(22-1)+62-1)ec (x2-1) (x8-2x6+3x4-2x2+1)=0. $\chi^2-1 =) \chi = \pm 1$ is a root. The egn dirick by not. 28-276+324-22+1 =0. $\frac{2x^{6}}{x^{4}} - \frac{2x^{6}}{x^{4}} + \frac{3x}{x^{4}} - \frac{2x^{2}}{x^{4}} + \frac{1}{x^{4}} = 0$ $x^4 - 2x^2 + 3 - \frac{2}{x^2} + \frac{1}{x^4} = 0$ (x1+1)-2(n2+1)+3=0. 7: x2+1/2 1 = 7 = 29+1 == At the state of th

37/14

Differential Calculus:

And its Application:

Differentiation and deseratives of Simple functions.

The vate of Change in y with suspect to or can be measured Using the derivative &.

dy in physics velocity is equal

The method of finding the delivative of a function is called differentiation.

Basic diffentiation formula!

- $\int \frac{d}{dx} c = 0$
- a) $\frac{d}{dx} x^n = nx^{n-1}$
- 3) de eax = aex.
- A) d sinax = a Cosax.

- 5) d los an = -a sinax
- 6) de tanax = a bot sec2ax.
- +) dx Sec an = a Socan tahax.
- 8) de Cosecan =a associan Cotan.
- 9) d. cotax = -a cosec² ax . ex = ex
- 10) d sin-1x = 1 -x2
- 11) de Cos'x = -1 Secon
- 12) $\frac{d}{dx} + \tan^2 x = \frac{1}{1+x^2}$
- 13) d (u±v)=du+dv.
- 19) d (uv) = udv + vdu.
- 15) du (4) = vu'-uv'.
- 16) dx (u= Cdu=cu!

the dervative of the following: d [fo 60 s 2x + 6 sin 2x + 7 sec 4 x]. 1) dx [4x3] d [= Cps 2xi +6 Sin 2xi +7 Sec 4x] = 5(-2602x)+ A = 4 (2) 3-1] =-108 Cos2x + 12 Cos2x + 28 Sec + 12 tan dy [4x3+5 sinx7. find the durvative of the following: d [4x3+5 Sinx] = 4(3x3-1)+5 Cosx. d [4 lot Fx+ btcm3x] =- 20 losec Fx+ 18 bec 3x D. d [4 6t Fox+6+an3x] = 12x2+56sx. 2) d [3+7/ec8x ++ cosec x] = 0+ + [8 sec8x tan8x] d [e79+8053x] 3) dx [eTx+8cos3x] = 7e7x €8[3 lin 3x] d [8etx+9x9+608x]=8(1etx+9(0x2-1)+6(8 ex)
=32etx+81x8+48ex. = Te -248 in 3x. 4) d [5+x6+ COS 5x+7e47] d [865 x + 4 Sir / x] = 8 = +4 \ \(\frac{1}{1-x^2} + 4 \ \frac{1}{1-x^2} d (n+x+cos nx+te) =: 0+6x = 5 Sin fx +74e4x. = 6x15-5,513,6x+28eA7 = -4 OS = -

to	dn Louis	A 22 18 9 2 25 5.	and h
Price's	= 4 tos=	tx = 4 los 4 x	+-1
etnet kn	1 4 105 - 4 105 - 1 + 70 10 10 10 10 10 10 10 10 10 10 10 10 10	wis .	1+22
고)	privally we	durvative of	WH . 1 200
x E . d.	Some = X	PERIOHA + KR to	1. 1. 141
Pivad &	wink = Sinx es (ex-le	Cos x2 (2x).	NP 1
2) 0	n (n+12)(e7-le	المواد	7 1
alf.	x + trut2) (ex-1) (2-1-)	
2 134 (FA	ALL LEY LES A	- (e +togst) (25(+1)
3 P + 1	\$1844958 = [11	opalabtate 1	J 6
H.A.	* = & Alase	Fx 1 7	
	**************************************	1 2 sore ()	D CA
	Sr-N	• • •	
	Frie :		
	JA-17		

$$y = x + los x.$$

$$\frac{dy}{dx} = 1 - ls uny$$

$$\frac{d^2y}{dx^2} = -los x.$$

$$\frac{dy}{dx} = x(-e^{-x}) + e^{-x}(-1) + b(e^{x}) + e^{x}.$$

$$= -xe^{-x} + e^{-x} + be^{x} + e^{-x}(-1) + (e^{-x}) + b(e^{x}) + o(e^{x}) + o(e^$$

4) y=ex Sin PT y=-24, +2y=0 . Wealth y = dy = ex Cosx + Sinx ex. 42 = d29 = ex(-sinx)+(0sxe7+Sinxex+Cosxex =- Junx ex + Cosxex + Junxex + Kosxex 42-24, +24= 2 Cosxe - 2 Cex cosx + Sinx cx + 2ex Sinx = 265xex-2ex 65x-256xe7+2ex 50, 16x 20 p 1 + x = t (cox 1 ling i If y = eax subx. PT y = 2ay + (2+16) y =0 y= du= ear (blos br) + Sibx agax = ear blosbat Sinbace 42 dey = eax (-b2 Sinbx) + blosbx ae x + Sinbx aex

or that that blosbx =-bear Subx + blosbx ac + Subx ac taear b Cosba 92-204, +(2+b2)y= -b20x 820 bx + b60s bx dex + Sin bix a/eax + a cax b/cos bin - 2acax b Cosbx - 2a sibbxaeax (1) 1) - (1) + a ead sin by + b ead sin by

PT x3y3 -2xy2 +24,=0 y1=dy=3x2-0 =3x2 42= dry = 3(22) = 6x y3 = d3y = 6(1) = 6 x8y3-2xy2+2y1= x8(6x)+213x2) = 6x2-12x2+6x2. e 65x + Sina? 4) y=(x+ fx2-1) m +1 (x2-1) y2+xy,-my=0. y,=dy = m (x+ 1x2-1) m-1 (1+1/2 (x2-1)-1/2) (2x) m(x+(x-1)2) m-1 (1+ /x-1/2) = m (x+ (x2-1)/2) m-1 [1+ 1/(x2-1)/2] y= day = m (m-1) (n+(2-1)/2) (1+ 1/2 (x2-1)/2) (1+ (2-1) /2)+m (x+(2+1)/2)m-1 [(x2-1)/2(1)-n/2(x2-15/2 2x (x2-1)y2 + xy = my=0.

2 in (100-12

```
application to apprential.
           triding the auce
           radius of awarture.
             radius of huntine P = [1+4] 7/2
            where y; and y; dif
         Find the addition of auvature
         parabola
                   2yy_1 = 4a
y_1 = \frac{4a}{2y} = \frac{2a}{y}
y_1(4a) = \frac{2a}{a} = 2
                  y2 = -2a dy
                  y_{2} = \frac{-2a}{y^{2}} y_{1}
                 y_2 = \frac{-2a}{y^2} \times \frac{2a}{y}
y_2 = \frac{-2a}{y} \times \frac{2a}{y}
                 y_{1} = -\frac{4a^{2}}{y^{3}} =
                 y_{a}^{2}(9,a) = -\frac{4a^{2}}{a^{5}} = -\frac{4}{a}
Radius of aurature e= [1+y,2] 1/2
```

= [+4] 1/2 Radius cannot le in negative padius of $e = \frac{a5/2}{1}$ $(y^2)(x^2)$ 2) Find the radius of aurature point (1, 1) on the care vx+vy=1. Given $\sqrt{x}+\sqrt{y}=1$ at $(\frac{1}{4},\frac{1}{4})$ i.e. $x^{\frac{1}{5}}+y^{\frac{1}{5}}=1$ $\sqrt{x}^{\frac{1}{5}}+\sqrt{y}^{\frac{1}{5}}y_{1}=0$. $y_1 = -\frac{1}{2}x^{-1/2} = \frac{-y'/2}{2x'/2}$ $y_2 = \frac{-y'/2}{2x'/2}$ $y_3 = \frac{-y'/2}{2x}$ y, (4, 4) = -(4)/2 = -1 $y_{e} = -\left[\frac{1}{2}\left(-\frac{1}{2}y^{-1/2}\right) - y_{1} - y^{-1/2}\left(-\frac{1}{2}\right)x^{-1/2}\right]$ $=\frac{-\left[\frac{1}{4}\right]^{1/2}\left(\frac{1}{2}\left(\frac{1}{4}\right)^{1/2}\left(\frac{1}{2}\left(\frac{1}{4}\right)^{1/2}\left(\frac{1}{4}\right)^{1/2}\left(\frac{1}{4}\right)^{1/2}\left(\frac{1}{4}\right)^{1/2}\right]}{\frac{1}{4}}$ $=\frac{-1/2+1/2}{1/4}=\frac{1}{1/4}=\frac{1}{4}$ $P = \frac{(1+y_1^2)^{3/2}}{1+4} = \frac{(1+(1)^2)^{3/2}}{1+4} = \frac{3/2}{4} = \frac{\sqrt{2}}{2}$

$$y_{1}(1,1) = -\frac{1}{1} = -1$$
 $y_{1}(1,1) = -\frac{1}{1} = -1$
 $y_{2}(1,1) = -\frac{1}{1} = -1$
 $y_{3}(1,1) = -\frac{1}{1} = -1$
 $y_{4}(1,1) = -\frac{1}{1} = -1$

$$y_1 = -\frac{1}{x^2}$$
 $y_2 = -\frac{1}{x^2}$
 $y_3 = \frac{1}{x^2}$
 $y_4 = \frac{1}{x^2}$

$$=\frac{y+y}{x^2}=\frac{2y}{x^2}=2$$

$$= \frac{(1+1)^{3/2}}{2} = \frac{(2)^{3/2}}{2} = \frac{75^{2}}{2} = 52$$

$$y_1(a_1a) = \frac{-3(2)-(a)}{2(a)(a)}$$

$$= \frac{-4a^2}{2a^2}$$

$$y_{2} = \frac{2 \times y \left[-6 \times -2 y y_{1}\right] - \left[-3 \times^{2} - y^{2}\right] 2 \left(x y_{1} + y\right)}{4 \times^{2} y^{2}}$$

$$y_2(a_1a) = 2a^2 \left[-6(a) - 2(a)(-2)\right] - \left[-3(a)^2 - a^2\right]$$

$$= 2\left[a(-2) + a\right].$$

$$= -\frac{4a^3 - 8a^3}{+ 4a^4} = \frac{112a^3}{14a^4} = 30 - \frac{3}{6}$$

$$=\underbrace{\left(1+4\right)^{3/2}}_{-3/2}=\underbrace{\left(\frac{\pi}{3}\right)^{3/2}\alpha}_{3}=\frac{-\pi\sqrt{5}\alpha}{3}$$

a Radius of Questine p = 61th al

F) find the audies of Guarature of the parabolos x=a+2. y= ent. out 7.

x=a+2 y=2a+

dx = 2a+ dy=2a

dt = 2a

$$\frac{dx}{dt} = 2at$$

$$\frac{dy}{dt} = 2a$$

$$y = \frac{d^2y}{dx^2} = \frac{d}{dx} \left(\frac{dy}{dx} \right) \frac{dt}{dx}$$

$$= \frac{d}{dt} \left(\frac{1}{4} \right) \frac{1}{2at}$$

$$= \frac{d}{dt} \left(\frac{1}{4} \right) \frac{1}{2at}$$

$$= \frac{1}{\sqrt{2}} \frac{1}{2at}$$

$$y_{e} = \frac{1}{2at^{3}}$$

$$\varphi = \frac{[1 + (y_1)^{\frac{1}{2}}]^{\frac{3}{2}}}{y_2}$$

$$= \frac{[1 + (y_1)^{\frac{1}{2}}]^{\frac{3}{2}}}{[1 + (y_1)^{\frac{1}{2}}]^{\frac{3}{2}}}$$

$$= \frac{[1 + (y_1)^{\frac{1}{2}}]^{\frac{3}{2}}}{2at}$$

$$\frac{\sqrt{1+\frac{2}{t^2}}}{\sqrt{2at}}$$

$$= -\left[\frac{t^2+1}{t^2}\right]^{3/2} \cdot 2at^3$$

$$= -\left(t^2+1\right)^{3/2} \cdot 2at^3$$

$$= -\left(t^2+1\right)^{3/2} \cdot 2at^3$$

$$= -(t^{2}t)^{\frac{3}{2}} \cdot 2at^{3}$$

$$= -(t^{2}t)^{\frac{3}{2}} \cdot 2at^{3}$$

$$= -(t^{2}t)^{\frac{3}{2}} \cdot 2a$$

$$=-(\xi^2+1)^{3/2}\cdot 2a$$

The radius Cannot be in negative So radlus of auvature @ (241) 1.2a.

find the readles of Curvature at (a,0) on the Curre 213 = 23-23

Given
$$xy^2 = a^3 - x^3$$

$$y^2 = \frac{a^3 - x^3}{x}$$

$$\frac{1}{x^2} = \frac{x(-3x^2) - (a^3 - x^3)}{x^2}$$

$$\frac{x^{2}}{x^{2}} = -2(x - (3x^{3}) + a^{3} + x^{3})$$

$$2yy_1 = -\frac{2x^3 - a^3}{x^2} = -\frac{(2x^3 + a^3)}{x^2}$$

$$y_1 = \frac{-2x^3+a^3}{2yx^2}$$

$$y_{1} = \frac{-2x^{2}+a}{2yx^{2}}$$

$$y_{1}(a_{1}0) = -\frac{2a^{3}+a^{3}}{2(0)x^{3}}$$

$$= \frac{a^{3}}{a} = \frac{a^{3}}{a^{3}}$$

Velocity and Acceleration:

Velocity:

Veloc

ed calegation!

The rate of change of velocity is the Acceleration and its given day acceleration = $\frac{dv}{dt} = \frac{d^2s}{dt^2} = a$.

Note:

- :) Initial Velocity V= ds at time t=0
- ii) Initial acclesiation a = $\frac{d^2s}{dt^2}$ at time t=0.

Problems!

- 1) The distance-time formalls of moving particles & S=2t3+3t2-72t+1 ished
 - 9) Velocity and t=3 sec.
 - ii) Initial velocity -
- (R) Instial acceleration -
- W) vaceleration after 4 Sec.

Ashn!-

Given: S=2t3+3t2-72t+1.

 $V = \frac{dS}{dt} = 6t^2 + 6t - 72$

 $\alpha = \frac{d^2S}{dt^2} = \frac{dv}{dt} = 12t + 6.$

i) V(+=35ec) = 6(3)2+6(3)-72

=0

(ii) V(=0) = 6(0)+6(0) -72=-72 units/sec.

Tii) Q(t=0) = 12(0)+6 =6. unity =c2

(v) O(+=+) = 12(4)+6 + ... = 54. Units/sec2.

2) The distance-time formula of a moving particle is $S = \frac{t^3}{3} \cdot \frac{7}{2}t^2 + 6t - 10 = 0$ find.

i) Velocity at t=35c.

 $\frac{1}{50}$ Solven $\frac{1}{3}$ $\frac{1}{3}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{3}$ $\frac{1}{2}$ $\frac{1}{2$

 $\sqrt{\frac{1}{2}} = \frac{3t^2}{2t} + \frac{14t}{2} + \frac{1}{2}$

ds = t2-1/2 +6.

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$$V_{(t=3\,\text{sec})} = 3^{2} - 7(3) + 6$$

$$= 9 - 21 + 6$$

$$= -6 \text{ units / sec}.$$

(iv) acceleration at t=4 Sec.

The distance time formula of a moving particle 18 3=
$$\pm \frac{3}{6}$$
 - Fit 2 +6t-10. Find.

In Initial Velocity.

$$V = \frac{dS}{dt} = \frac{3t^{2}}{62} - 5(2t) + 6$$

$$= \frac{t^{2}}{2} - 10t + 6.$$

$$a = \frac{d^2s}{dt^2} = \frac{pt}{z} - 10$$

Initial Velocity
$$V_{(t=0)} = 0^{2} - 6 + 6$$

velocity at t=3 Sec.

Velocity at t=3 Sec.

$$9 -10(3) +6 = 9$$
 $9 -30 +6$
 $9 -48 -48$

$$= \frac{9}{2} - 24 = \frac{9 - 48}{2} = \frac{-39}{2}$$

$$= \frac{9}{2} - 48 = \frac{9}{2} - 48 = \frac{9}{2}$$

$$= \frac{9}{2} - 48 = \frac{9}{2} - 48 = \frac{9}{2}$$

$$= \frac{9}{2} - 48 = \frac{9}{2} - 48 = \frac{9}{2}$$

$$= \frac{9}{2} - 48 = \frac{9}{2} - 48 = \frac{9}{2}$$

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acceptedation at
$$t = 4 \sec c$$
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$$acceptedation at $t = 4 \sec c$.

$$acceptedation at $t = 4 \sec c$.

$$acceptedation at $t = 4 \sec c$.$$$$$$

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Engents and sommal

Tangent:

The steeright wine which touches the Gave at a paint is called the tangent.

Noamal:

Normal is the straight line which is perpendicular to the targent and passing through the point at which the tangent touches the Curve.

Note:

i) slope of a tangent = dy

ii) slope of a Normal = m

(iii) Egn of a dangent => y y = m(x-x)

iv) Eqn of a normal = $y-y_1=\frac{1}{m}(n-n_1)$

En targent and Problems! find the egn of tangent and normal to the cure by = 3-2 at (1,1).

dy = 24. Given 2y = 3-xn, at (1,1).

2 dy = 8-2x

Egn dja normal => y-1 = 1 (x-1)

[n-y=0]

a) Find the agn of the Tangent and marrial to the aure y= 5-2x-3x iat (2, 1) GIven . y= n-2x-3x2. $\frac{dy}{dx} = 0 - 2 - 3(2x)$ = -2-6x. dy =-bx-2. Jn Slope of the tangent m = -14. Slope of the normal = == 14 = 14. Egn of the tangent y-y, = m (x-x1) 14x+y+11-28=0 14x+y-17 =0.

Egn of the Normal $y-y_1 = \frac{1}{17}(x-x_1)$ $y+11 = \frac{1}{14}(x-2)$ $y+11 = \frac{1}{14}(x-2)$ y+11 =

the tangent m= 9 Intergration! normal m= -5. slope of Intergration Egn of the tangent y-y = m (x-x,) basic formula! y-4= 1/5 (x-2) $\int_{X}^{n} dx = \frac{x^{n+1}}{n+1} + C$ Fy-20 = 4x-8 1x-by +12=0. Cos ax dx = Sirox + C - cos an + c Ay-16 = - 5x +10 (ocar da $\int \frac{1}{\pi} dn = \log n$ лх+4y-10-16=0 J tanaxoln = log (Gleax) + C カカナ49 -26-0 Seconda = log (Hanax + vsecan) + C 801 xd - 301401 Setandz = tanax + 4 S Cosec ax dx = -Cotan +C Judy = uv-Svale.

12) Sodx = Cx + C. Juv dz = UV, -U'V2+U'13-(100) definite integral? Jaenadn = xenx - 2xenx 2enx Ts an integral where [0,5] = 0 = x = the limits are given. [0,0] = 0 = x = 5 [0,0] = 05 x < 5 Inteférite antergral!- (0,5]=0 =x =5 3) In2 logn du. Is an Entergral where the Rosmits Problems Parth Anthe Anth $U = \log x$ $V_1 = \frac{2}{x}$ $U' = \frac{1}{x}$ $V_1 = \frac{2}{x}$ $V_2 = \frac{2}{x}$ $V_3 = \frac{2}{x}$ 1) Ste3x + Cos 4x+ + x+3 + Sec24x +3) dn Partly = 5 e 8x + Son4x + log(6x+3) + tan4x +3x +c. Juv dn = vv, - u'v2 + u"1855 Sign dx = logx 3 - 1 x4 = 1 x 60 = logn x3 - 2x - 2x - ... - to = logx 23 - x3, x3 + + c.

Sidortoso = 1 \$) In tan'x dx: Sag todas In Jan x-1 J dx Care 0 - 601001 500 - Sunso Sinder = x Jolx 650 = 17 60520 In 0: 19 Cas20 Jurds : 44 - 0/1/2 + 4"1/3 -Jatan xdx = ntanx - lagseex - x 1) Jehanda Casia = 2) Sinax = 3 dx 3) In3 sin3x dx 1) Sx d sin2 in dx 5) Sx 3 Gos 2 +x dx

Asea bounded by a closed Curve The definite intergral Jydx = Jx dy. gives the area of the region which is bounded by the Guare . y= /(x), The axis of De and the two ordinates & and and - &= b. I find the area bounded by the aure y= x2+x from x=1 and x=3. $\int_{a}^{b} y \, dx = \int_{a}^{b} x \, dy.$ $\int_{0}^{b} y dx = \int_{0}^{3} x^{2} + x$ $= \sqrt{\frac{x^3}{3} + \frac{x^2}{2}}$

= 13 12 - 5 1 + 1 = \[\frac{50+10}{6} \] - \[\frac{2+3}{6} \] = [8] - [5] 125 6 7 6 7 21 $\int e^{6\pi} x^5 dx = \chi^5 e^{5x} - \frac{5xe^{5x}}{25} + \frac{5e^{5x}}{125}$ 2) $\int \sin 4x \, e^3 x \, dx$ $\int Sinan e^{3\pi} dn = e^{3\pi} \int Sinan - \cos 3e^{3\pi} - \frac{as}{4}$ $+ 2e^{3\pi} \frac{\cos 4\pi}{\cos 2} + 27e^{3\pi} \frac{\cos 4\pi}{\cos 2} - \frac{\cos 4\pi}{\cos 2}$ (Standar of a Swarm of Saftoson

$$\int_{3}^{2} \int_{3}^{2} \int_{3$$

```
12 = 23 + Costa
    = 23+5 m 24
   = x1 ( -2 ) -4,3 ( :x - sin 2n)
      +12(23+sin24)+1, [-.
```

Lind the case a bounded by the Curro y= 2 41 from 2 = 1 , to 3. y dn = } x +1 $\frac{8180368}{3} + 2 = \sqrt{3} + 2 = 1$ $= \frac{\sqrt{3}+3n}{3}$ $= \begin{bmatrix} 1 & 4 & 3 \\ 3 & 3 \end{bmatrix} - \begin{bmatrix} 1+3 \\ 3 & 3 \end{bmatrix}$ = 36 - 4 = 320 Aind the curea bounded by the Cure) g dx = (2 dx =) 0/1 = [x4] 4. 2 4 1 $=\frac{256}{4} - \frac{1}{4} = \frac{255}{4}$

J= 22 from x=0-10 1 Jy dx = J2 dn Sino=0 $d = \frac{1}{3} \int_{0}^{\pi} \int_$ find the area brounded by one leave 4=22 Jaom x=062 Sydx= J2ardr. $\left(\frac{2x^3}{3}\right)^2$ $\frac{16}{3} - \frac{0}{3}$

= 1 15 500 1 -0

15° 1 - 46° 1 - 6° 11

and the area of the b using integration me that The egn of the Circle with Center of the exign a radius b Here z varies from x=0 to x=b and $=4\left[\frac{b^{2}}{a}S_{0}^{2}-1\right]$ $=\frac{4b^2u}{4} = b^2\Pi$

Volume!

The Volume of the Solid obtained by rotating the daca bounded by the Couve y= 1 (52) and x-axis hetween x=a and x=b obout the x axis is integral Jxiyax is equal to

The volume of when the our bounded by the Gure y= 1(x) and y anis is sevolved about the y anis letween y=a, y=b is intergrat actorbe!

daea: Pagabóle > y= 4ax, lingt ox=0, and x=b. Fr=120 pubola = a la sa sa da.

find the Volume of the Spapers of unders of a using integrationes, a Volume of the Sphar is Obtained when the ware bounded by the Semi windle 2. x2+y2= 2 and the x anis when It is notated rabort the x-axis vote known That 22+y2=x2 13 a Circle when center at the origin with radius , when we connited a similarde, x, varies from -r to r and y=2-2-x. .. Volume of the sphere of Tig dx $\int_{\alpha} \pi y^2 dx = \int_{\alpha} \pi (x^2 - x^2) dx$ 2 (2-2) dn 12 Tu Trac x3/10

Find the Whome of the right Circular lone of base sodius V. bounded by the line OB and x-axis is notated by about the x-axis, the Obtained? :. Here I varies from 0 to h y= 1/x. y=mx where m= 7.) Try dx = 2 11 /2 x dx. of the sedn

. 17 2 23 h JSih Mx Cosnx = - Cos x sin x + m-1. = Sin x x x n-1
m+n when mis odd (n= odd o reven) EATH = m-1 m-3 m+n-2 mapping 3+gn A71

In= Sunadx. nIn= - lon " -1 x Losx + (n-1) Inz. Non 1x dx = n-1 n-3 2 (nis cold) O Sin x dx = n-1 - 2-1 5-1/2 (nis way In = flos x dx nIn=600-1x Sinx+6-1) In-2 los x dx = n-1. n-3. 1 65 h dn = 1 1 13 --- /2 [n is even) Evaluate Entragent Scos x dx Ving 2) Visual integration method ii) Reduction formula. ii) find the scale

May Dusual untegration method: Cos x dx = Jas x Cosn dx put y= sinx = (1- sin 2 x) Cosx dx in (230 (ring) dy : x) x 200 $= \left| \frac{y^3}{y^3} \right| + c$ = [13 hx - 3 m3x] + G) In= Stoom dx. x x x x + 2 I 1 Who king 37 Cook & Sinx + 2] , Keels 4 tol who have the control of the start of the sta

(ax+b) ndx = (n+1)a O nove n=3 (odd) 1/2 (as 2 dx = 1/3 Evaluate intergral Sin 5x vdx 1) Using Usual substitutional method e) reduction formula. 8) 1/2 sins & da. find. Son:
i) Usual Substitution method. Ssinfada = SisinAn Sina da z S (sin2n) 2 sin ndn Let y=losx x dy = sinxdx = = (1-cosx) sinxdx -dy = sinxdx. = - ((-dy+y1)dy

 $= -\left[y - \frac{2y^3}{3} + \frac{y^5}{5}\right] = -\cos x + \frac{2}{3}\cos^3 x - \frac{\cos^2 x}{5}$ ii) Reduction method In Join dx . The stand $I_{n} = \frac{1}{n} \left[- \frac{1}{3} \sin^{n-1} x \cos x + (n-1) I_{n-2} \right]$ In = 5 J- Sin 1 x 600 x + 4 Dz = = [-Sintxloox+4][-bin2xloox+e] [- 5 [- sinta cox + 4 [- sin x 60x +2 [sin x dx] = 1 [- Sin 4 605x+ 1/3 [-sin2x 605x-260x]+C. iii) y Sin Fin dx ... Odd)
Hear n=s (odd) 1/2 sin 5 x dx = (n-1) (n-2) (n-2) ... /3 = 7.2/-= 18 .

2) Sinta dx. A) 1) (65 % dx Sough du = 1/ Cos n-1 doing of Usual Integration Method Sin4xdx = man = 6 Las & Sina+ 5 Is Go Ta sinx+ 5 [cos 2 Sinx+ 1) Using Reduction method. $\int \sin^4 x \, dx = \int \int \sin^3 x \, \cos x + 3 \, I_2$ who I for the sinx + of Source + a Sinx -4 - Sin 3x Cosx +3 [- Sin x Cosx + I] (i) (i) (os xdx = $\frac{(n-1)(n-3)(n-7)}{(n-2)(n-4)}$ = 1 [- Sinx Cosx + 3/ [- Sinx Cosx +: 20 +c] $=\frac{5}{62}\cdot\frac{3}{4}\cdot\frac{1}{2}\cdot\frac{11}{2}$ $=\frac{511}{32}\cdot\frac{1}{32}\cdot\frac{11}{$ (ii) Sin trada. $\int_{0}^{\infty} \sin^{4}n \, dx = \frac{(n-1)(n-2)(n-5)}{n(n-2)(n-4)} \cdot \frac{1}{2} \cdot \frac{1}{2}$ Evaluate:

Spin x los x dx Using (1) Intergration method
(ii) Intergration method = 311

- Sin3x losx-3/ Sin x losx+C Eq: [657xdx = 1 65x sinx + 6 Is (n=4) 1 65 x Sinx + 6/ [+ 65 9 x Junx + 4/ [/ 65 2 x Sinx + 2/3],] = 5 = 4 Cost & Sinx + 64 [+ Cost x Sinx + 1/5 [/3 Cost x Sinx n-1) (n-3) (n-5) / when

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Eg Suntx dx: 3.1 1/ = 5/6 (when both man is even) Eg. Jas x dx = 6.4.2 = 16 Sun x cos x dx = 4.2:6/4:7
12.10.8:44.7 Sinmy las nedx = men coshe x Sin Sin m-2 Los x dx) = 72 605 Se Sint x + 3 [70 605 x Sin 30 + 2/0 Sunx = -1 65 & Sintx+/ [-1 658 x Sin2x+/5] -18 ione value is

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Salog x dx spar. Strondx - 6882 Area of the Region bounded by x=a, x=b and a) Cosx dx = sinx a curre, lies above the x axis is 12 dx = logx $\int o \, dx = C$ SEdn = S dx = Fx $\int \frac{1}{x+2} \, dx = \log \left(x+2 \right)^{\frac{1}{2}}$ $\int_{-\sqrt{2}+3}^{1} dx = \int_{-\sqrt{2}}^{1} \int_{-\sqrt{2}+3}^{2} dx = \int_{2}^{1} \int_{-\sqrt{2}+3}^{2} dx = \int_{2$ Ana voj du sigion bounded = Sady.

eby a luare, y=9; y: b à dies right o

to y-anis is $\int_{1}^{\infty} \int_{1}^{\infty} \frac{1}{x^{2}} dx = \int_{1}^{\infty} \int_{1}^{\infty} \int_{1}^{\infty} \frac{1}{x^{2}} \int_{1}^{\infty} \int_{$ $\int \sqrt{n^2 - a^2} \, dx = \frac{2}{2} \sqrt{n^2 - a^2} - \frac{a^2}{2} \left(\frac{\partial \ln \sqrt{a}}{\partial a} \right)$ a liare y=a, y=b à lies lest = f-ndy.

to y-axis is 1) strea of the engion decunded by $\int \frac{dx}{2^{2}-x^{2}} = \frac{1}{a(2)} \log \left(\frac{2+x}{2+x}\right) + C$ $\int (x-2x)^5 dx = \frac{(x-2x)^6}{6(-2)} = \frac{(x-2x)^6}{-12}$ and below the x-axis a x-axx=b) a c and below the x-axis a x-axx=b) a c l

6) Area of the region abounded right = fady + f-x
and left of the y-axis & y-a & y=b a $\int_{a^{2}-x^{2}}^{dx} = \frac{1}{a^{2}} \log \left(\frac{a+x}{a-x}\right) + C$ Jax+6) dn = (ax+6) n+ (n+1)(a)

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Find the area of the region bounded by 3x-2y+6=0 and Given: 3x-2y+6=0, oc=1, x=3 and x-ani When x=1, when x=3, g ARIA = Sy dx Area = \ 3x+6 dx. $=\frac{1}{2}\left[\frac{3x^2+6x}{a}+6x\right]$ = 1/ 24+24

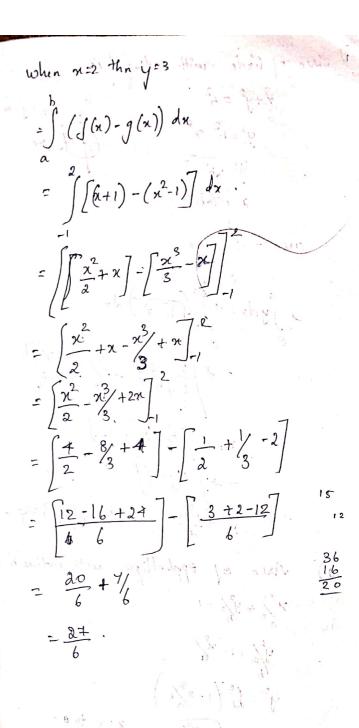
of the region bounded by the Curre y=x2-5x+4, x=2, x=3 4 x-axis when seed, y=+2 when x=3 x=-2 = - \[\frac{\alpha^3}{3} - \frac{5\alpha}{2} + 4\bar{\bar{\gamma}}{2} \] =1, y=3 & y=axis (left).

$ \frac{1}{2} \left[\frac{4}{2} \right] dy $ $ = \frac{1}{2} \left[\frac{4}{2} \right] - \frac{1}{2} \right] $ $ = \frac{1}{2} \left[\frac{4}{2} \right] - \frac{1}{2} \left[\frac{4}{2} \right] - \frac{1}{2} \right] $ $ = \frac{1}{2} \left[\frac{4}{2} \right] - \frac{1}{2} \left[\frac{4}{2} \right] -$
--

$$-\left(\frac{q-1}{2}\right) - \left(\frac{1-6}{2}\right) + \left(\frac{05-30}{2}\right) - \left(\frac{9-18}{2}\right)$$

$$= \frac{q}{2} + \frac{5}{2} + \frac{7}{2}$$

$$= \frac{q}{2} + \frac{7}{2} + \frac{7}{2$$



$$= 4 \int_{0}^{\frac{1}{2}} \frac{1}{3} \left(\frac{b^{2} - b^{2}}{b^{2} - b^{2}} \right) dx$$

$$= 4 \int_{0}^{\frac{1}{2}} \frac{1}{3} \left(\frac{b^{2} - b^{2}}{b^{2} - b^{2}} \right) dx$$

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$$= 4 \int_{0}^{\frac{1}{2}} \frac{1}{3} \left(\frac{b^{2} - b^{2}}{b^{2} - b^{2}} \right) dx$$

$$= A \frac{b\Pi}{a} = b\Pi dg \cdot Didg .$$

a) Area of emplellipse with radius his

$$\frac{x^{2}}{4} + \frac{y^{2}}{2} = 1$$

$$y^2 = b^2 \left(1 - \frac{\pi^2}{\alpha}\right)$$

Volume:
1) Volume generated cabout x - axis
V=) 17 y dn (cubic vints)

- Ve) Tin dy (cubic Units).
-) Find the volume of the solid generated by the ellipse of the solid generated the x axis.

$$\frac{x^{2} + y^{2} = 1}{x^{2} + y^{2} = 1 - \frac{x^{2}}{\alpha}}$$

$$\frac{y^{2} = 1 - \frac{x^{2}}{\alpha}}{y^{2} = h^{2} \left(1 - \frac{x^{2}}{\alpha}\right)}.$$

$$=1-\frac{n^2}{\alpha}$$

$$=1-\frac{n^2}{\alpha}$$

$$=\frac{1}{a}$$

$$=\frac{1}{a}$$

$$=\frac{1}{a}$$

$$=\frac{1}{a}$$

Volume =
$$\int_{-a}^{a} \frac{1}{11} y^2 dx$$

= $2 \int_{-a}^{a} \frac{1}{15} \frac{b^2}{1 - \frac{3}{2}} \frac{1}{2} dx$.
= $\frac{2\pi b^2}{a^2} \left(\frac{2}{a^2 - x^2}\right) dx$.
= $\frac{2\pi b^2}{a^2} \left(\frac{a^2 x - \frac{2}{3}}{a^3}\right) dx$.
= $\frac{2\pi b^2}{a^2} \left(\frac{a^3 - \frac{2}{3}}{a^3}\right)$.
= $\frac{2\pi b^2}{a^2} \frac{a^3 - \frac{2}{3}}{3}$.
= $\frac{4\pi b^2}{a^3}$. Cubic Units.

$$\frac{x^{2} + y^{2}_{0}}{x^{2}} = 1 - \frac{y^{2}_{0}}{x^{2}}$$

$$x^{2} = \frac{a}{a}(1 - \frac{y^{2}_{0}}{b^{2}}).$$

Unit $y = -b t d b$.

Volume: $V = \int \pi x^{2} d y$.

$$= 2\pi \int \frac{a}{b^{2}} \left(1 - \frac{y^{2}_{0}}{b^{2}}\right) d y$$

$$= 2\pi a \int \frac{a}{b^{2}} \left(1 - \frac{y^{2}_{0}}{b^{2}}\right) d y$$

$$= 2\pi a \int \frac{a}{b^{2}} \left(1 - \frac{y^{2}_{0}}{b^{2}}\right) d y$$

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MATHEMATICS I I - B.TECH - BIOTECHNOLOGY ONLINE QUESTIONS WITH ANSWERS UNIT I MATRICES

Objective type questions	opt1	opt2	opt3	opt4	Answer
The sum of the main diagonal elements of a matrix is called	trace of a matrix	quadratic form	eigen value	canonical form	trace of a matrix
If λ_1 , λ_2 , λ_3 , λ_n are the eigen values of A ,then $k\lambda_1$, $k\lambda_2$, $k\lambda_3$,k λ n are the eigen values of	kA	kA^2	kA^-1	A^-1	kA
If atleast one of the eigen values of A is zero, then det A =	0	1	10	5	0
The equation det (A-λI) = 0 is used to find	characteristic polynomial	characteristic equation	eigen values	eigen vectors	characteristic equation
det (A-λI) represents	characteristic polynomial	characteristic equation	quadratic form	canonical form	characteristic polynomial
If λ_1 , λ_2 , λ_3 , λ_n are the eigen values of A ,then $1/\lambda_1$, $1/\lambda_2$, $1/\lambda_3$, $1/\lambda_n$ are the eigen values of	A^-1	А	A^n	2A	A^-1
If λ_1 , λ_2 , λ_3 , λ_n are the eigen values of A ,then λ_1^p , λ_2^p , λ_3^p , λ_n^p are the eigen values of	A^-1	A^2	A^-p	A^p	A^p
If all the eigen values of a matrix are distinct, then the corresponding eigen vectors are	linearly dependent	unique	not unique	linearly independent	linearly independent
The eigen values of a matrix are its diagonal elements	diagonal	symmetric	skew-matrix	triangular	triangular
If the sum of two eigen values and trace of a 3x3 matrix A are equal, then det A =	λ_1λ_2 λ_3	0	1	2	0
If the characteristic equation of a matrix A is $\lambda^2 - 2 = 0$, then the eigen values are	2,2	(-2,-2)	(2^(1/2),- 2^(1/2))	(2i,-2i)	(2^(1/2),- 2^(1/2))
If 1,5 are the eigen values of a matrix A, then det A =	5	0	25	6	5
The eigen vector is also known as	latent vector	row vector	column vector	latent square	latent vector
If 1,3,7 are the eigen values of A, then the eigen values of 2A are	1,3,7	1,9,21	2,6,14	1,9,49	2,6,14
To multiply a matrix by scalar k, multiply	Any row by k	every element by k	any column by k	diagonal element by k	every element by k

A system of equation is said to be inconsistent if they have	one solution	one or more solution	no solution	infinite solution	no solution
Eigen value of the characteristic equation λ^2 -4 = 0 is	2, 4	2, -4	2, -2	2, 2	2,-2
Eigen value of the characteristic equation $\lambda^3-6\lambda^2+11\lambda-6=0$ is	1,2,3	1, -2,3	1,2,-3	1,-2,-3	1,2,3
Largest Eigen value of the characteristic equation $\lambda^3-3\lambda^2+2\lambda=0$ is	1	0	2	4	2
Smallest Eigen value of the characteristic equation λ^3 -7 λ^2 +36 = 0 is	-3	3	-2	6	-2
Sum of the principal diagonal elements =	product of eigen values	product of eigen vectors	sum of eigen values	sum of eigen vectors	sum of eigen values
Product of the eigen values =	(- A)	1/ A	(-1/ A)	A	A
A cause matrix A its transpose AAT have the	same eigen	different	same eigen	different eigen	same eigen
A square matrix A its transpose A^T have the	vectors	eigen vectors	values	values	values
If 1 and 2 are the eigen values of a 2X2 matrix A, then the eigen values of A^2 is	2, 4	3,4	5,6	1, 4	1, 4
If 1 and 2 are the eigen values of a 2X2 matrix A, then the eigen values of A^-1is	2,1/2	1,1/2	1,2	4,1/2	1,1/2
If a real symmetric matrix of order 2 hasthen the matrix is a scalar matrix.	equal eigen	different	equal eigen	different eigen	equal eigen
	vectors	eigen vectors	values	values	values
If A and B are nxn matrices and B is a non singular matrix then A and B^-1AB have	same eigen	different	same eigen values	different eigen values	values
If the eigen values of A are 2,3,4, then the eigen values of Adj A is	vectors 1/2,1/3,1/4	eigen vectors 1/2,-1/3,1/4	2,5,6	2,5,-6	1/2,1/3,1/4
The maximum value of the rank of a 4x5 matrix is	1	5	4	3	4
A square matrix A which satisfies the relation A^2 = A is called	nilpotient	idempotient	Hermitian	Skew - Hermitian	idempotient
A matrix is idempotient if	A^3 = A	A^2 = 0	A^1 =A	A^2 = A	A^2 = A
If the rank of A is 2, then the rank of A^ -1 is	3	2	4	1	2
If sum of two eigen values of 3x3 matrix A are equal to the trace of the matrix, then the determinant of A is	1	2	0	5	0
If a matrix A is equal to A^T then A is a matrix.	symmetric	non symmetric	skew-symmetr	icsingular	symmetric
If a matrix A is equal to -A^T then A is a matrix.	symmetric		skew-symmetr	_	skew-symmetric
A square matrix A is said to beif the determinant value of A is zero.	singular	non singular	symmetric	non symmetric	
A square matrix A is said to beif the determinant value of A is not equal to zero.	singular	non singular	symmetric	non symmetric	non singular
A square matrix A is said to be singular if the determinant value of A is	1	2	non zero	zero	zero
0					
A square matrix A is said to be non singular if the determinant value of A is A square matrix in which all the elements below the leading diagonal are zeros, it is	1	2	non zero	zero	non zero
called anmatrix.	upper triangula	r lower triangula	aı symmetric	non symmetric	upper triangular
A square matrix in which all the elements above the leading diagonal are zeros,it is					
called anmatrix.	upper triangula	r lower triangula	-	non symmetric	lower triangular
A unit matrix is amatrix.	scalar	lower triangula	aı symmetric	non symmetric	scalar
A system of equation is said to be consistent if they have	one solution	one or more solution	no solution	infinite solution	one or more solution
If rank of A is equal to the rank of [AB] then the system of equations is	Consistent	inconsistent	symmetric	non symmetric	Consistent
If rank of A is not equal to the rank of [AB] then the system of equations is	Consistent	inconsistent	symmetric	non symmetric	inconsistent

UNIT II THEORY OF EQUATIONS

Objective type questions	opt1	opt2	opt3	opt4	Answer
If α , β , γ are the roots of the equation $x^3-px+q=0$, then $\Sigma 1/\alpha =$	pq	p+q	p-q	p/q	p/q
If α , β , γ are the roots of the equation $x^3 = 7$, then $\Sigma \alpha^3$ is	10	21	34	14	21
A root of $x^3-3x^2+2.5 = 0$ lies between	1.5 and 2	1.2 and 1.8	1 and 2	1.1 and 1.2	1.1 and 1.2
In an equation with real coefficients, imaginary roots must occur in	non conjugate pairs	conjugate pairs	real pairs	imaginary pairs	conjugate pairs
If $f(\alpha$) and $f(\beta$) are of opposite signs, then $f(x){=}0$ has atleast one root between α and $\beta provided$	f(x) is continuous in (a,b)	f(x) is discontinuous in (a,b)	f'(x) is continuous in (a,b) x^3-	f(x) is continuou s in (-a,-b) x^3-	f(x) is continuous in (a,b)
If α , β , γ are the roots of the equation x^3+2x+3=0, then α +3, β +3, γ +3 are the roots of the equation	x^3+9x^2+29x- 24=0	x^3-9x^2+29x- 24=0	9x^2+29x+24 =0		x^3-9x^2+29x- 24=0
If one root is double of another in $x^3-7x^2+36=0$, then its roots are	3,4,-2	3,6,5	4,6,-2	3,6,-2	3,6,-2
The equation whose roots are 10 times those of $x^3-2x-7 = 0$ is	x^3+200x- 7000=0	x^3-200x- 7000=0	x^3- 200x+7000=0	x^3+200x+ 7000=0	x^3-200x- 7000=0
If α , β , γ are the roots of the equation x^3+px^2+qx+r=0, then $\Sigma(1/\alpha\beta)$ =	pr	p+r	p-r	p/r	p/r
V3 and -1+i are the roots of the biquadratic equation	x^4+2x^3-x^2- 6x-6=0	x^4-2x^3-x^2- 6x-6=0	x^4+2x^3+x^ 2-6x-6=0	x^4+2x^3- x^2+6x- 6=0	x^4+2x^3-x^2- 6x-6=0
If α , β ,y are the roots of the equation x^3 -3x+2=0, then the value of α ^2+ β ^2+y^2 is	4	6	8	2	6
If there is a root of $f(x) = 0$ in the interval [a,b], then sign of $f(a)/f(b)$ is	minus	plus	minus or plus	minus and plus	minus
If α , β , γ are the roots of the equation $x^3 + px^2 + qx + r = 0$, then the condition for $\alpha + \beta + \gamma$ is	p+q=r	pq=r	p-q=r	p/q=r	pq=r
The three roots of $x^3 = 1$ are	1,1/2(-2±v3i)	1, 1+i	1,1/2(-1±√3i)	1, 1-i	1,1/2(-1±V3i)
One real root of the equation $x^3 + x - 5 = 0$ lies in the interval	(2,3)	(3,4)	(1,2)	(-3,-2)	(1,2)
If two roots of $x^3 - 3x^2 + 2 = 0$ are equal, then its roots are	1,1,-2	1,2,1	1,-1,2	2,1,-1	1,1,-2
The cubic equation whose two roots are 5 and 1-I is	x^3+7x^2+12x- 10=0	x^3-7x^2-12x- 10=0	x^3- 7x^2+12x+10 =0	x^3- 7x^2+12x- 10=0	x^3-7x^2+12x- 10=0
The sum and product of the roots of the equation $x^5 = 2$ are	0 and 1	2 and 3	0 and 2	1 and 2	0 and 2
One real root of the equation $x^3 + 2x^2 + 5 = 0$ lies between	3 and -2	(- 3 and - 2)	(5 and 2)	(- 5 and - 2)	(- 3 and - 2)
If the roots of the equation x^4+2x^3- α x^2-22x+40=0 are -5,-2, 1 and 4, then α =	11	15	20	21	21
If for the equation $x^3-3x^2+kx+3=0$ one root is the negative of another, then the value of k is	3	-3	1	-1	-1
If α , β ,yare the roots of $2x^3-3x^2+6x+1=0$, $\alpha^2+\beta^2+\gamma^2$ is	(15/4)	-3	(-15/4)	(33/4)	(-15/4)
X+2 is a factor of	x^4+2				$2x^4 - 2x^3 - x + 2$
If α + β +y=5; $\alpha\beta$ + β y+y α =7; $\alpha\beta$ y =3 then whose roots are α , β ,y is	$x^3 - 7 = 0$	$x^3 - 7x^2 + 3 = 0$	$x^3 - 5x^2 + 7x - 3 = 0$	$x^{3}+7x^{2}-3=0$	$\int x^3 - 5x^2 + 7x - 3 = 0$
If one of the roots of the equation $x^3-6x^2+11x-6=0$ is 2, then the other two roots are	1 and 3	0 and 4	-1 and 5	-2 and 6	1 and 3
Any value of x, for which the equation is satisfied, is known as the of the equation.	factor $-\frac{a_2}{a_0}$	- solution	function	coefficient	solution

In algebraic equations, solutions are known as of the equation.	Roots or zeros	function	degree	order	Roots or zeros
The roots of the cubic equation can be obtained by method.	Ferrari's	lagrange's	Horner's	cardano's	cardano's
The one of the relation between roots and coefficients of the equation is $-(a_2/a_0)$	(-a1/a0 = sum of the roots)	(-a1 = sum of the roots)	(a0/a1 = sum of the roots)	(a1/a0 = sum of the roots)	(-a1/a0 = sum of the roots)
The one of the relation between roots and coefficients of the equation is =	Sum of the products of the	•	Sum of the products of	Sum of the	Sum of the products of the
The equation whose roots are the reciprocals of the roots of is	$\frac{(x^3+1)}{p(x^2+1)}/r=0$	\!\!r.(&+1)\!\p(\x+1)=C	$r\vec{x} + p\vec{x} + 1 = 0$	<i>r</i> x+ <i>px</i> +1=($)rx^3 + px + 1 = 0$
If the roots of x^3-3x^2 , take in a little hetic progression then the sum of squares of the largest and the smallest roots is	3	5	6	10	6
A root of $x^3 - 8x^2 + \sqrt{2}$ ere $\sqrt[6]{a}$ and $\sqrt[6]{q}$ are real numbers is . The real root is	2	6	9	12	2
If a real root of $f(x) = 0$ lies in [a, b], then the sign of $f(a)$. $f(b)$ is	Minus	plus	plus or minus	none	Minus
Theory of equations consists of methods of obtaining of equations.	coefficients	functions	solutions	factor	solutions
For the linear equation ax + b = 0, the solution is, $a \ne 0$.	a/b	-b/a	a	b/a	-b/a
The roots of quartic equation are obtained by method. No literal equation exist for finding the solution of algebraic equation of	cardano's	Ferrari's	lagrange's	Newton's	Ferrari's
degree	n > 2	n > 3	n>=4	n>=5	n>=5
The one of the relation between roots and coefficients of the equation is $-a_3/a_0$ =	sum of the products of the roots taken two	sum of the products of the roots taken three	sum of the products of the roots taken four	sum of the products of the roots taken five.	sum of the products of the roots taken three
The one of the relation between roots and coefficients of the equation is $(-1)^n a_n/a_0 =$	product of coefficient	product of function	product of roots	sum of the roots	product of roots
Atleast one root of the equation lies between if f(a) and f(b) are of different (opposite) sign.	–a and –b	–a and b	a and b	a and –b	a and b
The common solutions of the equation $z^4 + 1 = 0$, $z^6 - i = 0$ are	(-1+i)/V2, (1- i)/V2	(-1-i)/V2, (1- i)/V2	(-1+i)/V2, (-1- i)/V2	(- 1+i)/V3,(1- 2i)/V3	(-1+i)/V2, (1- i)/V2
If the equation $x^4 - 4x^3 + ax^2 + bx + 1 = 0$ has four positive roots then $a = 2$? and $b = 3$?	6,-4	-6, 4	6, 4	-6,-4	6,-4
Every equation of the odd degree has atleastone real root.	one	two	three	four	one
If an equation remains unaltered on changing x to 1/x it is called aequation.	quadratic	cubic	reciprocal	polynomia I	reciprocal
If two roots of $x^3 - 3x^2 + 5x + k = 0$ are equal, but opposite in sign, then what is the value of k ?	-14	-15	16	20	-15
A polynomial equation whose roots are 3 times those of the equation $2x^3 - 5x^2 + 7 = 0$ is:	3x^3 -15x^2 + 21 = 0	2x^3 -15x^2 +189 = 0	2x^3 +15x^2 - 189 = 0	3x^3 +15x^2 + 21 = 0	2x^3 -15x^2 +189 = 0
The number of real zeros of the polynomial function x^2 +1 is:	1	0	2	4	0
If α is an r -multiple root of $f(x)=0$, then which of the following polynomial has α as an(r -1) - multiple root ?	f^2 (x) = 0	f'(x) = 0	f (x) = 0	f (-x) = 0	f'(x) = 0

If - 2 + 3i is a root of the polynomial equation $p(x) = 0$, then another root is:	2 + 3i	2 -3i	-2 - 3i	3- 2 i	-2 - 3i
A zero of the polynomial x^3 + 2x - i equals:	- (i)	1	1-i	1+i	- (i)
If α,β are the roots of ax^2 -bx -c = 0 , then α + β equals:	(- b / a)	(- c / a)	(a / b)	(b / a)	(b / a)
If α , β ,y are the roots of the equation x^3 +px^2+qx+r=0, then the for $\alpha\beta$ + β y+y α equals	(-p /q)	(-p)	q	(-q)	q
If α , β , γ are the roots of the equation $x^3 + px^2 + qx + r = 0$, then $(1/\alpha) + (1/\beta) + (1/\gamma)$ is	(-q/r)	(-p/r)	(q/r)	(-q/p)	(-q/r)
If α , β , γ are the roots of the equation x^3 +px^2+qx+r=0, then 1/ $\beta\gamma$ +1/ $\gamma\alpha$ +1/ α β equals	(-p/q)	(p/r)	(-p/r)	(-q/r)	(p/r)
If α is a root of a reciprocal equation $f(x) = 0$, then another root of $f(x) = 0$ is:	(-1/α)	1/α^2	να	(1/α)	(1/α)
The equation $x^3 + 2x + 3 = 0$ has:	one positive real root	one negative real root	three real roots	four real roots	one negative real root
Greatest possible number of real roots of $x^10 - 10x^6 - 5x^3 + x + 4 = 0$ is :	6	5	10	8	6
How many real roots are there for the equation $x^5 - 6x^2 - 4x + 5 = 0$?	5	1	3	0	3
If 3 is a double root of the equation $8x^3 - 47x^2 + 66x + 9 = 0$, the third root is:	(-1/8)	(1/8)	8	-8	(-1/8)

UNIT III DIFFI	ERENTIAL CALO	CULUS AND ITS	S APPLICATIO	N	
Objective type questions	opt1	opt2	opt3	opt4	Answer
The derivative of x^n is	$(n-1) x^{(n-1)}$	n x^(n-1)	(n-1) x^n	$n \times (n+1)$	n x^(n-1)
The derivative of sinx is	Sinx	cosx	-sinx	cosx	cosx
The derivative of a constant is	0	1	-1	00 00	0
The derivative of a constant is	O	1	-1	ω	O
The derivative of a^x , $a>0$, $a\neq 1$ is	a^x	x a^(x-1)	a^x loga	loga	a^x loga
The derivative of $e^{-(-x)}$ is	e^x	x e^x	e^(-x)	-e^(-x)	-e^(-x)
The second order derivative of x^3-5x^2+3x+4			()	()	
is	$3x^2 - 10x + 3$	6	6x-10	$3x^2-10x$	6x-10
The second order derivative of x^3 + tanx	$6x - 2 (secx)^2$	$6x+2 (secx)^2$	$6x + 2 \sec x$	6x-2 secx	6x+2
is	tanx	tanx	tanx	tanx	(secx) ² tanx
	turn.	tuini			(seek) 2 tallit
The second order derivative of logx is	1/x	1	0	∞	1/x
is	$3x^2 - 10x + 3$	6	6x-10	$3x^2-10x$	6x-10
				(xsinx-	
The derivative of x cosx is	$(-x\sin x + \cos x)$	(xsinx + cosx)	(-xsinx-cosx)	cosx)	(-xsinx+ cosx)
				(-xcosx-	
The derivative of x sinx is	(xcosx-sinx)	(-xcosx+sinx)	(xcosx+sinx)	sinx)	(xcosx+sinx)
			$(-e^{(x)}) + x$	(-e^(x))-x	
The derivative of x e^x is	$e^{(x)} - x e^{(x)}$	$e^{(x)} + x e^{(x)}$	e^(x)	e^(x)	$e^{(x)} + x e^{(x)}$
			$(-e^{(x)}) + x$	(-e^(x))-x	
The derivative of $x e^{-(-x)}$ is	$e^{(x)} + x e^{(x)}$	$e^{(x)}$ -x $e^{(x)}$	e^(x)	e^(x)	$e^{(x)}$ -x $e^{(x)}$
If $f(x) = \sqrt{2}x$ then $f'(2) =$	(1/2)	(-1/2)	-2	1	(1/2)
The derivative of x logx is	logx + 1	logx - 1	1/x	(-1/x)	logx + 1
5	8	8		(-16	8
The second order derivative of sin4x is	16 sin4x	$(-16 \sin 4x)$	16 cos4x	cos4x)	16 sin4x
		,		(-16	
The second order derivative of cos4x is	16 sin4x	$(-16 \sin 4x)$	16 cos4x	cos4x)	$(-16\cos 4x)$
1110 00001110 01001 0001 0001 000 011 1000000	10 2111 111	(10 311 11)	10 2051	302)	(10 000)
The second order derivative of $e^{(x)}$ is	(-e^(x))	(-e^(-x))	e^(x)	e^(-x)	e^(x)
((- (/)	(- (/)	- ()	- ()	- ()
The second order derivative ofe^(-x) is	(-e^(x))	e^(x)	(-e^(-x))	e^(-x)	e^(x)
()	(- (/)	- ()	(- ())	- ()	- ()
The second order derivative ofe ^(-2x) is	$(-4e^{(2x)})$	$(-4e^{(-2x)})$	$4e^{-2x}$	$4e^{-2x}$	$4e^{-2x}$
The second order derivative of	$4x^3+12x^2+2$	(' (=))	(===)	(===)	(===)
$x^4+4x^3+x^2+3x+4$ is	x+3	12x^2+24x+2	24x+24	24	12x^2+24x+2
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The second order derivative of $x^{(n)}$ is	n x^ (n-1)	n (n-1) x^(n-1)	n(n-1) x^(n-2)	n (n-1)x^n	n(n-1) x^(n-2)
The second derivative of $(1-x^{(2)})$ is	2x	(-2x)	2	(-2)	(-2x)
If $x= a t^2$, $y=2at$ then $dy/dx=$	(-1/t)	1	1/t	-1	1/t
, ,	,				
If $x=a \sin^{(3)} t$, $y=\cos^{(3)} t$ then $dy/dx=$	cot t	tant	(-cot t)	(- tan t)	(-cot t)
If $x = a(1 + \sin \theta)$, $y = a(1 + \cos \theta)$ then			7	•	· -)
dy/dx=	cot t	tant	(-cot t)	(- tan t)	(-cot t)
If $xy=c^2$ then $dy/dx=$	y/x	(-y/x)	x/y	(-x/y)	(-y/x)
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The slope of the tangent to the hyperbola $x^2 - y^2 = 12$ at $(4,2)$ is	4	2	(1/2)	(1/4)	2
The slope of the tangent to the curve $y=x \sin x$ at $(\pi/2, \pi/2)$ is	-1	-2	2	1	1
The slope of the tangent to the curve $x^{(2)} = 4y$ at the point $x=-2$ is	-1	-2	2	1	-1
The gradient of the tangent to the curve at the	4	10	10	2.4	10
point x=2 to the curve y= $4x^{(3)}-15x^{(2)}$ is	4	-12	-18	-24	-12
The gradient of the tangent to the curve at the					
point $x=3$ to the curve $y=3x^{2}-7x-2$ is	3	4	9	11	11
The slope of the normal to the hyperbola x^2 -					
$y^2 = 12$ at (4,2) is	2	(1/2)	(-1/2)	(-1/4)	(1/2)
The slope of the normal to the curve $y=x \sin x$ at (•	•		
$\pi/2$, $\pi/2$) is	-1	-2	2	1	-1
The slope of the normal to the curve $x^{(2)} = 4y$ at	1	2	2	1	1
the point x=-2 is	-1	-2	2	1	1
The slope of the normal to the curve at the point					
$x=2$ to the curve $y=4x^{(3)}-15x^{(2)}$ is	(-1/12)	-12	(1/12)	12	(1/12)
The slope of the normal to the curve at the point					
$x=3$ to the curve $y=3x^{(2)}-7x-2$ is	-11	(-1/11)	11	(1/11)	(-1/11)
If $f(x) = \sin x$ then $f'(0) = \dots$	0	-1	1	-2	1
If $f(x) = \cos x$ then $f(0) = \dots$	2	-1	-2	1	-1
If $f(x) = \log x$ then $f(1) = \dots$	2	-1	-2	1	1

UNIT-IV INTEGRAL CALCULUS AND ITS APPLICATION

Objective type questions	Opt 1	Opt2	Opt3	Opt4
$\int x^n dx = \dots$	$x^{(n+1)}/(n+1) + C$	$x^{(n-1)}/(n-1)+C$	nx^ (n-1)+ C	$(n+1) x^{(n+1)} + C$
$\int \cos x dx = \dots$	sinx + C	$\cos x + C$	$(-\cos x)+C$	(-sinx)+C
$\int \sin x dx = \dots$	sinx + C	$\cos x + C$	(-cosx)+C	(-sinx)+C
$\int e^{x}(x) dx = \dots$	(-e^x)+ C	$e^{(-x)} + C$	$(-e^{(-x)})+C$	$e^{x} + C$
$\int e^{-(-x)} dx = \dots$	(-e^x)+ C	$e^{(-x)} + C$	$(-e^{(-x)})+C$	$e^{x} + C$
If u and v are differentiable functions then $\int u dv = \dots$	uv+∫v du	uv+∫v du	(-uv)+∫ v du	(-uv)-∫v du
$\int \cos^{4}(4) x dx$ (from 0 to $\pi/2$) =	$3\pi/16$	$5\pi/16$	$7\pi/16$	$9\pi/16$
$\int \cos^{4}(6) x dx$ (from 0 to $\pi/2$) =	$3\pi/16$	$5\pi/16$	$7\pi/16$	$9\pi/16$
$\int \cos^{4}(9) x dx$ (from 0 to $\pi/2$) =	$3\pi/16$	$5\pi/16$	$7\pi/16$	$9\pi/16$
$\int \sin^{5}(5) x dx$ (from 0 to $\pi/2$) =	$\pi/15$	$\pi/15$	$8\pi/15$	$8\pi/15$
$\int \sin^{4}(7) x dx$ (from 0 to $\pi/2$) =	$\pi/15$	1/15	$16\pi/35$	16/35
$\int \cos 2x \ dx = \dots$	$(\sin 2x)/2 + C$	$(\cos 2x)/2 + C$	$(-\cos x)/2+C$	$(-\sin x)/2+C$
$\int \sin 3x dx = \dots$	$(\sin 3x)/3 + C$	$(\cos 3x)/3 + C$	$(-\cos 3x)/3+C$	$(-\sin 3x)/3+C$
$\int (1/x) dx = \dots$	1+ C	log x+C	(-1)+C	$(-\log x)+C$
The volume of the solid of revolution generated by revolving the plane area bounded by the circle $x^2+y^2=a^2$ about its diameter is	(4/3)πa^3	(2/3)πa^3	(1/3)πa^3	πa^3
The volume of the solid of revolution generated by revolving the plane area bounded by the circle $x^2+y^2=2^2$ about its diameter is	$(32/3)\pi$	$(1/3)\pi$	$(2/3)\pi$	π
The volume of the solid of revolution generated by revolving the plane area bounded by the circle $x^2+y^2=3^2$ about its diameter				
is	16π	9π	36π	π
The Volume of a sphere of radius 'a' is	$2/3 \pi a^3$	$4/3 \pi a^3$	1/3 π a^3	π a^3
The surface are of the sphere of radius 'a' is	4πa^2	πa^2	3πa^2	2πa^2
$\int x e^{\wedge}(x) dx = \dots$	$(-x)e^{(x)}-e^{(x)}+c$	$xe^{(x)+e^{(x)+c}}$	$(-x)e^{(x)}+e^{(x)}+e^{(x)}$	$c \times e^{(x)}-e^{(x)}+c$
∫ cosmx dx=	(sinmx)/m + C	$(\cos mx)/m + C$	(-cosmx)/m+C	(-sinmx)/m+C
$\int \sin x dx = \dots$	$(\sin nx)/n + C$	$(\cos nx)/n + C$	(-cosnx)/n+C	(-sinnx)/n+C

∫ dx=	x+C	1	0	x^2
∫ 5dx=	x+C	5x+C	x^2+C	5+C
$\int 3x^{(2)} dx = \dots$	3x^(2)+C	x+C	x^2+C	$x^{(3)} + C$
$\int Sec^{(2)} x dx = \dots$	secx.tanx+C	tanx+C	$tan^{(2)} x + C$	Secx+C
$\int Secx. tanx dx = \dots$	secx.tanx+C	tanx+C	$tan^{(2)} x + C$	Secx+C
$\int e^{(2x)} dx = \dots$	$(-e^2x)/2 + C$	$e^{(-2x)/2} + C$	$(-e^{(-2x)})/2+C$	e^2x/2+ C
$\int e^{-(-2x)} dx = \dots$	$(-e^{(-2x)})/2 + C$	$e^{(-2x)/2} + C$	$(-e^{(-2x)})/2+C$	$e^{(-2x)/2} + C$
The Volume of a sphere of radius '2' is	$16/3 \pi$	$32/3 \pi$	$8/3 \pi$	8 π
The surface area of the sphere of radius '3' is	36π	9π	27π	18π
$\int x^{(2)} dx = \dots$	$(x^{(2)/2})+C$	$(x^{(3)/3})+C$	x+C	2x+C
$\int x \log x dx = \dots$	1-logx+C	logx+C	0	1
$\int \csc^{(2)} x dx = \dots$	cotx+C	tanx+C	(-tanx)+C	$(-\cot x)+C$
$\int \sec^{2}(2) x dx = \dots$	cotx+C	tanx+C	(-tanx)+C	(-cotx)+C

Answer

 $x^{(n+1)}/(n+1) + C$

sinx + C

(-cosx)+C

 $e^x + C$

(-e^(-x))+C

uv+∫v du

 $3\pi/16$

 $5\pi/16$

 $5\pi/16$

8/15

16/35

 $(\sin 2x)/2 + C$

 $(-\cos 3x)/3+C$

log x+C

 $(4/3)\pi a^3$

 $(32/3)\pi$

 36π

 $4/3 \pi a^3$

4πa^2

 $xe^{(x)}-e^{(x)}+c$

(sinmx)/m+ C

(-cosnx)/n+C

x+C

5x+C

x^(3) +C

tanx+C

Secx+C

 $e^2x/2 + C$

 $e^2x/2 + C$

 $32/3 \pi$

 36π

 $(x^{(3)/3})+C$

1-logx+C

(-cotx)+C

tanx+C

UNIT - V ORDINARY DIFFERENTIAL EQUATIONS

Objective type questions	opt1 A e^ (-2x)+ B e^	opt2 A e^ (2x)+ B e^	opt3 A e^ (-2x)+ B	opt4 A e^ (2x)+ B e^	Answer A e^ (-2x)+ B e^
The solution of the differential equation (D^2 + 5D+6)y=0 is	(-3x)	(3x)	e^ (3x)	(-3x)	(-3x)
The solution of the differential equation (D^2 + 6D+9)y=0 is	(A+Bx) e^ (3x)	(A+Bx) e^ (x)	(A+Bx) e^ (-2x)	(A+Bx) e^ (-3x)	(A+Bx) e^ (-3x)
The solution of the differential equation (D^2 -4D+4)y=0 is	(A+Bx) e^ (3x)	(A+Bx) e^ (-2x)	(A+Bx) e^ (-3x)	(A+Bx) e^ (2x)	(A+Bx) e^ (2x)
The particular integral of (D^2 -3D+2)y=12 is	(1/5)	(1/6)	(1/4)	(1/3)	(1/6)
The complementary function of (D^2 -2D+1)y=x sinx is	(A+Bx) e^ (-x)	(A+Bx) e^ (x)	(A+Bx) e^ (-2x)	(A+Bx) e^ (2x)	(A+Bx) e^ (x)
If f(D)= D^ (2)- 2, 1/f(D) e^(-2x) is	0.5 e^ (2x)	-0.5 e^ (2x)	0.5 e^ (-2x)	0.5 e^ (3x)	0.5 e^ (2x)
The particular integral of (D^2+4) y= cos2x is	(x cos2x)/2	(sin2x)/2	(sin2x)/2	(x sin2x)/4	(x sin2x)/4
If (D^2 +4)y=0 is a linear differential equation then general solution is	A cos2x+ B sin4x	Acos2x+Bsin2x	Asin2x+Bcos4x	Asin4x+Bsin4x	Acos2x+Bsin2x
	e^(3x) (A cos2x+	e^(3x) (A	e^(3x) (A	e^(2x) (A	e^(3x) (A
If $(D^2 - 6D + 13)$ y = 0 is a linear differential equation then G.S. is	B sin2x)	cos4x+ B sin4x)	cos2x+ B sin2x)	cos2x+ B sin2x)	cos2x+ B sin2x)
	A e^ (x)+ B e^	A e^ (-x)+ B e^	A e^ (x)+ B e^ (-	A e^ (2x)+ B e^	A e^ (x)+ B e^
The solution of the differential equation (D^2 -4D+3)y=0 is	(3x)	(3x)	3x)	(-3x)	(3x)
	A e^ (x)+ B e^	A e^ (-x)+ B e^	A e^ (-x)+ B e^	A e^ (-x)+ B e^	A e^ (-x)+ B e^ (-
The solution of the differential equation (D^2 +3D+2)y=0 is	(2x)	(2x)	(x)	(-2x)	2x)
The particular integral of $(D^2 + 3D + 2)y = 2 e^(x)$ is	e^(x)/3	(-e^(x))/3	e^(x)/6	(-e^(x))/6	e^(x)/3
The particular integral of (D^2+4) y= e^(x) is	1/5* e^(x)	1/5* e^(-x)	1/6* e^(x) e^(αx)	1/6* e^(x)	1/5* e^(-x)
If the roots of the auxilliary equation are real and distinct then the	Ae^(m1x)+Be^(m		(Acosβx+Bsinβx		Ae^(m1x)+Be^(
C.F is	2x)	(A+Bx) e^ (m1x) e^(αx))	(m2x)	m2x)
If the roots of the auxilliary equation are real and equal then the C.F	Ae^(m1x)+Be^(m	(Acosβx+Bsinβx			
is	2x))	(A+Bx) e^ (mx)	(A+Bx) e^ (-mx)	(A+Bx) e^ (mx)
	A = A/4\ . D = A/	e^(-αx)		e^(αx)	- A (·)
If the roots of the auxilliary equation are complex then the C.F is	Ae^(m1x)+Be^(m 2x)	(Acospx+Bsinpx		(Acosβx+Bsinβ x)	e^(αx)
	,	/ 1/25\004(11)	(A+Bx) e^ (mx)	,	$(A\cos\beta x + B\sin\beta x)$
The particular integral of (D^2 +10D+24)y= e^(-x) is	(1/35) e^(-x)	(-1/35)e^(-x)	(-1/25)e^(-x)	(1/25)e^(-x)	(1/25)e^(-x)
The particular integral of (D^2+9) y= cos2x is	cos2x/13	(-cos2x)/13	(-cos2x)/5	cos2x/5	cos2x/5
The particular integral of (D^2+9) y= cos3x is	x cos3x/2	(-x cos3x)/2	(xcos3x)/6	(-xcos3x)/6	(xcos3x)/6
The particular integral of $(D^2 + 12D + 27)y = e^{-x}$ is	(1/16) e^ (-x)	(-1/16) e^ (-x)	(1/16) e^ (x)	(-1/16) e^ (x)	(1/16) e^ (-x)

	A e^ (15x)+ B e^	A e^ (-15x)+ B	A e^ (15x)+ B	A e^ (-15x)+ B	A e^ (-15x)+ B
The solution of the differential equation (D^2 +19D+60)y=0 is	(4x)	e^ (4x)	e^ (-4x)	e^ (-4x)	e^ (-4x)
	A e^ (5x)+ B e^	A e^ (5x)+ B e^	A e^ (-5x)+ B	A e^ (-5x)+ B	A e^ (-5x)+ B e^
The solution of the differential equation (D^2 +13D+40)y=0 is	(8x)	(-8x)	e^ (-8x)	e^ (8x)	(-8x)
	A e^ (-5x)+ B e^	A e^ (5x)+ B e^	A e^ (5x)+ B e^	A e^ (-5x)+ B	A e^ (5x)+ B e^
The solution of the differential equation (D^2 -9D+20)y=0 is	(4x)	(-4x)	(4x)	e^ (-4x)	(4x)
	A e^ (-8x)+ B e^	A e^ (-8x)+ B	A e^ (8x)+ B e^	A e^ (8x)+ B e^	A e^ (8x)+ B e^
The solution of the differential equation (D^2 +D-72)y=0 is	(-9x)	e^ (9x)	(9x)	(-9x)	(-9x)
The solution of the differential equation (DA2, 11D, 42), —0 is	A e^ (14x)+ B e^	A e^ (-14x)+ B	A e^ (-14x)+ B	A e^ (14x)+ B	A e^ (14x)+ B
The solution of the differential equation (D^2- 11D-42)y=0 is	(-3x) A e^ (15x)+ B e^	e^ (-3x) A e^ (-15x)+ B	e^ (3x) A e^ (15x)+ B	e^ (3x) A e^ (-15x)+ B	e^ (-3x) A e^ (15x)+ B
The solution of the differential equation (D^2- 12D-45)y=0 is	(3x)	e^ (3x)	e^ (-3x)	e^ (-3x)	e^ (-3x)
The solution of the unferential equation (b. 2. 125 45)y=0 is	A e^ (-10x)+ B e^	` '	A e^ (10x)+ B	A e^ (-10x)+ B	A e^ (10x)+ B
The solution of the differential equation (D^2-7D-30)y=0 is	(-3x)	e^ (-3x)	e^ (3x)	e^ (3x)	e^ (-3x)
The particular integral of (D^2 +19D+60)y= e^x is	(-e^(-x))/80	(e^(-x))/80	(e^x)/80	(-e^x)/80	(e^x)/80
The particular integral of (D^2+25) y= cosx is	(cosx)/24	(cosx)/25	(-cosx)/24	(-cosx)/25	cosx/24
The particular integral of (D^2+25) y= sin4x is	(-sin4x)/9	(sin4x)/9	(sin4x)/41	(-sin4x)/41	(sin4x)/9
The particular integral of (D^2+4) y= sin2x is	(-xsin2x)/4	xsin2x/4	(-xcos2x)/4	xcos2x/4	(-xcos2x)/4
The particular integral of (D^2+1) y= sinx is	xcosx/2	(-xcosx)/2	(-xsinx)/2	xsinx/2	(-xcosx)/2
The particular integral of (D^2 -9D+20)y=e^(2x) is	e^(2x) /6	e^(2x) /(-6)	e^(2x) /12	e^(2x)/(-12)	e ^ (2x) /6
The particular integral of (D^2 +D-72)y= e^(7x) is	e^(7x)/16	e^(-7x)/16	e^(7x)/(-16)	e^(-7x)/(-16)	e^(7x)/(-16)
The particular integral of (D^2-1) y= sin2x is	(-sin2x)/5	sin2x/5	sin2x/3	(-sin2x)/3	(-sin2x)/5
The particular integral of (D^2+2) y= cosx is	(-cosx)	(-sinx)	cosx	sinx	COSX
The particular integral of (D^2- 7D-30)y= 5 is	(1/30)	(-1/30)	(1/6)	(-1/6)	(-1/6)
The particular integral of (D^2- 12D-45)y= -9 is	(-1/5)	(1/5)	(1/45)	(-1/45)	(1/5)
					A e^ (14x)+ B
The solution of the differential equation (D^2- 11D-42)y=21 is	(-1/42)	(1/42)	(1/2)	(-1/2)	e^ (-3x)
The particular integral of (D^2+1) y= 2 is	1	2	-1	-2	2