

KARPAGAM ACADEMY OF HIGHER EDUCATION

(Deemed to be University Established under Section 3 of UGC Act 1956) Pollachi Main Road, Coimbatore – 641 021, Tamil Nadu

Department of Mathematics

| Subject : Mathematical Statistics Practical III | Semester III | LTPC |
|---|-----------------------------|------|
| Subject Code : 16MMP311 | Class : II M.Sc Mathematics | 4004 |

List of Practical:

- 1. Introduction to SPSS Package
- 2. Working with windows in SPSS
- 3. Defining variables in variable view window in SPSS
- 4. Drawing of graphs and diagrams in SPSS Package
- 5. Standard deviation for individual and discrete series using SPSS Package.
- 6. Standard deviation continuous series using SPSS Package.
- 7. Coefficient of variation for individual and discrete series using SPSS Package.
- 8. Calculation of Mean and variance for binomial distribution using SPSS Package.
- 9. Calculation of Mean and variance for Poisson distribution using SPSS Package.
- 10. Karl Pearson's Correlation using SPSS Package.
- 11. Rank Correlation Coefficient using SPSS Package.
- 12. Testing Hypothesis using t test in SPSS Package.
- 13. Testing Hypothesis using Z test in SPSS Package.
- 14. Testing Hypothesis using chi-square test in SPSS Package.
- 15. Interpretation of results in the SPSS output viewer.



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| Sl. No. | Question | | | | | | | | | |
|---------|--|--|----------------|----------|---------|------------|-----------|----------|----------|----------------|
| | a) Discuss in detail what do you mean by Data View and Variable View | | | | | | | | | |
| 1 | b) You are asked to draw up Marks(X) and Age (Y) for 20 imaginary data and | | | | | | | | | |
| | calculate correlation for the data. | | | | | | | | | |
| | Mr. Gowtham, F | Perso | nal Ma | nager is | s conce | rned ab | out abs | enteeis | m. He | decides to |
| | sample the record | rds to | o deter | nine if | absente | eeism is | s distril | outed e | venly t | hroughout |
| | the six-day wor | the six-day work-week. The null hypothesis to be tested is: absenteeism is | | | | | | | | |
| | distributed evenl | y thr | oughou | it the w | eek. Th | e samp | le resul | ts are a | s follov | vs: |
| | | Ι | Day | | Nun | ber of | absent | ees | | |
| | | N | /Ionday | | | 12 | 2 | | | |
| 2 | | Γ | luesday | | | 9 |) | | | |
| | | V | Vednes | day | | 1 | 1 | | | |
| | | Γ | <u>'hursda</u> | у | | 10 | 0 | | | |
| | | F | riday | | | 9 |) | | | |
| | | Saturday | | | 9 | | | | | |
| | Using χ^2 test | of | signific | ance, c | comput | $e \chi^2$ | value. | Is the | null ł | ypothesis |
| | rejected? Note: 7 | The l | evel of | signific | ance is | 0.01 an | nd table | value | is 15.08 | 6. |
| | The heights of F | athei | rs (X) a | nd their | Sons (| Y) are g | given b | elow. C | Calculat | e Spearman's |
| 2 | Rank Correlation | n Co | efficien | t. | | | | | | |
| 3 | | Х | 180 | 155 | 170 | 174 | 160 | 172 | 166 | |
| | - | Y | 170 | 165 | 180 | 180 | 164 | 169 | 170 | |
| | Certain pesticide | e is p | backed | into ba | gs by a | a machi | ine. Ra | ndom s | samples | of 10 bags are |
| 4 | drawn and their | conte | ents are | found t | o weig | h (in kg | g) as fol | lows. | _ | _ |
| 4 | 50 49 52 44 45 48 46 45 49 45 | | | | | | | | | |
| | Test if the average packing can be taken to be 50 kg. | | | | | | | | | |
| | a) Bring out the Data Entry Procedures in SPSS. | | | | | | | | | |
| | b) Draw a Pie diagram for the following data. | | | | | | | | | |
| | | Year Sales in Units | | | | | | | | |
| 5 | | | | Uni | t I | 200 | C | | | |
| | | | | Unit | Π | 120 | C | | | |
| | | | | Unit | II | 130 | 0 | _ | | |
| | | | | Unit | IV | 180 | C | | | |

Question Paper

| | Calculat | e the e | xpecte | d frequ | uency | y for th | e follo | wi | ng da | ata fo | or th | e gi | ven a | ttribu | ites, | |
|----|---|-------------------|---------------|-------------------------|-------------|--|---------------------|-------------------|----------------|----------------|---------------|------------|------------------------|--------|--------------|----|
| | condition | ns of h | o <u>me a</u> | nd con | ditio | ns of c | hild as | in | deper | nden | t. | | | _ | | |
| | | | | | | | Con | diti | ions | of H | ome | 9 | | | | |
| | | | | ~ | | | | C | lean | | D | irty | 7 | | | |
| 6 | | | Cor | dition | 15 (| Clean | | 7 | 0 | | 50 |) | | | | |
| | | | OI C | niid |] | Fairly | | 8 | 0 | | 20 | 0 | | | | |
| | | | | | _ | Clean | | | | | | | | | | |
| | 2 | | | |] | Dirty | | 3 | 5 | | 4 | 5 | | | | |
| | Use χ^2 te | est at 5 | <u>% leve</u> | l to sta | ate w | hether | the tw | 08 | attrib | utes | are i | inde | pende | ent. | | |
| _ | Find the | Mean | and St | andarc | 1 Dev | viation | for the | e gi | iven l | belov | <i>w</i> da | ita s | $\frac{\text{et.}}{2}$ | 20 | ٦ | |
| | | A C | 10 | 12 | 14 | · 10 | 18 | _ | 20 | 22 | 2 | 4 | 26 | 28 | _ | |
| | Colculat | I o Donk | Corro | Jation | / for tl | 12 | 13 n volu | | 12 | 11 | 1 | 0 | 0 | 3 | | |
| | Very 1 2 3 4 5 6 7 8 | | | | | | | | | | | | | | | |
| 8 | Produc | rtion | 100 | $\frac{2}{102}$ | 104 | 1 10 | 7 104 | 5 | 112 | 10 | 3 | 99 | _ | | | |
| | Unemp | loved | 15 | 102 | 13 | 11 | 10. | , | 12 | 10 |) | 26 | | | | |
| | Explain | the fea | tures c | f Corr | elatio | on and | calcul | ate | Cor | elati | on o | coef | ficien | t for | the | |
| 0 | following data. | | | | | | | | | | | | | | | |
| 9 | Х | 52 | 63 | 4 | 5 | 36 | 72 | | 65 | | 47 | | 25 | | | |
| | Y | 62 | 53 | 5 | 1 | 25 | 79 | | 43 | | 60 | | 33 | | | |
| | Certain | pestici | de is p | acked | into | bags | by a r | nac | chine | . Ra | ndoi | m s | ample | es of | 10 bags an | e |
| 10 | drawn ar | nd their | r conte | nts are | e foui | nd to v | veigh (| in | kg) a | s fol | low | s. | | | | |
| _ | 50 Tract if d | 49 | 52 4 | 44 4 - 1-: | 5 4 | 8 4 | 6 45 | 4 | 9 4 | -5 | | | | | | |
| | Colculat | <u>e aver</u> | age pa | tondo | can c | e take | n to be | $\frac{2}{2}$ | J Kg. | ina | data | | | | | |
| 11 | M | arks | | 20 | 30 | 4 | $) \qquad 5$ | $\frac{1}{10}$ | 6 | $\frac{1}{0}$ | uata 7(|) | | | | |
| 11 | Marks 20 30 40 50 60 70 No of Students 8 12 20 10 6 4 | | | | , | | | | | | | | | | | |
| | Calculate | e Corre | elation | coeffi | cient | for th | e follo | wii | ng da | ta: | - | | | | | |
| 12 | Age (X | () 5 | 2 | 63 | 45 | 36 | 5 7 | 2 | 6 | 5 | 4 | 7 | 25 | | | |
| | BP (Y) |) 6 | 2 | 53 | 51 | 25 | 5 7 | 79 | 4 | 3 | 6 | 0 | 33 | | | |
| | Accordin | ng to th | ne IQ l | evel a | nd th | e ecor | omic | cor | nditio | ns o | f the | eir h | omes | s 1000 | 0 students a | at |
| | a col | llege v | vere o | raded | Use | χ^2 te | est to t | find | d out | wh | ethe | r th | ere is | s anv | associatio | m |
| | betw | een ec | onomi | c cond | ition | at hor | ne and | IO |). | | etiie | 1 11 | 010 1 | , any | ussociulio | |
| | | | | Ecor | nomie | с | IO | | | | - | | | | | |
| 13 | | | | Con | ditior | is | High | | Low | 1 | Tota | al | | | | |
| | | | | Rich | 1 | | 460 | | 140 | | 600 | | | | | |
| | | | | Poor | • | | 240 | | 160 | | 400 | | | | | |
| | POOL | | | | 1 | | 240 | | 200 | | 100 | 0 | _ | | | |
| | | | | | | | | | | | | | | | | |
| | (<i>IVOl</i> | ind our | t the re | <i>y sign</i> lation | hetu | $\frac{1}{1000}$ is $\frac{1}{10000000000000000000000000000000000$ | J.UJ (ll Iarketi | <i>ו</i> מו חס | and s | valle Sales | $\frac{1}{1}$ | J.ð the | +). follo | wing | data | — |
| 14 | | $\frac{1100}{28}$ | $\frac{1}{1}$ | | 38 | 35 | 33 | <u>11g</u> 4(| $\frac{1}{10}$ | 32 | 36 | | 33 | wing | uata. | |
| 11 | Y 2 | 23 3 | 34 3 | 3 3 | 34 | 30 | 26 | 28 | 8 3 | 31 | 36 | , | 38 | | | |
| | Certain | brand of | of rice | is pac | ked i | nto ba | gs by a | ı m | achir | ne. R | and | om | samp | les of | 15 bags ar | ·e |
| 15 | drawn a | nd thei | r conte | ents ar | e fou | nd to v | weigh | (in | kg) a | s fo | llow | s. | -1 | | | |
| 15 | 50 49 | 52 | 44 4 | 45 48 | 8 4 | 6 45 | 49 | 4 | 5 5 | 0 52 | 2 5 | 54 | 53 5 | 51 | | |
| | Test if the average packing can be taken to be 50 kg. | | | | | | | | | | | | | | | |

Mathematical Statistics – Practical - III

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(Deemed to be University Established Under Section 3 of UGC Act 1956)

POLLACHI MAIN ROAD, EACHANARI (PO), COIMBATORE –641 021



Enable | Enlighten | Enrich (Deemed to be University) (Under Section 3 of UGC Act 1956)

DEPARTMENT OF MATHEMATICS

M.Sc Mathematics

| Name of the Course | : Mathematical Statistics Practical - III |
|--------------------|---|
| Course Code | : 16MMP311 |
| Year | : II Year |
| Semester | : III Semester |
| Class | : II M.Sc Mathematics |

INDEX

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INTRODUCTION TO SPSS PACKAGE

Objective

To understand how SPSS package is useful for the purpose of data analysis.

Introduction

Originally it is an acronym of "Statistical Package for the Social Science" but now it stands for "Statistical Product of Service Solution".

One of the most popular statistical packages which can perform highly complex data manipulated and analysis with simple instruction.

The Four Windows

- ✤ Data Editor
- ✤ Output Viewer
- ✤ Syntax Editor
- Script Window

The Basic Analysis of SPSS Frequencies

The Analysis produces frequency table showing frequency counts and percentage of the values of individual variable.

Descriptive

This analysis shows the maximum, minimum, mean and standard deviation of the variables.

Correlation and Linear Regression Analysis

Association between correlation and linear regression estimates the co-efficient of the linear equation.

Chi-Square, ANOVA, T-Test

Independence (cross table), Frequency (Goodness of fit) one way and two way ANOVA and test.

WORKING WITH WINDOWS IN SPSS

Objectives

To understand how the windows in SPSS work.

The Four Windows

Data Editor Output Viewer Syntax Editor

Script Window

Data Editor

Spread sheet like system for defining entering, editing and displaying data, extension of the saved file will be 'save'.

Output Viewer

Displaying output and errors, extension of the saved file will be 'SPV'.

Syntax Editor

Text editor for syntax composition extension of saved file will be 'SPS'.

Script Window

To provides the opportunity to write full-blown programs in a basic like language. Tex editor for syntax composition extension of saved file will be 'SBS'.

WORKING WITH VARBIALE VIEW WINDOW IN SPSS

Objective

To know how to define variables in the variable view in data editor view.

Opening SPSS

Start \rightarrow All programs \rightarrow SPSS Inc \rightarrow SPSS.

There are two sheets in the window.

- Data View
- Variable View

Data View Window

The data view window.

This sheet is visible when you first open the data editor and this sheet contains the data.

Click on the tab labeled variable view.

Variable View Window

This sheet contains information about the data set that is stored with the data set.

Name

The first character of the variable name must be alphabetic.

Variable names must be unique, and have to be less than 64 characters. Spaces are NOT allowed.

Type

Click on the "type" box .The two basic types of variables that you will use are numeric and string. This column enables you to specify the type of variable.

Width

Width allows you to determine the number of character SPSS will allow to be entered for the variable.

Decimals

Number of decimals.

It has to be less than or equal to 16.

Label

You can specify the details of the variable.

You can write characters with spaces upto 256 characters.

Values

This is used and to suggest which numbers represent which categories when the variable represents a category.

Defining The Value Label

Click the cell in the value column.

For the value, and the label, you can put upto 60 characters.

After defining the values click add and then click OK.

DRAWING OF GRAPHS AND DIAGRAMS IN SPSS PACKAGE

Objective

To know how to draw graphs and diagrams in SPSS package.

Algorithm

Step 1: Start \rightarrow All program \rightarrow SPSS Inc \rightarrow SPSS

Step 2: Enter the given data in the variable view.

Step 3: Click Analysis \rightarrow Descriptive statistics \rightarrow Frequency

Step 4: Click gender and put it into the variable box.

Step 5: Click chart \rightarrow Bar / Pie chart and continue.

Step 6: Finally click ok in the frequency box.

Problem

How would you put the following information into SPSS?

| NAME | GENDER | HEIGHT |
|---------|--------|--------|
| Juanita | 2 | 5.4 |
| Sally | 2 | 5.3 |
| Donna | 2 | 5.6 |
| Sabrina | 2 | 5.7 |
| John | 1 | 5.7 |
| Mark | 1 | 6 |
| Eric | 1 | 6.4 |
| Bruce | 1 | 5.9 |
| | | |

Value 1: Represents Male

Value 2: Represents Female

SPSS Output

Frequencies

Statistics

Male or Female

| Ν | Valid | 8 |
|---|---------|---|
| | Missing | 0 |

Male or Female

| | | | | Valid | Cumulative |
|-------|------------|-----------|---------|---------|------------|
| | | Frequency | Percent | Percent | Percent |
| Valid | MALE | 4 | 50.0 | 50.0 | 50.0 |
| | FEMAL E | 4 | 50.0 | 50.0 | 100.0 |
| | Total | 8 | 100.0 | 100.0 | |



Frequencies

Statistics

| male or female | , |
|----------------|---|
|----------------|---|

| Ν | Valid | 8 |
|---|---------|---|
| | Missing | 0 |

| - | | | | Valid | Cumulative |
|-------|--------|-----------|---------|---------|------------|
| | | Frequency | Percent | Percent | Percent |
| Valid | MALE | 4 | 50.0 | 50.0 | 50.0 |
| | FEMALE | 4 | 50.0 | 50.0 | 100.0 |
| | Total | 8 | 100.0 | 100.0 | |



CALCULATION OF STANDARD DEVIATION FOR INDIVIDUAL AND DISCRETE SERIES USING SPSS PACKAGE

Objective

To calculate the standards deviation for individual and discrete series using SPSS package.

Algorithm

Step 1: Start \rightarrow all programs \rightarrow SPSS Inc \rightarrow SPSS

Step 2: Enter the given data in the variable view.

Step 3: Click analysis \rightarrow descriptive statistics \rightarrow frequency.

Step 4: click statistic option to choose the standard deviation \rightarrow continue and click ok.

Step 5: Finally we get the output.

Individual Series

Problem

1. Calculate the standard deviation for the data given below using SPSS package.

|--|

Formula:

Standard deviation=
$$\sqrt{\frac{\sum (x-\bar{x})^2}{n}}$$

Discrete Series

2. Calculate the standard deviation for the following data using SPSS package.

| No of Members | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 |
|---------------|---|---|---|---|----|----|---|---|---|----|----|----|
| Frequency | 1 | 3 | 5 | 6 | 10 | 13 | 9 | 5 | 3 | 2 | 2 | 1 |

Formula:

Standard deviation= $\sqrt{\frac{\Sigma f x^2}{\Sigma f} - [\frac{\Sigma f x}{\Sigma f}]^2}$

1. OUTPUT

No. of students

| N | Valid | 9 |
|------|-----------|----------|
| | Missing | 0 |
| Std. | Deviation | 13.14133 |

2. OUTPUT:

No. of members

| Ν | Valid | 60 |
|------|-----------|---------|
| | Missing | 0 |
| Std. | Deviation | 2.35038 |

Inference

Standard deviation for the given data for individual series using SPSS is 13.141. Standard deviation for the given data for discrete series using SPSS is 2.350.

STANDARD DEVIATION CONTINUOUS SERIES

Objective:

To know how to calculate the standard deviation for continuous series using SPSS Package.

Algorithm

STEP 1: Start \rightarrow All programs \rightarrow SPSS inc \rightarrow SPSS.

STEP 2: Enter the given data in the variable view.

STEP 3: Click analysis \rightarrow Descriptive statistics \rightarrow Frequencies.

STEP 4: Click statistic option to choose the mean and standard

Deviation \rightarrow Continue and Click OK.

STEP 5: Finally we get the output.

Problem

Calculate the standard deviation for the following data using SPSS package

| Income | 0-10 | 10-20 | 20-30 | 30-40 | 40-50 | 50-60 | 60-70 |
|---------|------|-------|-------|-------|-------|-------|-------|
| Rs(100) | 6 | 8 | 10 | 12 | 7 | 4 | 3 |

Solution

Given:

| Х | 0-10 | 10-20 | 20-30 | 30-40 | 40-50 | 50-60 | 60-70 |
|---|------|-------|-------|-------|-------|-------|-------|
| f | 6 | 8 | 10 | 12 | 7 | 4 | 3 |

Formula:

Standard deviation= $\sqrt{\frac{\sum fm^2}{\sum f} - \left[\frac{\sum fm}{\sum f}\right]^2}$

Calculation:

| X | f | m | m² | fm | fm² |
|-------|-------|----|---------------------|------------------------|-------|
| 0-10 | 6 | 5 | 25 | 30 | 150 |
| 10-20 | 8 | 15 | 225 | 120 | 1800 |
| 20-30 | 10 | 25 | 625 | 250 | 62500 |
| 30-40 | 12 | 35 | 1225 | 420 | 14700 |
| 40-50 | 7 | 45 | 2025 | 315 | 14175 |
| 50-60 | 4 | 55 | 3025 | 220 | 12100 |
| 60-70 | 3 | 65 | 4225 | 195 | 12675 |
| Σ | _f=50 | | $\sum \text{fm}=15$ | $50 \sum fm^2 = 61850$ | 0 |

Standard deviation =
$$\sqrt{\frac{\sum fm^2}{\sum f} - \left[\frac{\sum fm}{\sum f}\right]^2}$$

| $=\sqrt{\frac{61850}{50}}$ | $-\frac{(1550)^2}{(50)^2}$ |
|----------------------------|----------------------------|
| =\sqrt{1237} | - 961 |
| =\sqrt{276} | |
| =16.613 | |

Output

| N | Valid | 50 |
|--------|-----------|--------|
| | Missing | 0 |
| Mear | 1 | 31.00 |
| Std.] | Deviation | 16.782 |

| | | Frequency | Percent | Valid Percent | Cumulative Percent |
|----------------|-------|-----------|---------|------------------|-----------------------|
| | 5 | 6 | 12.0 | 12.0 | 12.0 |
| | 15 | 8 | 16.0 | 16.0 | 28.0 |
| 25 Valid 45 | 10 | 20.0 | 20.0 | 48.0 | |
| | 12 | 24.0 | 24.0 | 72.0 | |
| | 45 | 7 | 14.0 | 14.0 | 86.0 |
| | 55 | 4 | 8.0 | 8.0 | 94.0 |
| | 65 | 3 | 6.0 | 6.0 | 100.0 |
| | Total | 50 | 100.0 | 100.0 | |

Inference

The standard deviation for the given data for continuous series using SPSS is 16.782.

CALCULATION OF COEFFICIENT OF VARIATION FOR INDIVIDUAL SERIES

Objective

To know how to calculate the coefficient of variation individual and discrete series using SPSS package.

Algorithm

Step 1: Start \rightarrow All programs \rightarrow SPPS in C \rightarrow SPPS.

Step 2: Enter the given data in the variable view.

Step 3: Click Analyze→ Descriptive Statistics→ Frequencies.

Step 4: Click statistics option to choose the mean and standard deviation \rightarrow continue and click ok.

Step 5: Collect the mean and standard deviation values.

Step 6: Click Transforms \rightarrow Compute variables.

Step 7: Enter the target values.

Step 8: Finally find the coefficient of variation.

Step 9: The result will be appeared in data view.

Individual Series

Calculate the coefficient of mean and standard deviation for the given data below:

| X | 25 | 18 | 27 | 10 | 30 | 42 | 20 | 53 | 20 | |
|---|----|----|----|----|----|----|----|----|----|---|
| | | | | | | | | | | - |

Formula

Formula for individual value for mean

Mean = $\sum X/N$

Where N=number of items.

Calculation

| Χ |
|----|
| 25 |
| 18 |
| 27 |
| 10 |
| 30 |
| 42 |
| 20 |
| 53 |
| 20 |
| |

∑X =245

Mean =245/9 = 27.22

Formula

| Standard deviation | $=\sqrt{(\sum X - \overline{X})^2/n}$ | | |
|--------------------|---------------------------------------|---------------|--------------|
| | $=\sqrt{1381.5556/9}$ | =√153.5061778 | =12.38976101 |
| Standard deviation | = 12.39 | | |

Coefficient of variation of individual series value = std dev /mean = 12.39/27.22

= 0.45518

OUTPUT Individual Series

| N Valid | 9 |
|----------------|----------|
| Missing | 0 |
| Mean | 27.2222 |
| Std. Deviation | 13.14133 |

Coefficient of variation is = 0.48

Discrete Series

Calculate the coefficient of variation for the data given below using SPSS

| No. of. Members | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 |
|-----------------|---|---|---|---|----|----|---|---|---|----|----|----|
| Frequency | 1 | 3 | 5 | 6 | 10 | 13 | 9 | 5 | 3 | 2 | 2 | 1 |

Formula

Mean = $\sum f_x / \sum f$

Calculation

| X | F | f _x |
|----|---------------|------------------|
| 1 | 1 | 1 |
| 2 | 3 | 6 |
| 3 | 5 | 15 |
| 4 | 6 | 24 |
| 5 | 10 | 50 |
| 6 | 13 | 78 |
| 7 | 9 | 63 |
| 8 | 5 | 40 |
| 9 | 3 | 27 |
| 10 | 2 | 20 |
| 11 | 2 | 22 |
| 12 | 1 | 12 |
| | $\sum f = 60$ | $\sum f_x = 358$ |

Mean = $\sum f_x / \sum f$ = 358 / 60 = 5.96667 Mean = 5.9 (or) 6.0

Formula

Standard deviation = $\sqrt{\sum} f_x^2 / \sum f - \left[\sum f_x / \sum f\right]^2$

Calculation

| | Χ | X ² | F | f _x | $\mathbf{f}_{\mathbf{x}}^{2}$ | | | |
|-------------|---|-----------------------|---------------|--------------------|-------------------------------|-------|--|--|
| | 1 | 1 | 1 | 1 | 1 | | | |
| | 2 | 4 | 3 | 6 | 12 | | | |
| | 3 | 9 | 5 | 15 | 45 | | | |
| | 4 | 16 | 6 | 24 | 96 | | | |
| | 5 | 25 | 10 | 50 | 250 | | | |
| | 6 | 36 | 13 | 78 | 468 | | | |
| | 7 | 49 | 9 | 63 | 441 | | | |
| | 8 | 64 | 5 | 40 | 320 | | | |
| | 9 | 81 | 3 | 27 | 243 | | | |
| | 10 | 100 | 2 | 20 | 200 | | | |
| | 11 | 121 | 2 | 22 | 242 | | | |
| | 12 | 144 | 1 | 12 | 144 | | | |
| | | | $\sum f = 60$ | $\sum f_x = 358$ | $\sum f_{x^{2}} = 2462$ | | | |
| | | Stan | dard devia | ation $=\sqrt{24}$ | 462 /60 –[358 / | '60]² | | |
| | | | | $=\sqrt{4}$ | ·1.03 –[5.96]² | | | |
| | | | | =\/4 | 1.03 - 35.52 | | | |
| | | | | $=\sqrt{5}$ | .5 | | | |
| | | | | = 2 | .347 | | | |
| Coefficient | Coefficient of variation of discrete series value = std.dev /mean | | | | | | | |
| | | | | = 2 | 2.347 / 5.967 | | | |
| | | | | = | 0.3933 | | | |
| | | | | | | | | |

OUTPUT

| Discrete Series | | | | | | |
|------------------------|---------|--|--|--|--|--|
| N Valid | 60 | | | | | |
| Missing | 0 | | | | | |
| Mean | 5.9667 | | | | | |
| Std. Deviation | 2.35038 | | | | | |

Coefficient of variation is = 0.39

Inference

The coefficient of variation for the given data for individual series is 0.48

The coefficient of variation for the given data for discrete series is 0.39

Ex. No: 08

CALCULATING MEAN AND VARIANCE FOR BINOMIAL DISTRIBUTION USING SPSS PACKAGE

Binomial Distribution

A Random Variable X is said to follow binomial distribution, if its probability mass function is given by

 $P(X=x) = P(x) = \{ nC_x p^x q^{n-x} ; x=0,1,2,...,n \}$ = { 0 ;otherwise}

Hence the two independent constant n and p are known as the 'Parameters' of the distribution .The distribution is completely determined if n and p are known X refer the number of successes.

Problem

Assuming that one in 80 births in a case of twins, calculate the probability of 2(or)more sets of twins on a day when 30 births occurs obtained by using the binomial distribution.

Solution

Probability of twins birth = p = 1/80=0.0125q =1-p =1-0.0125q = 0.9875n=30 Mean = np=30*0.0125=0.375Variance= npq = 30*0.0125*0.9875=0.3703125 Binomial distribution is given by $P(x) = nc_x p^x q^{n-x}$ P (x≥2) =1-p(x<2) $=1-\{p(x=0)+p(x=1)\}$ $=1-\{30 C_0 (0.0125)^0 (0.9875)^{30}+30 C_1 (0.0125)^1 (0.9875)^{29}\}$ $=1-\{1*1(0.9875)^{30}+30(0.9875)^{29}(0.0125)\}$ =1-(0.6839+0.2597)=1-0.9436

P (x≥2) =0.0564

CALCULATION OF MEAN AND VARIANCE FOR POISSON DISTRIBUTION USING SPSS PACKAGE

Poisson Distribution

Poisson distribution was discovered by a French Mathematician-Cum-Physicist Simeon Denis Poisson in 1837. Poisson distribution is also a discrete distribution. He derived it as a limiting case of binomial distribution for n-trials. The binomial distribution is $(q+p)^n$. The probability of X successes is given by $P(X=x) = nC_x p^x q^{n-x}$. If the number of trials n is very large and the probability of success 'p' is very small so that the product np=m is non-negative and finite. The probability of x success is given by,

 $P(X=x) = \begin{cases} e^{-m}m^{x}/x! & \text{for } x=0,1,2,\dots\\ 0 & \text{Otherwise} \end{cases}$

Here 'm' is known as parameter of the distribution so that m>0.

Problem

Find the mean and variance to the following data which gives the frequency of the number of deaths due to horse kick in 10 corps per army per annum over twenty years.

X 0 1 2 3 4 Total

F 109 65 22 3 1 200

Obtain by using Poisson distribution.

Solution

Let us calculate the mean and variance of the given data

| Xi | f _i | $\mathbf{f}_{i}\mathbf{x}_{i}$ | $f_i x_i^2$ | |
|-------|----------------|--------------------------------|-------------|--|
| 0 | 109 | 0 | 0 | |
| 1 | 65 | 65 | | |
| 2 | 22 | 44 | 88 | |
| 3 | 3 | 9 | 27 | |
| 4 | 1 | 4 | 16 | |
| Total | 200 | 122 | 196 | |

Mean, $\overline{X} = \sum \frac{fix}{N} = 122/200 = 0.61$ Variance, $\sigma^2 = \sum \frac{fi^2x}{N} \cdot (\overline{X})^2 = 196/200 - (0.61)^2 = 0.61$ Hence, Mean = Variance = 0.61

CALCULATION OF KARL PEARSON CORRELATION USING SPSS PACKAGE

Objective

To find the correlation coefficient by Karl Pearson Correlation Coefficient for the given variables using SPSS package.

Algorithm

- **STEP 1:** Start \rightarrow All Program \rightarrow SPSS Inc \rightarrow SPSS.
- **STEP 2:** Enter the given data in the variable view.
- **STEP 3**: Click analysis \rightarrow Correlate \rightarrow Bivariate click the variable X and Y And put it into the variable box.
- **STEP 4:** Select the check box Karl Pearson Correlation and continue Then click OK in the frequency box.
- **STEP 5**: Finally we get the Output.

Problem

Calculate the Karl Pearson coefficient of correlation between two variables X and Y from the following data.

| Height of Father | 64 | 65 | 66 | 67 | 68 | 69 | 70 |
|------------------|----|----|----|----|----|----|----|
| Height of Sons | 66 | 67 | 65 | 68 | 70 | 68 | 72 |

Formula

$$r = \frac{n \left[\sum dx dy\right]}{\sqrt{\left[\sum (dx)^2 * \sum (dy)^2\right]^2}}$$

| х | dx | dx ² | у | dy | dy² | dxdy |
|----|----|-----------------|----|----|-----|------|
| 64 | -3 | 9 | 66 | -2 | 4 | 6 |
| 65 | -2 | 4 | 67 | -1 | 1 | 2 |
| 66 | -1 | 1 | 65 | -3 | 9 | 3 |
| 67 | 0 | 0 | 68 | 0 | 0 | 0 |
| 68 | 1 | 1 | 70 | 2 | 4 | 2 |
| 69 | 2 | 4 | 68 | 0 | 0 | 0 |
| 70 | 3 | 9 | 72 | 4 | 16 | 12 |

$$\sum dx^{2} = 28$$

$$\sum dy^{2} = 34$$

$$\sum dxdy = 25$$

$$\mathbf{r} = \frac{n \left[\sum dxdy\right]}{\sqrt{\left[\sum (dx)^{2} * \sum (dy)^{2}\right]}}$$

$$= \frac{25}{\sqrt{(28} * 34)}$$

$$\mathbf{r} = 0.81$$

| Correlations | | | | | | | | |
|----------------|-----------------|-----------|-----------|--|--|--|--|--|
| | | Height of | Height of | | | | | |
| | | Father | Sons | | | | | |
| Height of | Pearson | 1 | 810* | | | | | |
| Father | Correlation | 1 | .010 | | | | | |
| | Sig. (2-tailed) | | .027 | | | | | |
| | Ν | 7 | 7 | | | | | |
| Height of Sons | Pearson | 810* | 1 | | | | | |
| | Correlation | .010 | T | | | | | |
| | Sig. (2-tailed) | .027 | | | | | | |
| | Ν | 7 | 7 | | | | | |

OUTPUT

*. Correlation is significant at the 0.05 level (2-tailed).

Inference

 $0.75 \le 0.8 < 1$ strong positive relationship existing between the height of father and the height of son.

Ex. No: 11 CALCULATION OF RANK CORRELATION USING SPSS PACKAGE

Aim: To calculate the given value by Rank correlation coefficient in the package.

Algorithm

STEP 1: Start \rightarrow All program \rightarrow SPSS in c \rightarrow SPSS.

STEP 2: Enter the given data in the variable view.

STEP 3: Click analyze \rightarrow Correlation \rightarrow Bivariate.

STEP 4: Click the variable X and Y, Put it into the variable box.

STEP 5: Select Spearman check box and continues, then click ok in the Bivariate box.

STEP 6: Finally we get the output.

Calculation

Calculate rank correlation coefficient for the following data using SPSS package.

| First exam Score(X) | 88 | 95 | 70 | 60 | 50 | 80 | 75 | 85 |
|-----------------------|----|----|----|----|----|----|----|----|
| Second exam Score (Y) | 84 | 90 | 88 | 55 | 48 | 85 | 82 | 72 |

Formula

$$=1 - \left(\frac{6\Sigma(D^2)}{(N^3 - N)}\right)$$

Where D = Different between X and Y

N = Number of observation

Calculation

| Χ | Y | RX | RY | D=(RX-RY) | $D = (RX - RY)^2$ |
|----|----|----|----|-----------|-------------------|
| 88 | 84 | 2 | 4 | -2 | 4 |
| 95 | 90 | 1 | 1 | 0 | 0 |
| 70 | 88 | 6 | 2 | 4 | 16 |
| 60 | 55 | 7 | 7 | 0 | 0 |
| 50 | 48 | 8 | 8 | 0 | 0 |
| 80 | 85 | 4 | 3 | 1 | 1 |
| 75 | 82 | 5 | 5 | 0 | 0 |
| 85 | 72 | 3 | 6 | -3 | 9 |
| | | | | | $\Sigma D^2 = 30$ |

$$=1 - \left(\frac{6\Sigma(D^2)}{(N^3 - N)}\right)$$

$$=1-\left(\frac{6(30)}{(8^3-8)}\right)$$

$$=1 - \left(\frac{180}{8(64-1)}\right)$$

$$=1-\left(\frac{180}{504}\right)$$

=1-0.3571 = 0.6429

SPSS OUTPUT

| | | Correlations | | |
|----------------|--------------------|-----------------|------------|-------------|
| | | | first exam | second exam |
| | | | score x | score y |
| Spearman's rho | first exam score x | Correlation | 1 000 | 643 |
| | | Coefficient | 1.000 | .045 |
| | | Sig. (2-tailed) | | .086 |
| | | Ν | 8 | 8 |
| | second exam score | Correlation | 642 | 1 000 |
| | У | Coefficient | .043 | 1.000 |
| | | Sig. (2-tailed) | .086 | |
| | | Ν | 8 | 8 |

Inference

 $0.25 \le 0.6429 < 0.75$, moderate degree positive relationship existing between the first exam score and second exam score.

TESTING HYPOTHESIS USING T-TEST IN SPSS PACKAGE

Aim

Testing Hypothesis using t-test in SPSS package.

Algorithm

STEP 1: Start All Programs SPSS in C SPSS

STEP 2: Enter the given data in the variable view

STEP 3: Click Analyze Compare means One Sample T-test

STEP 4: Click the Variable X and put it into the variable box

STEP 5: Click options Confidence integral percentage at 95% continue

STEP 6: Put test value 10 ok

STEP 7: Finally we get the out put

Problem

Certain pesticide is packed in to bags be a machine a random sample of 10 days is drawn and their contents are found to weight (in kg) as follows

| | - | | | | | |
|------|-------|-------|-------|------|----|----|
| 50 4 | 49 52 | 44 45 | 48 40 | 6 45 | 49 | 45 |

Test if the average packing can be taken to be 50 kg.

Solution

Null Hypothesis

 $H_0:\mu=50$ kgs in the average packing in 50 kgs

Alternative Hypothesis

H₁:≠50 Kgs [Two Tailed]

Level Of Significance

Let α=0.05

Calculation

$$\overline{X} = \frac{473}{10} = 47.3$$

$$s = \sqrt{\frac{\Sigma(x - \overline{x})^2}{n - 1}} = \sqrt{\frac{64.1}{9}} \quad s = 2.668$$

$$\frac{\overline{X} \quad \overline{X} - \overline{X} \quad (\overline{X} - \overline{X})^2}{50 \quad 2.7 \quad 7.29}$$

$$49 \quad 1.7 \quad 2.89$$

$$52 \quad 4.7 \quad 22.09$$

$$44 \quad -3.3 \quad 10.89$$

$$45 \quad -2.3 \quad 5.29$$

$$48 \quad 0.7 \quad 0.49$$

$$46 \quad -1.3 \quad 1.69$$

$$45 \quad -2.3 \quad 5.29$$

$$49 \quad 1.7 \quad 2.89$$

$$45 \quad -2.3 \quad 5.29$$

$$49 \quad 1.7 \quad 2.89$$

$$45 \quad -2.3 \quad 5.29$$

$$t_0 = \left| \frac{47.3 - 50}{\frac{2.668}{\sqrt{10}}} \right| = \left| \frac{-2.7}{0.343695} \right|$$

 $t_0 = 3.2$

Expected Value

 $t_e = \left| \frac{\bar{x} - \mu}{\frac{s}{\sqrt{n}}} \right|$ follows t-distribution with (10-1) degrees of freedom is 2.262.

OUTPUT

One-Sample Statistics

| | N | Mean | Std. Deviation | Std. Error Mean |
|----------------------|----|---------|-------------------|--------------------|
| weights of pesticide | 10 | 47.3000 | 2.66875 | .84393 |

One-Sample Test

| | | Test Value = 10 | | | | |
|----------------------|--------|-------------------|----------|------------|--------------|-----------------|
| | | | | | 95% Confider | nce Interval of |
| | | | Sig. (2- | Mean | the Dif | ference |
| | t | df | tailed) | Difference | Lower | Upper |
| weights of pesticide | 44.198 | 9 | .000 | 37.30000 | 35.3909 | 39.2091 |

Inference

Since $t_0 > t_e$. H_0 is rejected at 5% level of significance and we conclude that the average packing cannot be taken to be 50 kgs.

TESTING HYPOTHESIS USING Z TEST IN SPSS PACKAGE

Aim

Testing hypothesis using z test in SPSS package.

Algorithm

STEP 1: Start \rightarrow All Program \rightarrow SPPS in C \rightarrow SPPS.

STEP 2: Enter the given data in the variable view.

STEP 3: Click Analyze \rightarrow Compare mean \rightarrow One sample t test.

STEP 4: Click the variable x and put it into the variable box.

STEP 5: Click Option \rightarrow Confidence interval percentage at 95% \rightarrow Continue.

STEP 6: Put test value 100 Ok.

STEP 7: Finally we get the output.

Testing Hypothesis Using Z Test in SPSS Package

Problem

The life time fluorescent bulbs of 100 samples are given below. Test the samples for the expected mean life time of 1600 for 5% level of significance.

| | | | - | |
|-------|------|------|------|------|
| 1450 | 1640 | 1615 | 1638 | 1672 |
| 1455 | 1650 | 1625 | 1639 | 1632 |
| 1460 | 1660 | 1635 | 1659 | 1653 |
| 1470 | 1670 | 1645 | 1679 | 1671 |
| 1480 | 1680 | 1655 | 1689 | 1673 |
| 1490 | 1690 | 1665 | 1673 | 1534 |
| `1500 | 1465 | 1675 | 1556 | 1644 |
| 1510 | 1475 | 1685 | 1458 | 1486 |
| 1520 | 1487 | 1453 | 1468 | 1476 |
| 1530 | 1495 | 1468 | 1567 | 1566 |
| 1540 | 1515 | 1497 | 1648 | 1498 |
| 1550 | 1525 | 1488 | 1623 | 1493 |
| 1560 | 1535 | 1526 | 1674 | 1463 |
| 1570 | 1545 | 1539 | 1684 | 1532 |
| 1580 | 1555 | 1499 | 1673 | 1573 |
| 1590 | 1565 | 1577 | 1494 | 1593 |
| 1600 | 1575 | 1469 | 1591 | 1461 |
| 1610 | 1585 | 1569 | 1593 | 1582 |
| 1620 | 1595 | 1589 | 1573 | 1536 |
| 1630 | 1605 | 1599 | 1582 | 1476 |
| | | | | |

Solution

Given n=100, µ=1600.

Null hypothesis

 $H_0:\mu=1600.$

(i.e) there is no significant difference between the sample mean and population mean.

Alternative hypothesis

 $H_1: \mu \neq 1600.$ (two tailed)

Level of significance:

Let α=0.05

Calculation of statistics

$$Z_{0} = \left| \frac{\bar{x} - \mu}{\frac{s}{\sqrt{n}}} \right| = \left| \frac{1570.73 - 1600}{\frac{73.496}{\sqrt{100}}} \right|$$
$$= \left| \frac{-29.27}{7.3496} \right| = 3.982$$
$$Z_{0} = 3.98$$

Expected value

$$Z_e = Z_0 = \left| \frac{\bar{x} - \mu}{\frac{s}{\sqrt{n}}} \right| \sim N(0, 1) = 1.96 \text{ for } \alpha = 0.05$$

SPSS OUTPUT:

One-Sample Statistics

| | | | Std. | Std. Error |
|--------|-----|---------|-----------|------------|
| | Ν | Mean | Deviation | Mean |
| z test | 100 | 1570.73 | 73.496 | 7.350 |

One-Sample Test

| | Test Value = 100 | | | | | |
|--------|------------------|----|----------|------------|--------------|-----------------|
| | | | | | 95% Confider | nce Interval of |
| | | | Sig. (2- | Mean | the Dif | ference |
| | t | Df | tailed) | Difference | Lower | Upper |
| z test | 200.109 | 99 | .000 | 1470.730 | 1456.15 | 1485.31 |

Inference

Since $Z_0 > Z_e$. We reject the null hypothesis at 5% level of significance and we conclude that there is a significant difference between the sample mean and the population mean.

Ex: No: 14

TESTING HYPOTHESIS USING CHI-SQUARE TEST IN SPSS PACKAG

Objective

Testing hypothesis using chi -square test in SPSS package.

Algorithm

Step 1: start \rightarrow all programs \rightarrow SPSS in c \rightarrow SPSS

Step 2: Enter the given data in the variable view.

Step 3: Click the data \rightarrow weight cases and select the frequency variable.

Step 4: Click analysis \rightarrow nonparametric test \rightarrow one sample test \rightarrow select automatically

compare Observed data to hypothesized and click run.

Step 5: Finally we get the output.

Problem

For goodness of fit the following information is derived from the record of an employee payroll the absenteeism of the employees during the weekdays is given below

| DAYS | ABSENCE |
|-----------|---------|
| Monday | 12 |
| Tuesday | 10 |
| Wednesday | 7 |
| Thursday | 8 |
| Friday | 13 |

Test the distribution of absenteeism is uniform across the week days.

Solution

Null hypothesis

 $H_{\circ}:\mu=\overline{x}$

There is no significance difference between during the absenteeism of weekdays.

Alternative hypothesis

H1:µ≠x

There is a significance difference between the absenteeism of weekdays.

Level of significance

Let α=0.05

Calculation of χ^2 statistics

$$\chi^2 = \sum_{i=1}^n \frac{(O-E)}{E}$$

| 0 | E | O-E | $(O-E)^2$ | $(O-E)^{2}/E$ |
|----|----|-----|-----------|---------------|
| 12 | 10 | 2 | 4 | 0.4 |
| 10 | 10 | 0 | 0 | 0 |
| 7 | 10 | -3 | 9 | 0.9 |
| 8 | 10 | -2 | 4 | 0.4 |
| 13 | 10 | 3 | 9 | 0.9 |

Degrees of freedom

df = (r-1) (c-1) $= (5-1) (2-1) \qquad df = 4$ Expected value: $\chi^2_{e} = 9.488$ $\chi^2_{o} < \chi^2_{e}$

 $\chi_0^{-} < \chi_e^{-}$ 2.6<9.488

OUTPUT

Test Statistics

| | no of absent |
|-------------|--------------|
| Chi-Square | 2.600^{a} |
| df | 4 |
| Asymp. Sig. | .627 |

a. 0 cells (0.0%) have expected frequencies less than 5. The minimum expected cell frequency is 10.0.

Inference

Since $\chi^2_o < \chi^2_e$ we accept the null hypothesis at 5% level of significance and we conclude that there is no significance difference between during the absenteeism of weekdays.

Ex. No: 15 INTERPERTATION OF RESULT IN THE SPSS OUTPUT VIEWER

Representation of data in the form of graphs and diagrams for use for better decision making going through graph and diagram one can easily understand the pattern of data over a period of time and one easily identify the up and downs of the data points by which the decision making is easy.

Standard deviation is measure of the dispersion which is mostly used. It is shows the amount of variation amount the shows in a particular variable .The compare two difference variable coefficient of variation is used with help of standard deviation and coefficient of variation decision making is easy.

When we get the measure of central value are closed each other for difference variables decision making is with the complicated foe such situation standard deviation. It the standard deviation values are consistence in natural. If the standard deviation values is more is shows that the values of seated one to another.

Binomial and Poisson are discrete are discrete probability distribution which gives an idea about how values of distributed .Binomial distribution is when we get only two possible outcomes and Poisson distribution is similar binomial and it is which rare events. The Binomial distribution the mean is calculated by $\mu = n p$ and variance = n pq. But in Poisson distribution the mean and variance $\lambda = n p$.

To measure the relationship between the variable correlation coefficient is used. There is different method but most popularly Karl Pearson correlation coefficient is used for measuring the relationship between quantitative data and spearman Rank correlation is used for measuring relationship between qualitative data. The correlation coefficient (value denoted by r) ranges between -1 to 1.

| r value | Relationship |
|----------------------------|--------------------------|
| 1 | Perfect positive |
| ≥0.75 and<1 | Strong positive |
| ≥ 0.25 and < 0.75 | Moderate degree positive |
| >0 and < 0.25 | Low degree positive |
| 0 | No correlation |
| \geq - 0.25 and < 0 | Low degree negative |
| \geq - 0.75 and < - 0.25 | Moderate degree negative |
| \geq - 0.75 and < -1 | Strong negative |
| -1 | Perfect negative |

The relationship between r-value from the following table.

In Hypothesis tests if the asymptotic significance value is less than the level of significance value (α). We accept the null hypothesis otherwise we reject the null hypothesis.